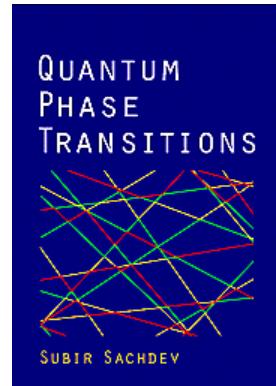


Quantum antiferromagnetism and the high temperature superconductors

Chiranjeeb Buragohain
Anatoli Polkovnikov
Subir Sachdev
Matthias Vojta (Augsburg)

Transparencies on-line at
<http://pantheon.yale.edu/~subir>

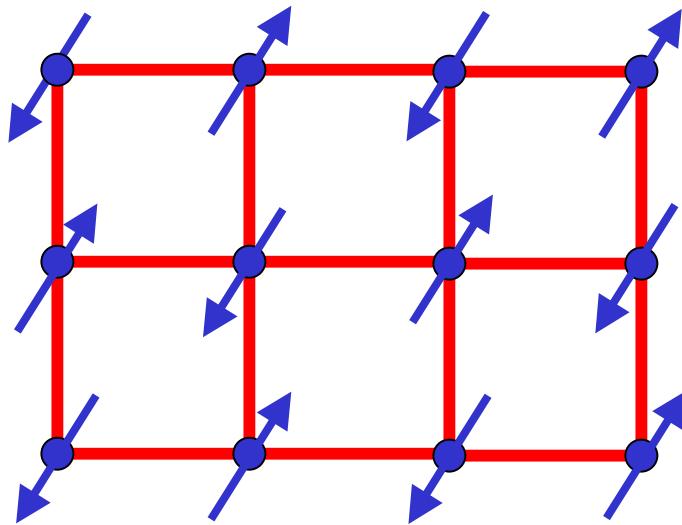
Science **286**, 2479 (1999).



Quantum Phase Transitions
Cambridge University Press

Parent compound of the high temperature superconductors: La_2CuO_4

Square lattice antiferromagnet

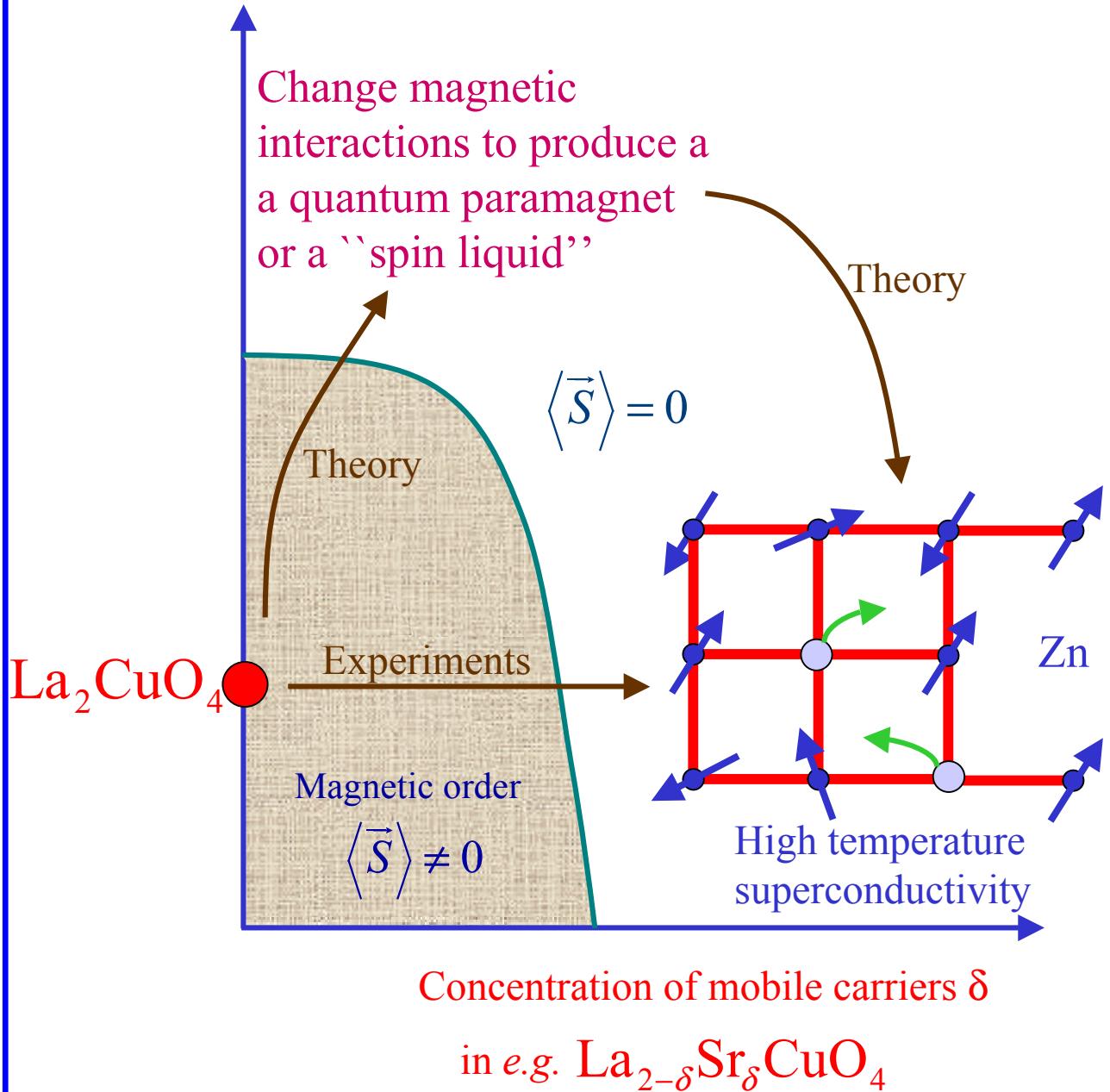


$$H = J_1 \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j$$

Ground state has long-range magnetic (Neel) order

$$\left\langle \vec{S}_i \right\rangle = (-1)^{i_x + i_y} N_0 \neq 0$$





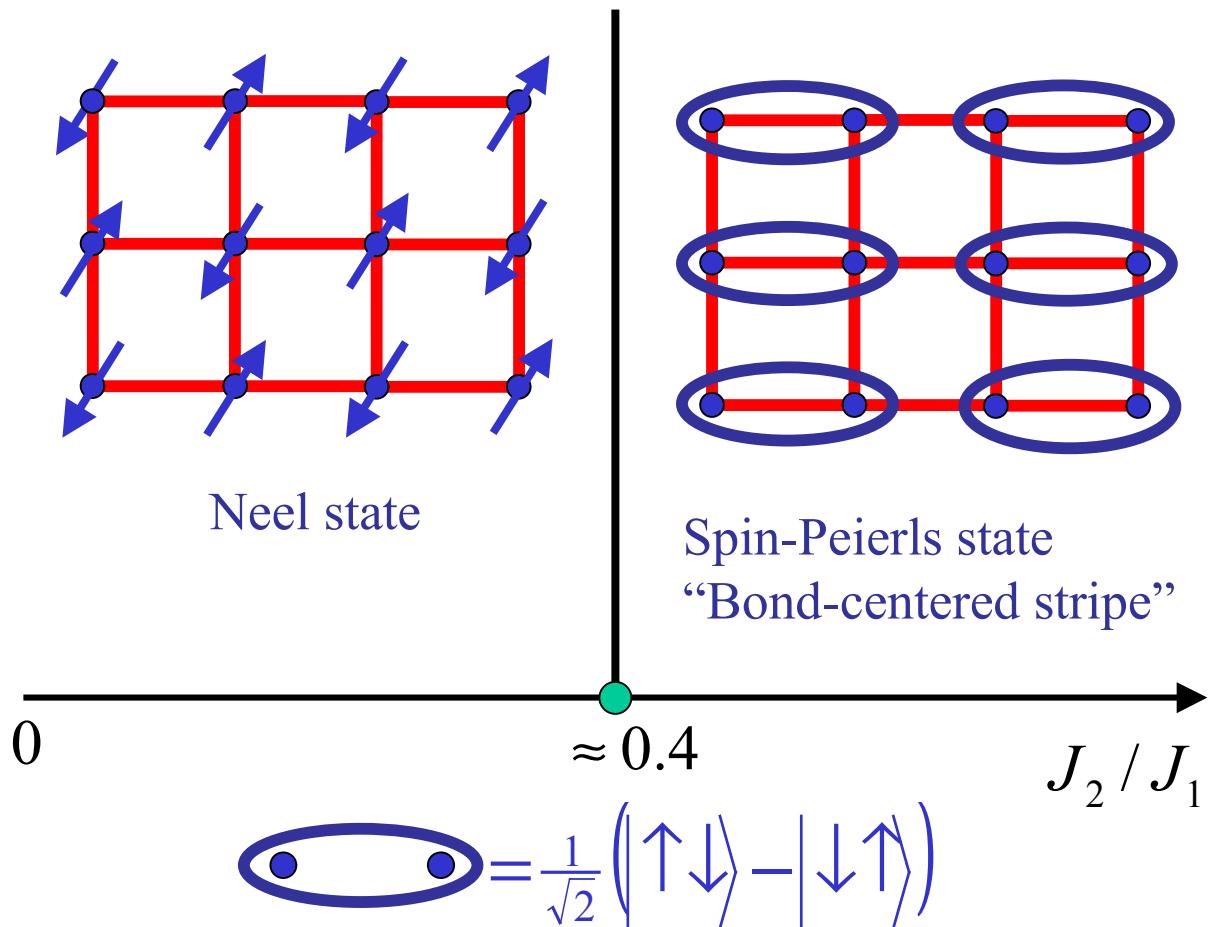
Outline

1. Paramagnetic ground states of two-dimensional antiferromagnets and their response to static non-magnetic impurities.
 - A. Spinon confinement
vs.
 - B. spinon deconfinement
(spin-charge separation)
2. Connection to d-wave superconductors
3. Recent experiments on non-magnetic impurities
 - a. NMR
 - b. Neutron scattering
 - c. Tunneling
4. Conclusions



1. Quantum paramagnets in two dimensional antiferromagnets

Square lattice with first (J_1) and second (J_2) neighbor exchange interactions



N. Read and S. Sachdev, Phys. Rev. Lett. **62**, 1694 (1989)

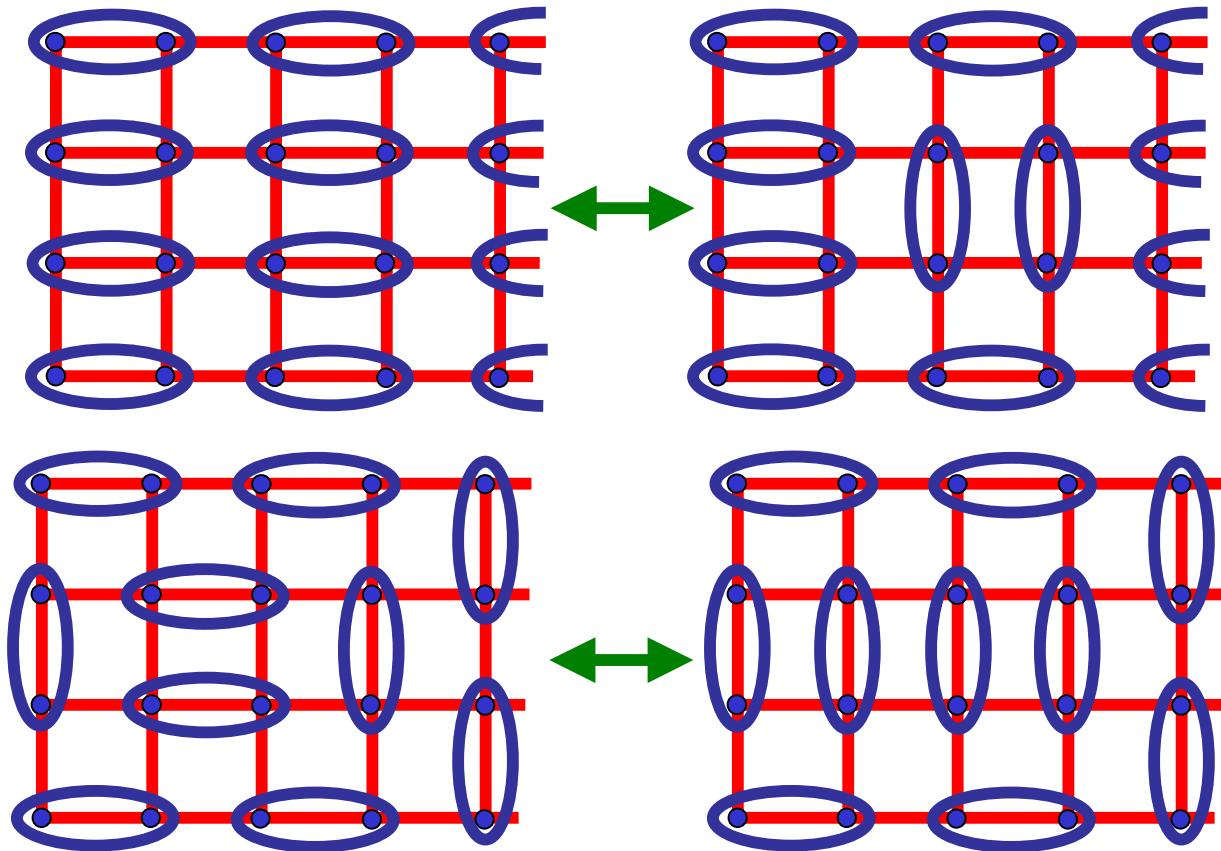
O. P. Sushkov, J. Oitmaa, and Z. Weihong,
condmat/0007329.

M.S.L. du Croo de Jongh, J.M.J. van Leeuwen, W. van
Saarloos, cond-mat/0002116.



Quantum dimer model –

D. Rokhsar and S. Kivelson Phys. Rev. Lett. **61**, 2376 (1988)



Quantum “entropic” effects prefer one-dimensional striped structures in which the largest number of singlet pairs can resonate. The state on the upper left has more flippable pairs of singlets than the one on the lower left. These effects always lead to a broken square lattice symmetry near the transition to the Neel state.

N. Read and S. Sachdev Phys. Rev. B **42**, 4568 (1990).



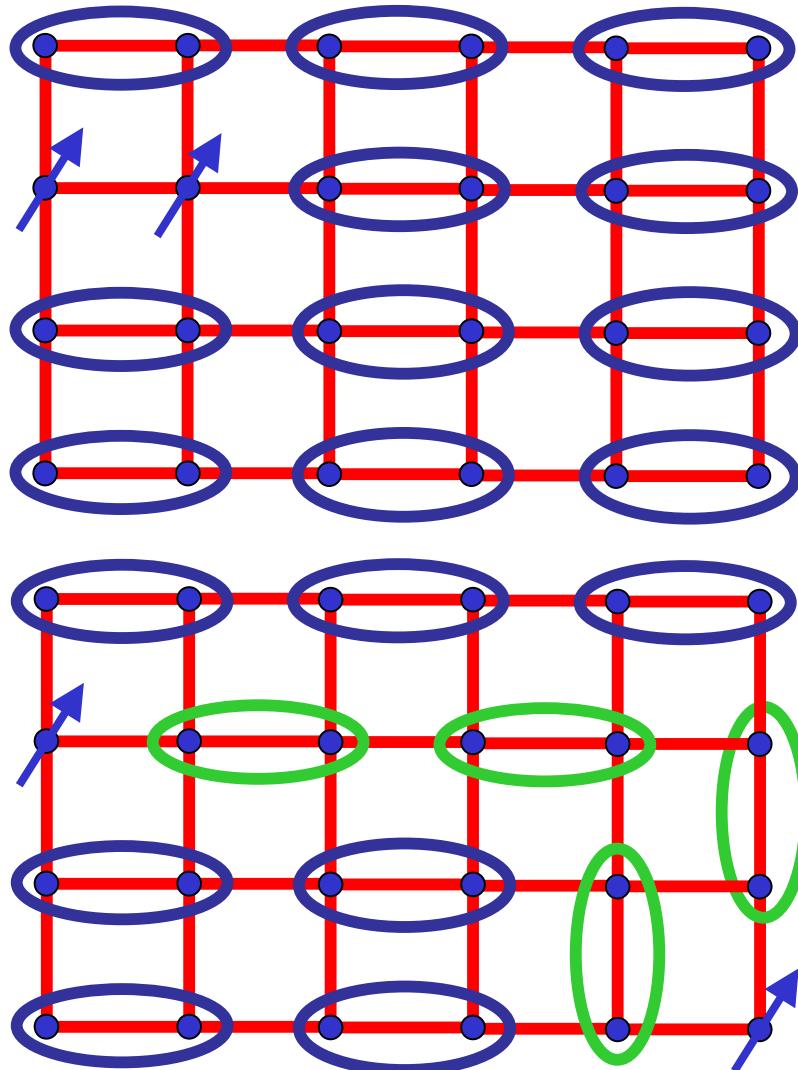
Excitations

Stable S=1 particle

Energy dispersion

$$\varepsilon_k = \Delta + \frac{c_x^2 k_x^2 + c_y^2 k_y^2}{2\Delta}$$

$\Delta \rightarrow$ Spin gap

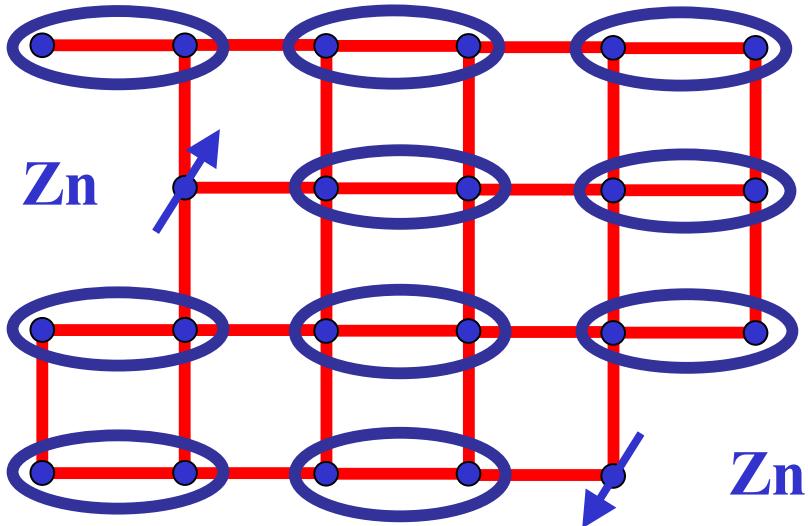
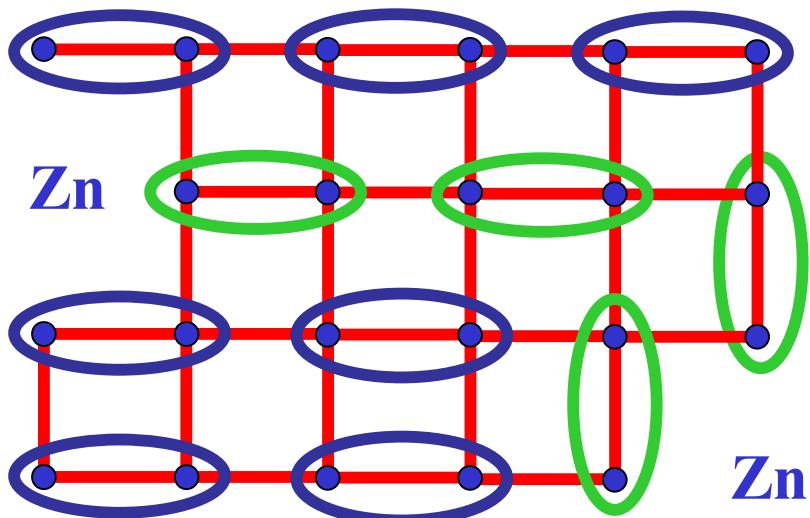


S=1/2 spinons are linearly confined by the line of “defect” singlet pairs between them



Effect of static non-magnetic impurities (Zn or Li)

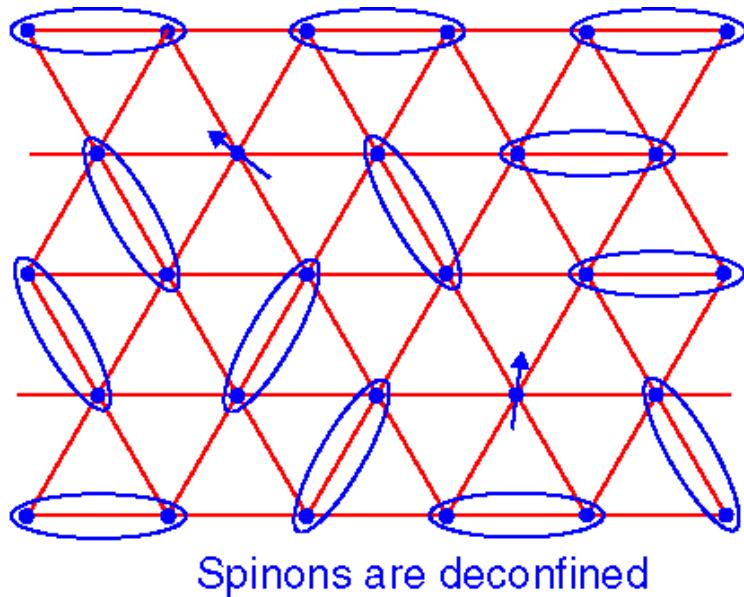
Impurities substitute for Cu ions



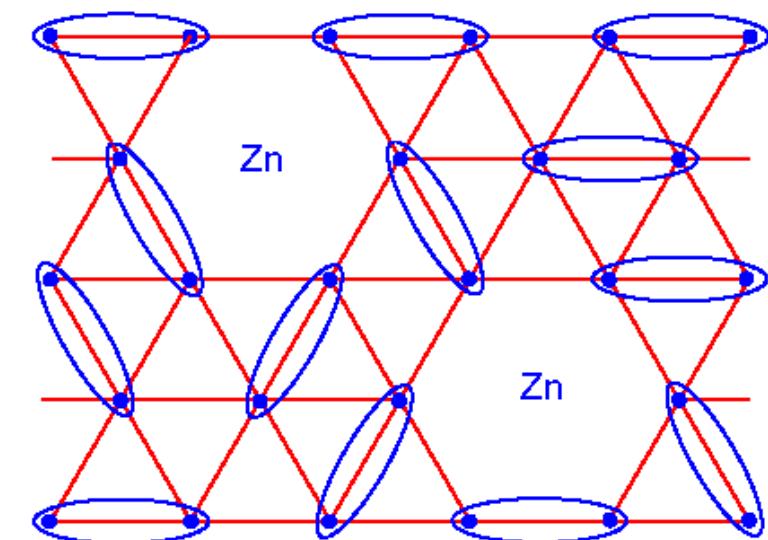
Spinon confinement implies that free $S=1/2$ moments must form near each impurity



B. Paramagnetic ground state with spinon deconfinement



“Spin
Liquid”



Free $S=1/2$ moments need not be present
near the impurities

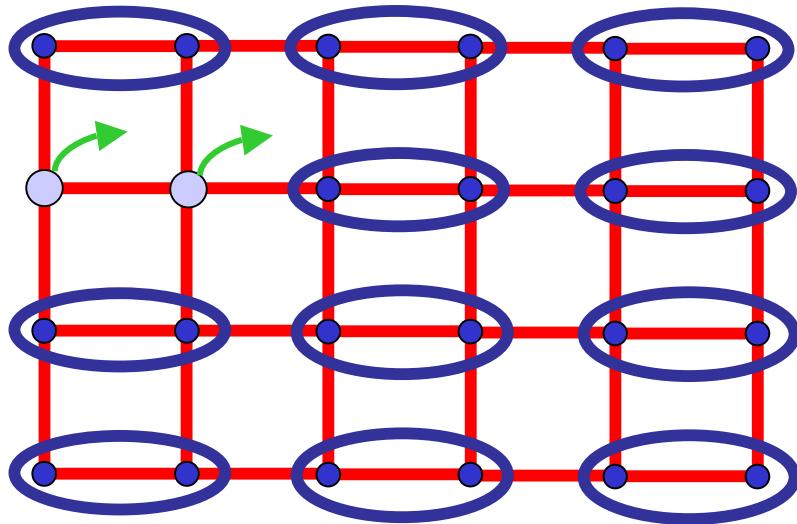
- P. Fazekas and P.W. Anderson, Phil Mag **30**, 23 (1974).
S. Sachdev, Phys. Rev. B **45**, 12377 (1992).
G. Misguich and C. Lhuillier, cond-mat/0002170.
R. Moessner and S.L. Sondhi, cond-mat/0007378.



2. Evolution with density of mobile carriers of density δ

δ is controlled by changing concentration of dopant ions outside the planes containing the Cu spins

A. Doping a paramagnet with confinement



Condensate of hole pairs

E. Fradkin and S. Kivelson, Mod. Phys. Lett B **4**, 225 (1990)
S. Sachdev and N. Read, Int. J. Mod. Phys. B **5**, 219 (1991).

B. Doping a deconfined paramagnet

Single hole condensate

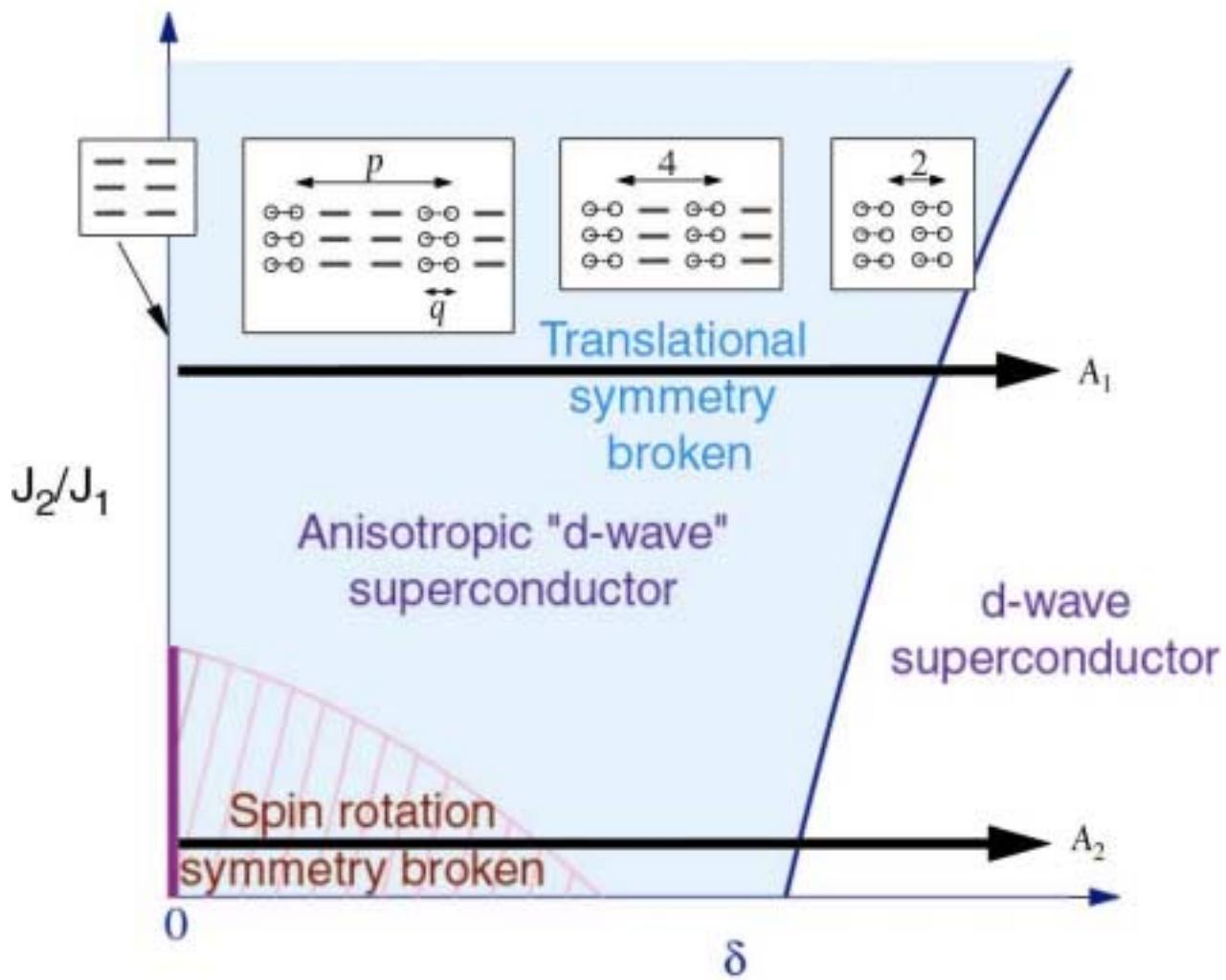
hc/(2e) flux quantum (S. Kivelson, D.S. Rokhsar and J.P. Sethna,
Europhys. Lett. 6, 353 (1988))

Stable hc/e vortices (S. Sachdev, Phys. Rev. B 45, 389 (1992))

+ other exotica (T. Senthil and M.P.A. Fisher,
[cond-mat/0006481](https://arxiv.org/abs/cond-mat/0006481))



Phase diagram for case A

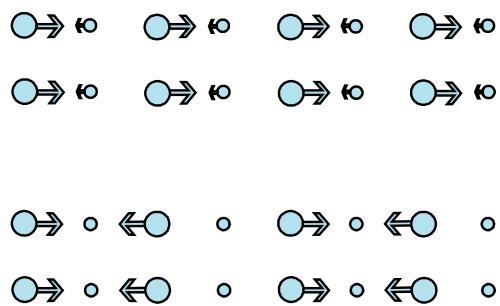


Superconductivity coexists with stripe order

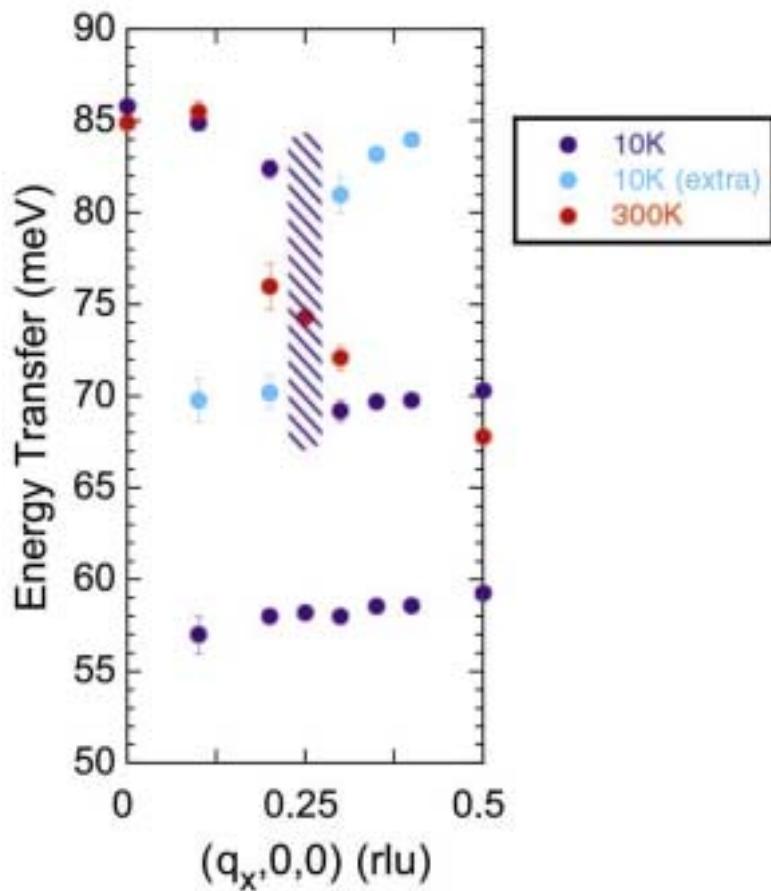
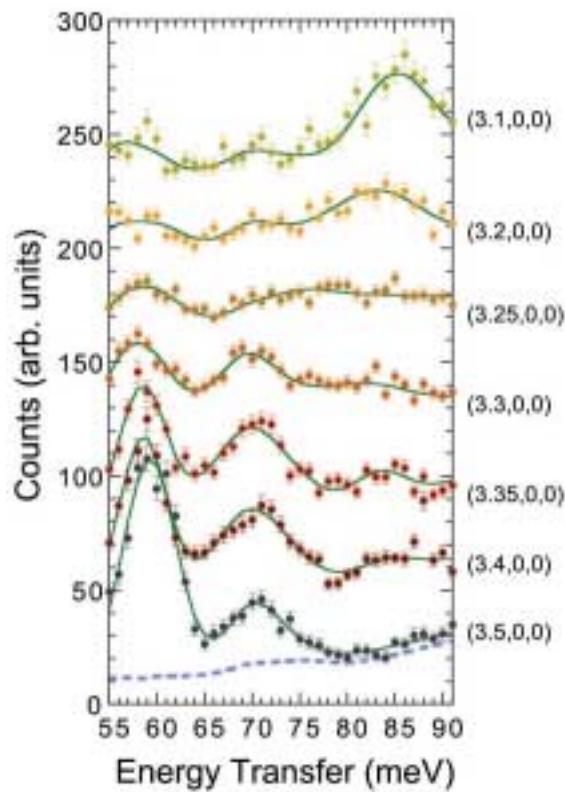


S. Sachdev and N. Read, Int. J. Mod. Phys. B **5**, 219 (1991).
M. Vojta and S. Sachdev, Phys. Rev. Lett. **83**, 3916 (1999).
See also J. Zaanen, Physica C **217**, 317 (1999) and
S. Kivelson, E. Fradkin and V. Emery, Nature **393**, 550 (1998)

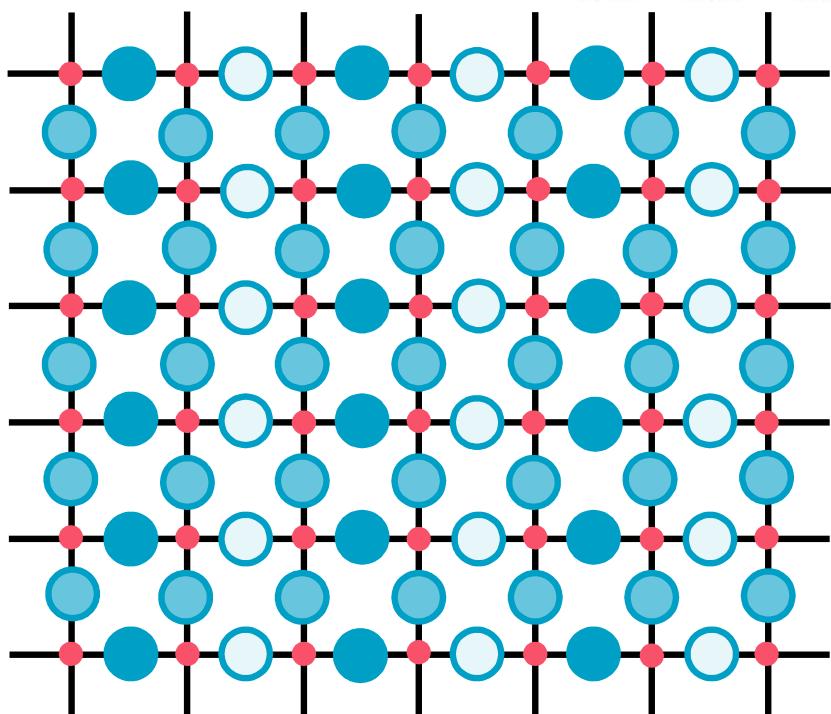
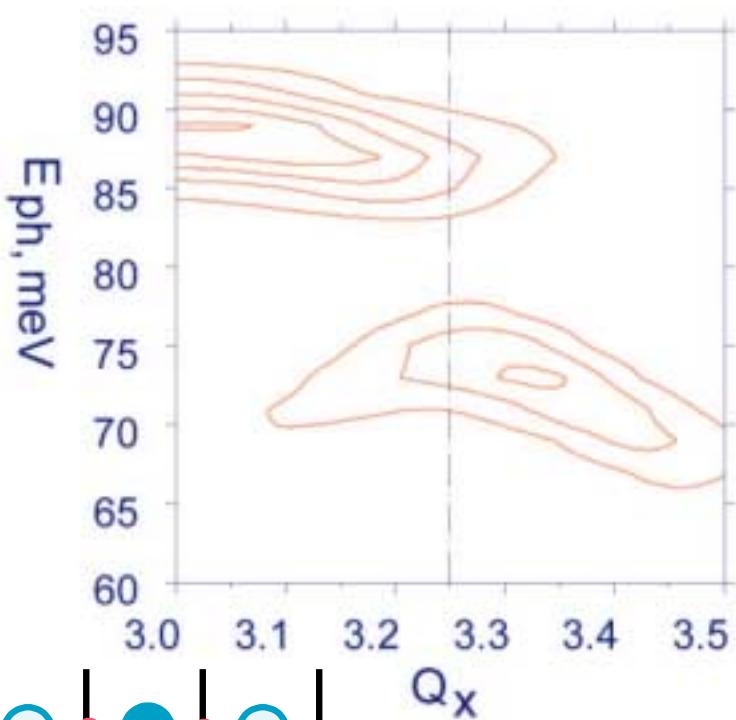
Neutron scattering
measurements of phonon
spectrum of superconducting
 $\text{La}_{1.85}\text{Sr}_{0.15}\text{CuO}_4$ by
R. J. McQueeney, Y. Petrov,
T. Egami, M. Yethiraj,
G. Shirane, and Y. Endoh,
Phys. Rev. Lett. **82**, 628 (1999)



● Oxygen
○ Copper



Computation of phonon spectrum by McQueeney *et al* using a simple model based on lattice modulation below



Evidence for predicted coexistence of
spin-Peierls order and
“d-wave” superconductivity.

S. Sachdev & N. Read, Int. J. Mod. Phys. B 5, 219 (1991).



Zn or Li impurities in doped Mott insulators

Case A



Striped insulator with spinon confinement

d-wave superconductor

Moments form near each Zn or Li.

This moment is quenched at a quantum phase transition at $\delta=\delta_c$.

D. Withoff and E. Fradkin, Phys. Rev. Lett. **64**, 1835 (1990).

C. Gonzalez-Buxton and K. Ingersent, Phys. Rev. B **57**, 14254 (1998).

Case B



Spin liquid with spinon deconfinement

d-wave superconductor

No moments form near Zn or Li ions substituted for Cu and impurity response evolves smoothly

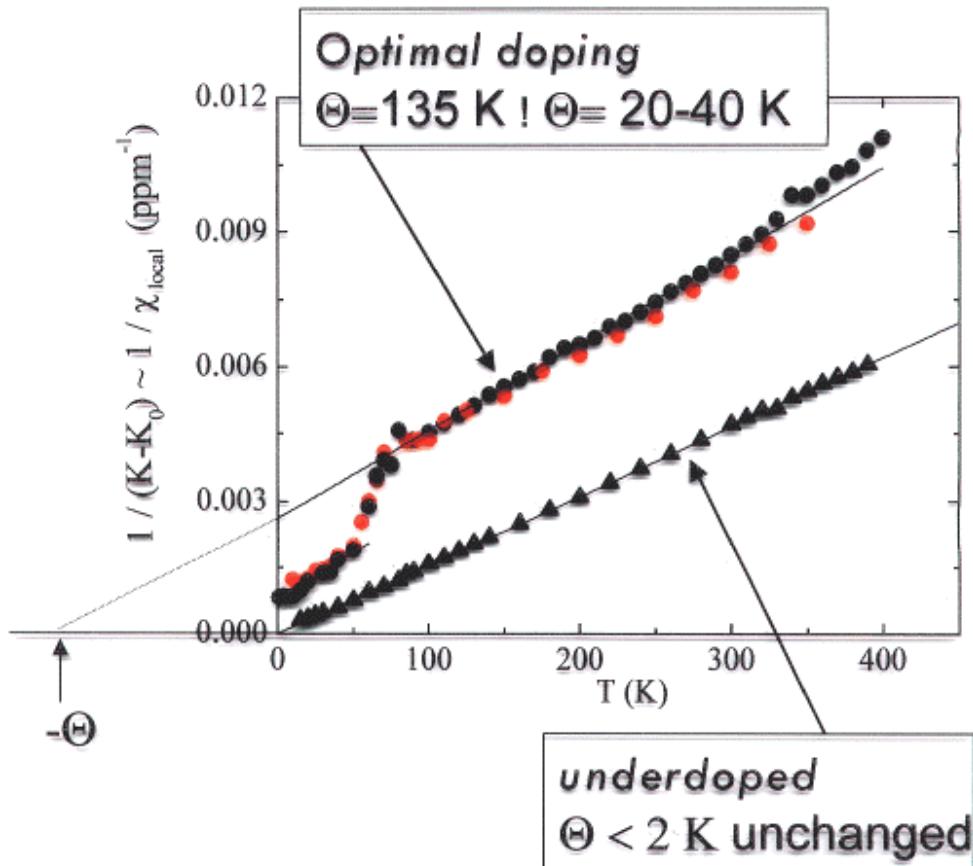


3. Recent experiments

a. NMR

J. Bobroff, H. Alloul, W.A. MacFarlane, P. Mendels, N. Blanchard, G. Collin, and J.-F. Marucco, cond-mat/0010234.

^{7}Li NMR below T_c



Inverse local susceptibility of
isolated Li impurities in YBCO

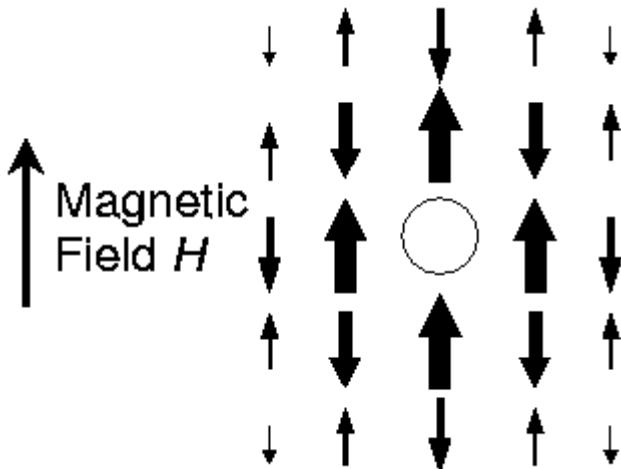


a. NMR

Zn impurity in $\text{YBa}_2\text{Cu}_3\text{O}_{6.7}$

Moments measured by analysis of Knight shifts

M.-H. Julien, T. Feher,
M. Horvatic, C. Berthier,
O. N. Bakharev, P. Segransan,
G. Collin, and J.-F. Marucco,
Phys. Rev. Lett. **84**, 3422
(2000); also earlier work of
the group of H. Alloul and the
original experiment of
A.M Finkelstein, V.E. Kataev,
E.F. Kukovitskii, and
G.B. Teitel'baum, Physica C
168, 370 (1990).

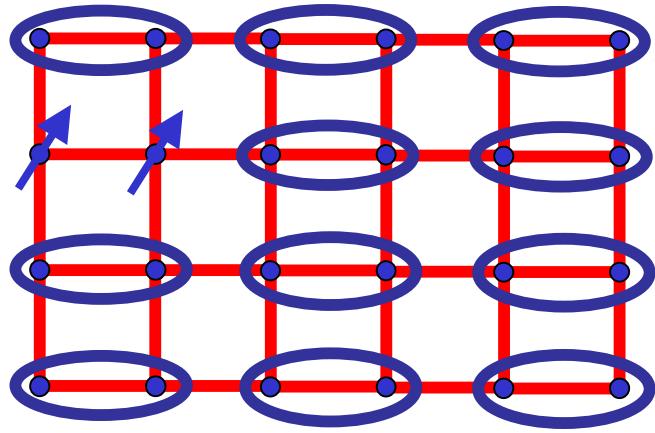


Berry phases of precessing spins do not cancel between the sublattices in the vicinity of the impurity: net uncancelled phase of $S=1/2$



b. Neutron scattering

S=1 resonance mode in YBCO



H.F. Fong, B. Keimer, D. Reznik,
D.L. Milius, and I.A. Aksay,
Phys. Rev. B **54**, 6708 (1996)

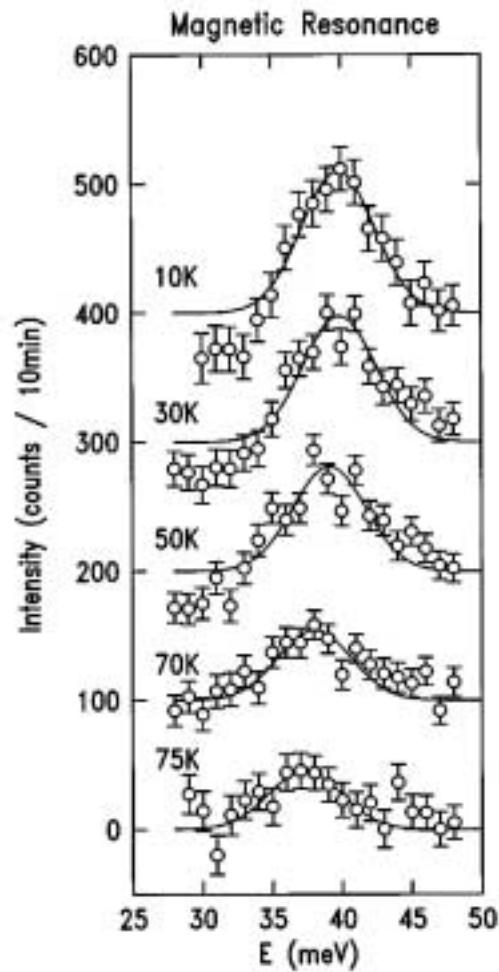


FIG. 8. Unpolarized beam, constant- \mathbf{Q} data [$\mathbf{Q}=(3/2, 1/2, -1.7)$] of the 40 meV magnetic resonance obtained by subtracting the signal below T_c from the $T=100$ K background. The lines are fits to Gaussians, as described in the text. For clarity successive scans are offset by 100.

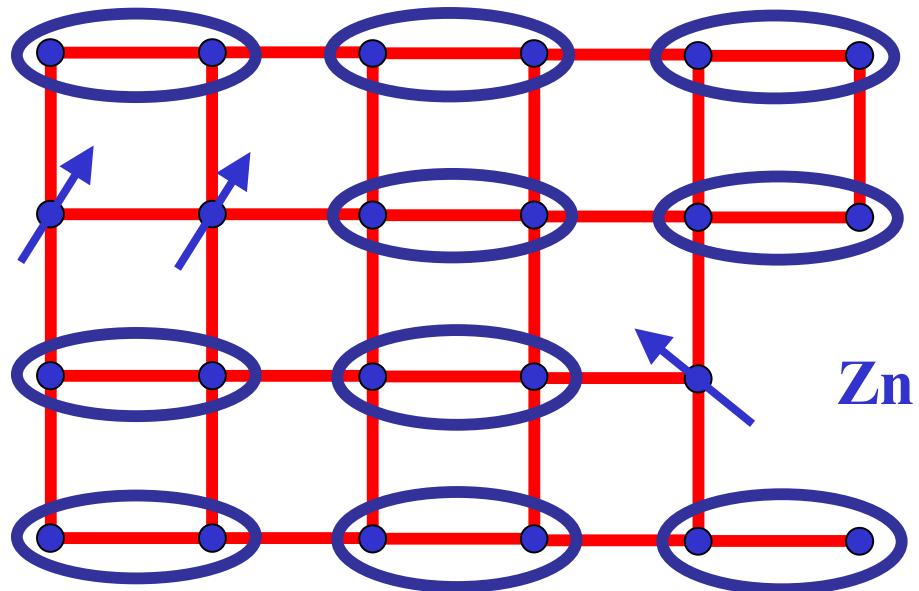
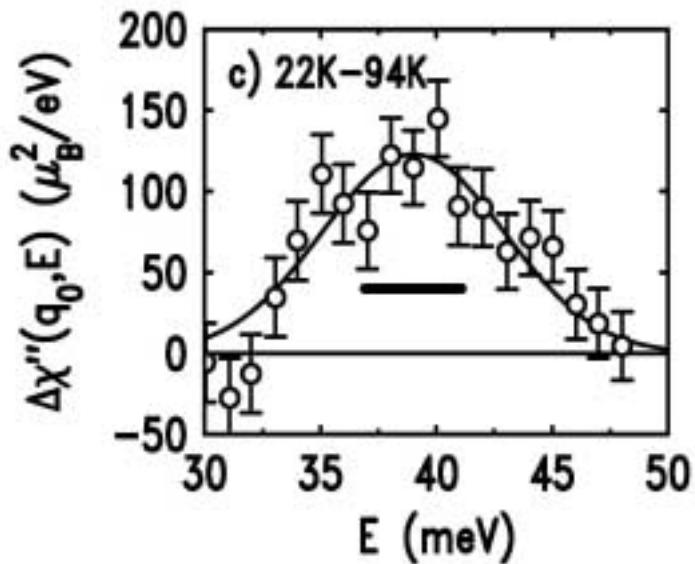
Spin-1 collective mode in $\text{YBa}_2\text{Cu}_3\text{O}_7$ - little observable damping at low T.

Coupling to superconducting quasiparticles unimportant



YBa₂Cu₃O₇ + 0.5% Zn

H. F. Fong, P. Bourges,
Y. Sidis, L. P. Regnault,
J. Bossy, A. Ivanov,
D.L. Milius, I. A. Aksay,
and B. Keimer,
Phys. Rev. Lett. **82**, 1939
(1999)

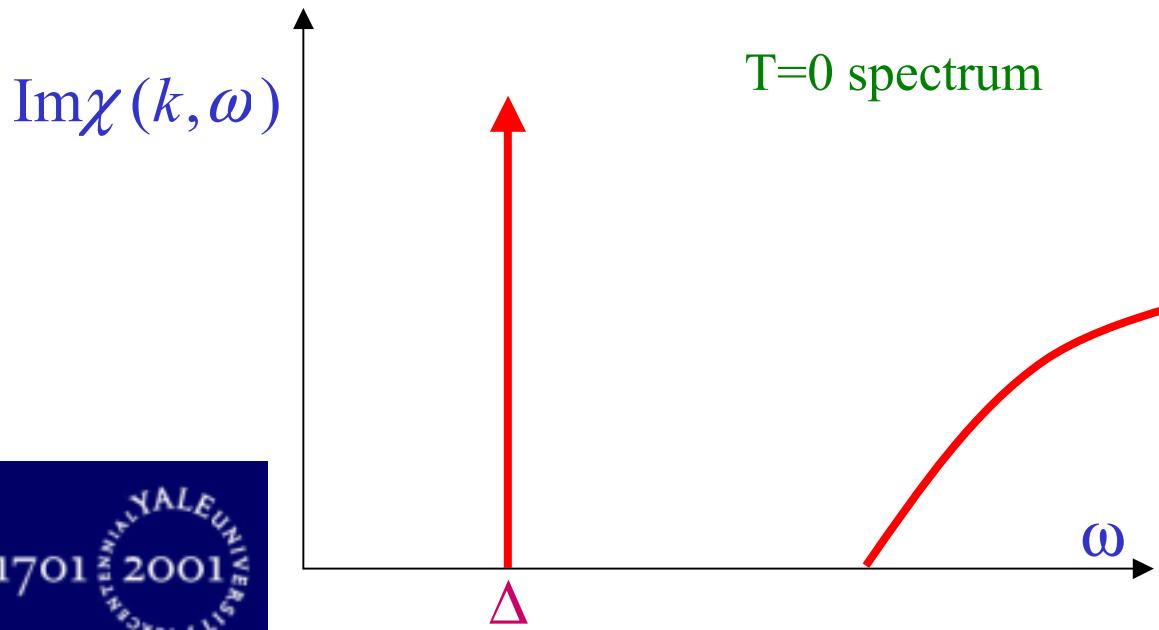


Quantum field theory for S=1 particle near magnetic ordering transition

$$\mathcal{S}_b = \int d^2x d\tau \left[\frac{1}{2} \left((\nabla_x \phi_\alpha)^2 + c^2 (\partial_\tau \phi_\alpha)^2 + r \phi_\alpha^2 \right) + \frac{g}{4!} (\phi_\alpha^2)^2 \right]$$

$\phi_\alpha \rightarrow$ 3-component antiferromagnetic order parameter

Oscillations of ϕ_α about zero (for $r > 0$)
 \rightarrow spin-1 collective mode



Quantum field theory for S=1 resonance in the presence of a non-magnetic impurity

Orientation of “impurity” spin -- $n_\alpha(\tau)$ (unit vector)

Action of “impurity” spin

$$\mathcal{S}_{\text{imp}} = \int d\tau \left[iS A_\alpha(n) \frac{dn_\alpha}{d\tau} - \gamma S n_\alpha(\tau) \phi_\alpha(x=0, \tau) \right]$$

$A_\alpha(n) \rightarrow$ Dirac monopole function

Boundary quantum field theory: $\mathcal{S}_b + \mathcal{S}_{\text{imp}}$

Recall -

$$\begin{aligned} \mathcal{S}_b = \int d^2x d\tau \left[\frac{1}{2} & \left((\nabla_x \phi_\alpha)^2 + c^2 (\partial_\tau \phi_\alpha)^2 + r \phi_\alpha^2 \right) \right. \\ & \left. + \frac{g}{4!} (\phi_\alpha^2)^2 \right] \end{aligned}$$



Renormalization group analysis: g and γ reach non-zero fixed point values

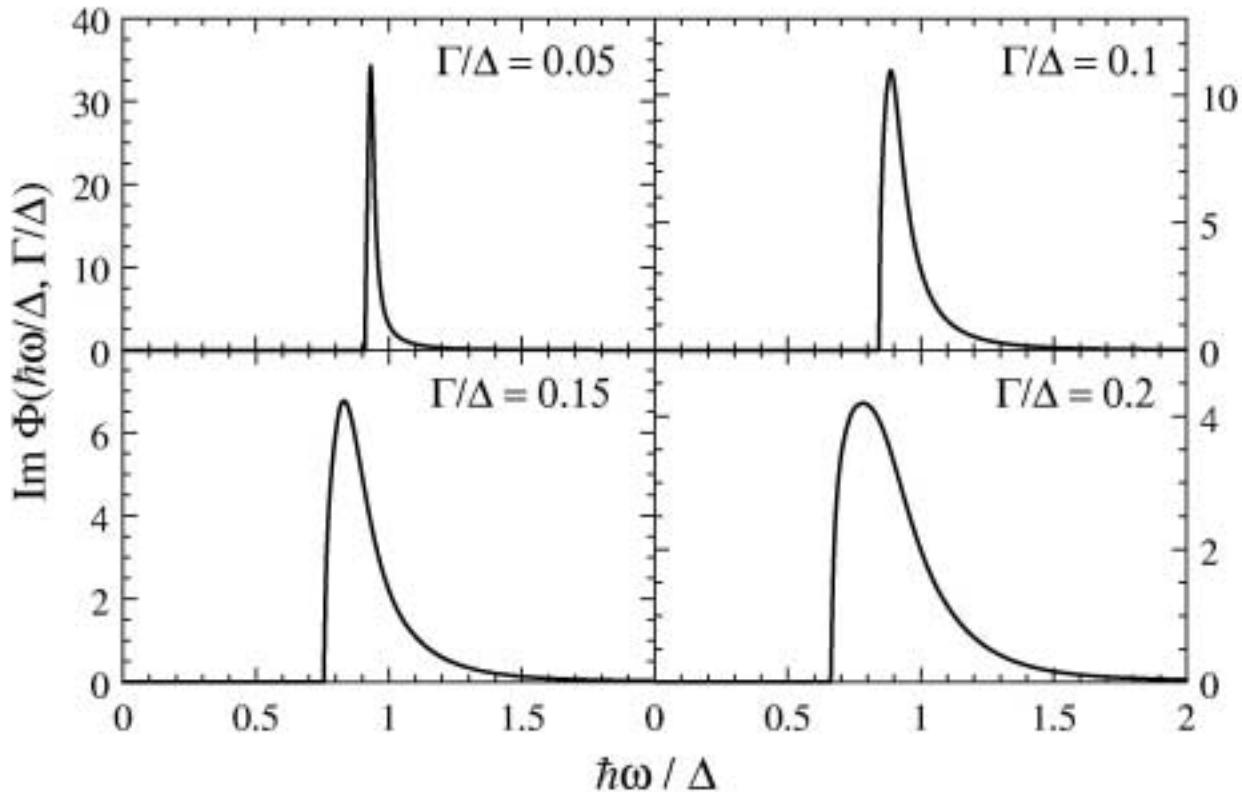
Predictions of quantum field theory

Without impurities $\chi(G, \omega) = \frac{A}{\Delta^2 - \omega^2}$

With impurities $\chi(G, \omega) = \frac{A}{\Delta^2} \Phi\left(\frac{\hbar\omega}{\Delta}, \frac{\Gamma}{\Delta}\right)$

$$\Gamma \equiv \frac{n_{\text{imp}} (\hbar c)^2}{\Delta}$$

$\Phi \rightarrow$ Universal scaling function. We computed it in a “self-consistent, non-crossing” approximation



Predictions: Half-width of line $\approx \Gamma$

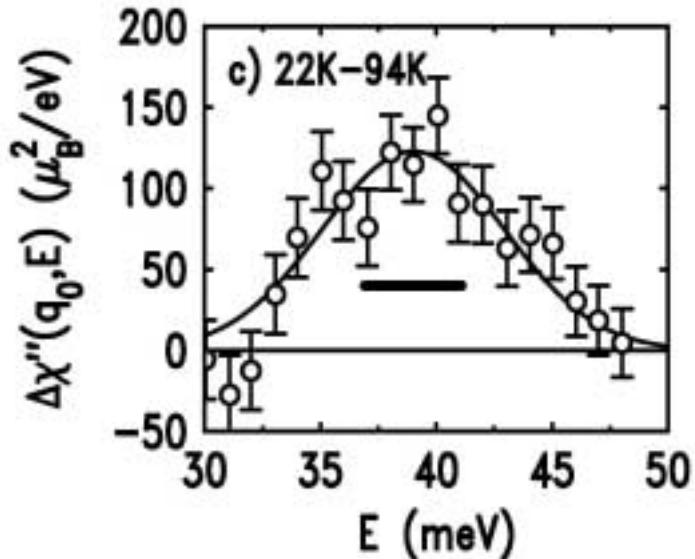
Universal asymmetric lineshape



S. Sachdev, C. Buragohain, M. Vojta, Science **286**, 2479 (1999)
 M. Vojta, C. Buragohain, and S. Sachdev,
 Phys. Rev. B **61**, 15152 (2000).

YBa₂Cu₃O₇ + 0.5% Zn

H. F. Fong, P. Bourges,
Y. Sidis, L. P. Regnault,
J. Bossy, A. Ivanov,
D.L. Milius, I. A. Aksay,
and B. Keimer,
Phys. Rev. Lett. **82**, 1939
(1999)



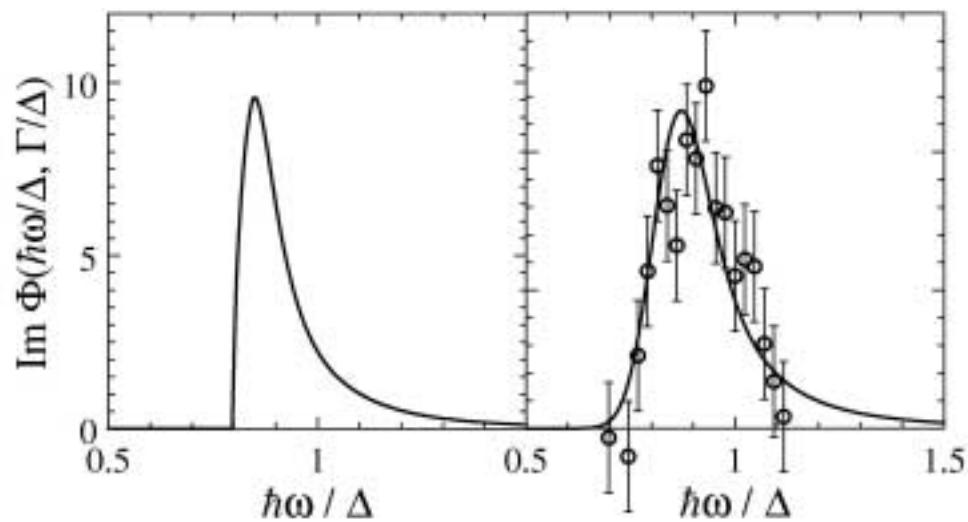
$$n_{\text{imp}} = 0.005$$

$$\Delta = 40 \text{ meV}$$

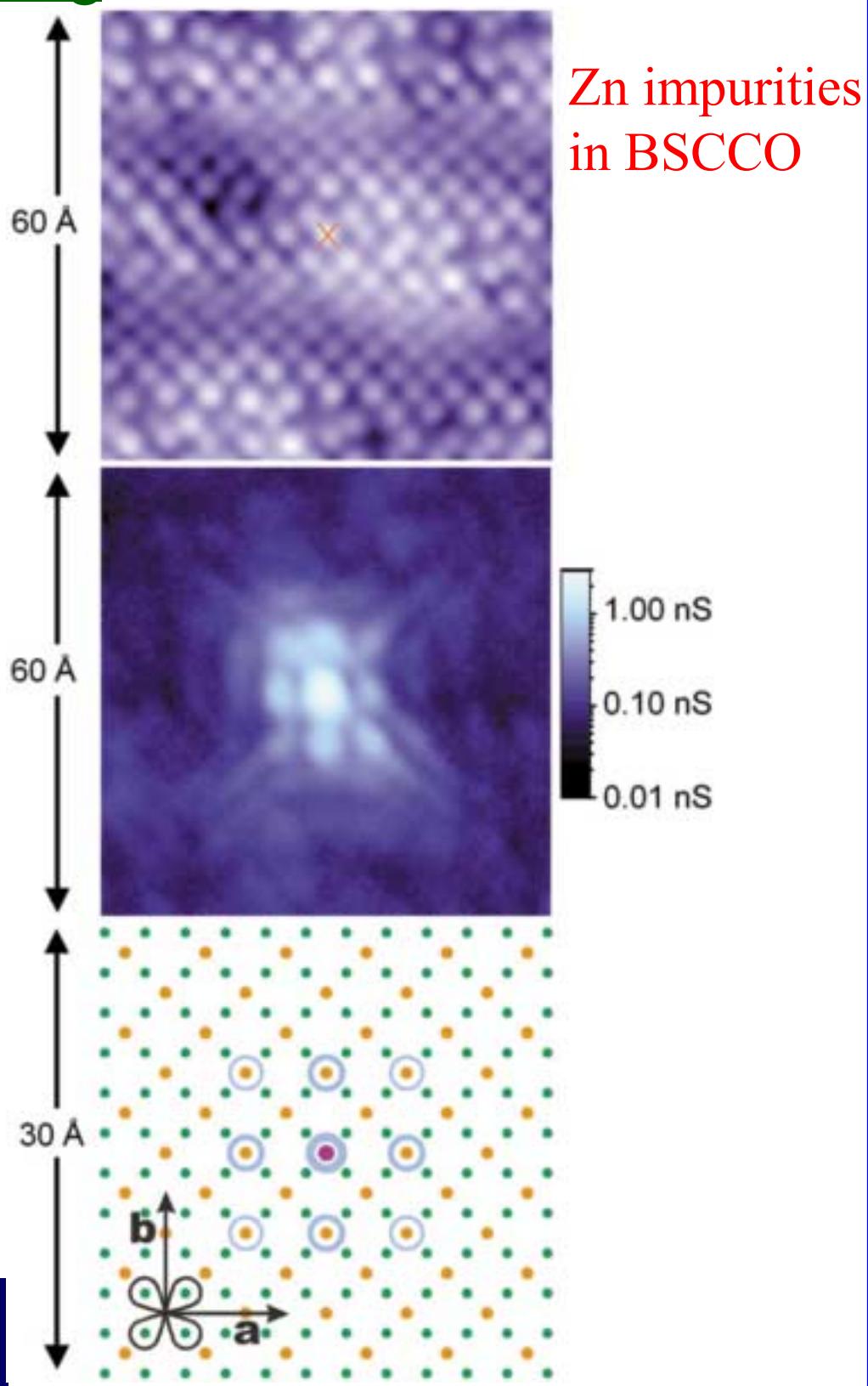
$$\hbar c = 0.2 \text{ eV}$$

$$\Rightarrow \Gamma = 5 \text{ meV}, \Gamma/\Delta = 0.125$$

Quoted half-width = 4.25 meV

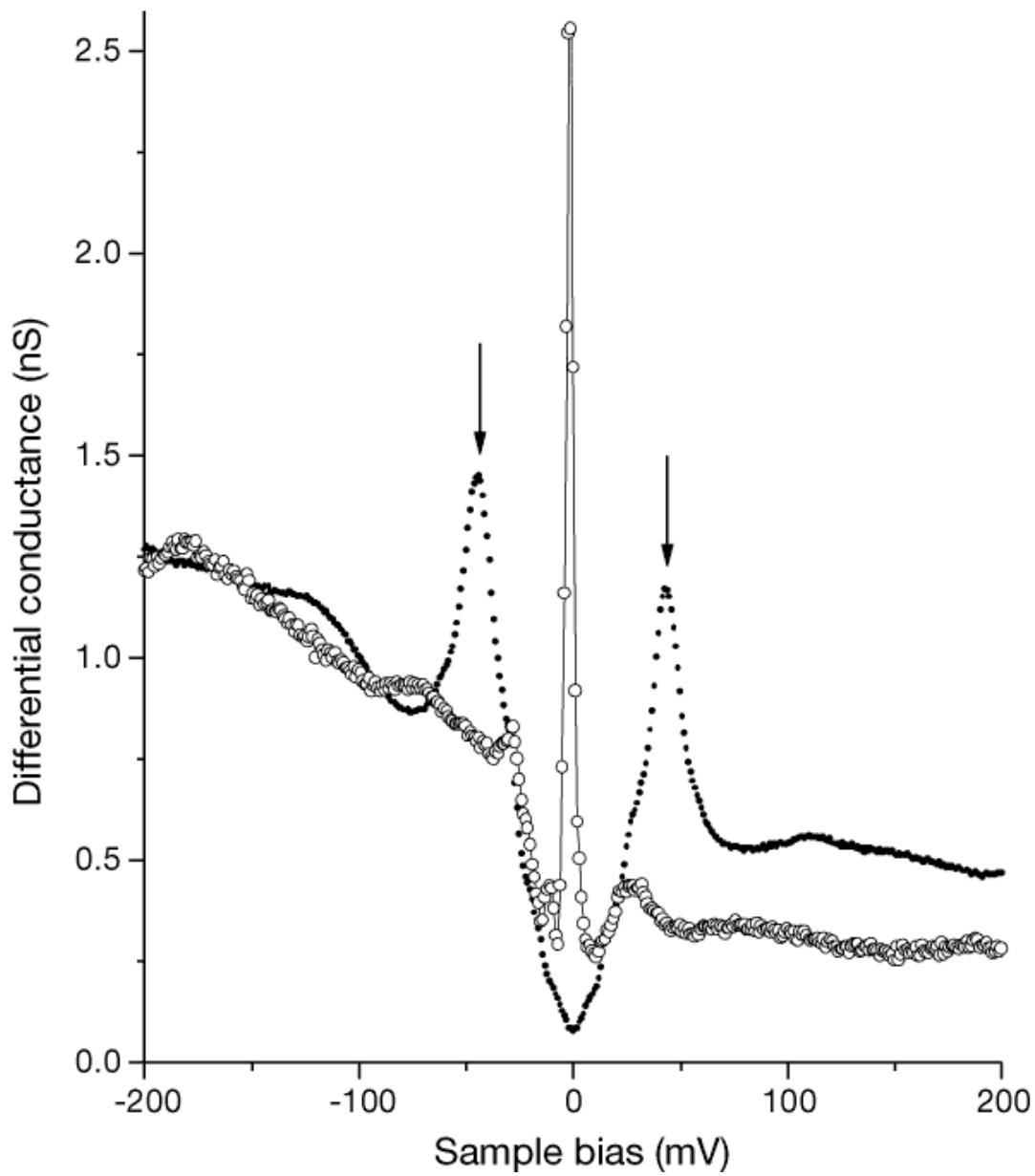


c. Tunneling



S. H. Pan *et al* Nature 403, 746 (2000)

c. Tunneling

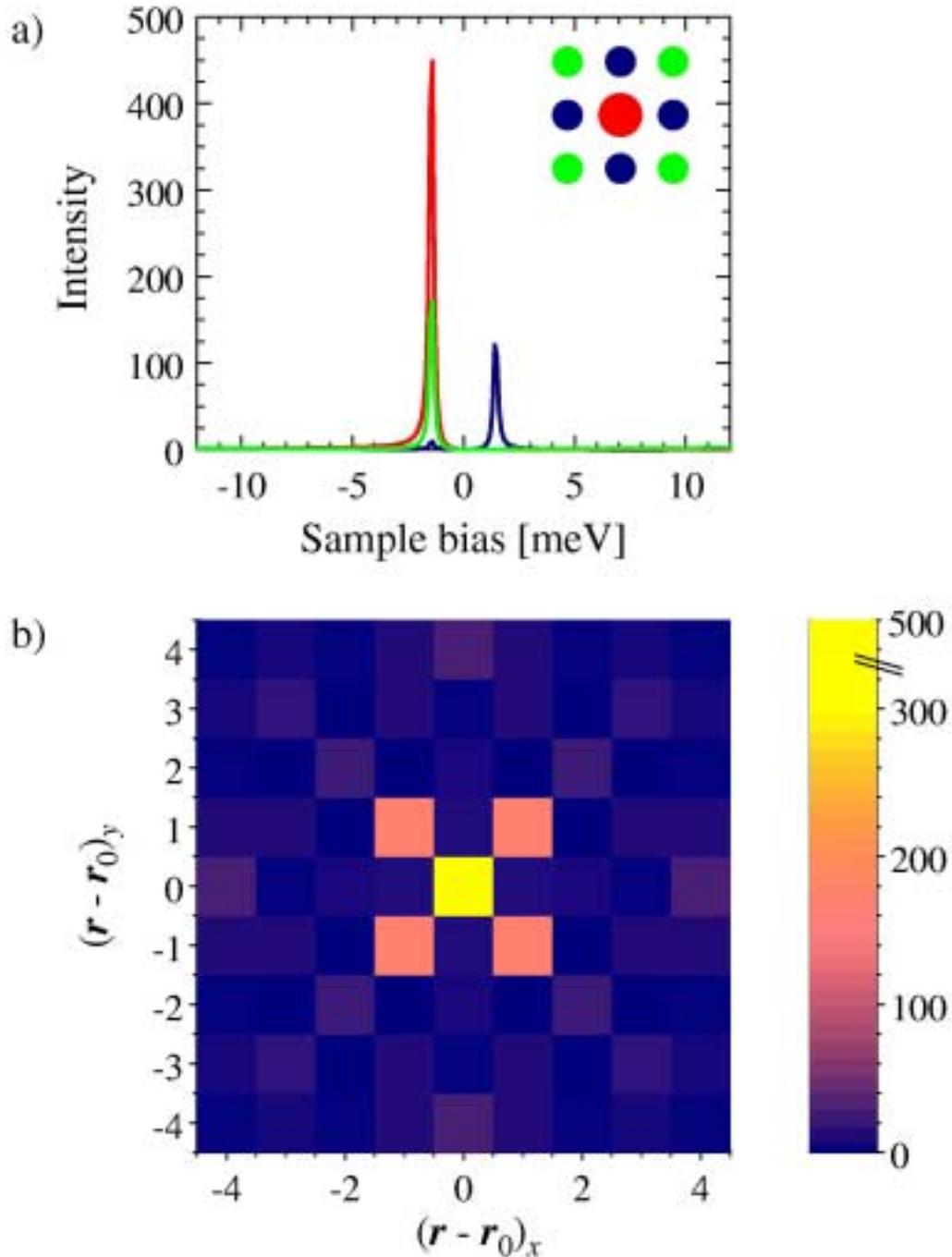


Zn impurity in BSCCO



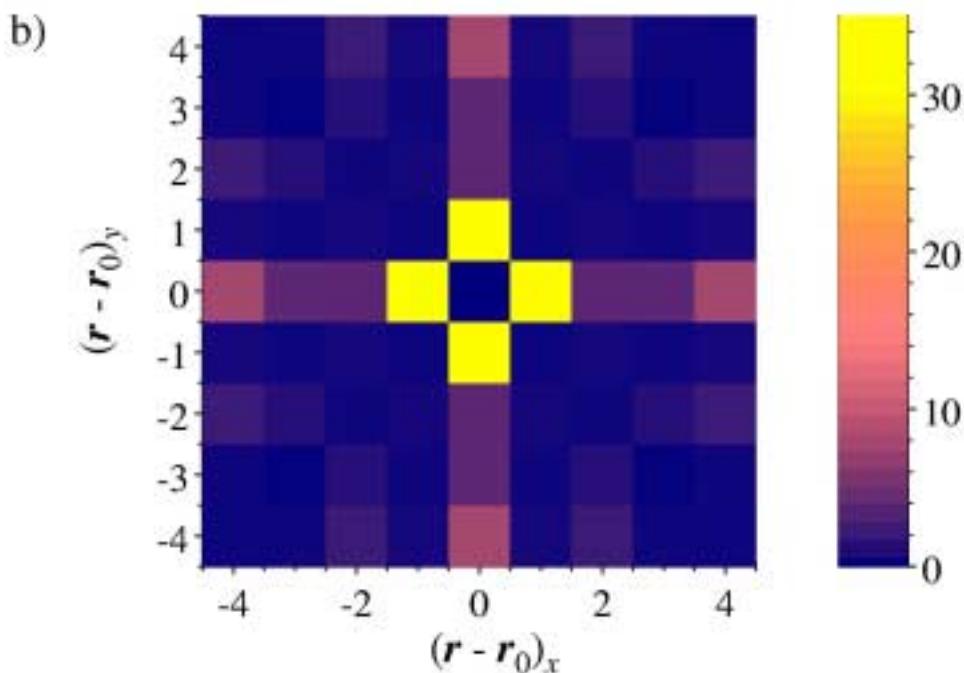
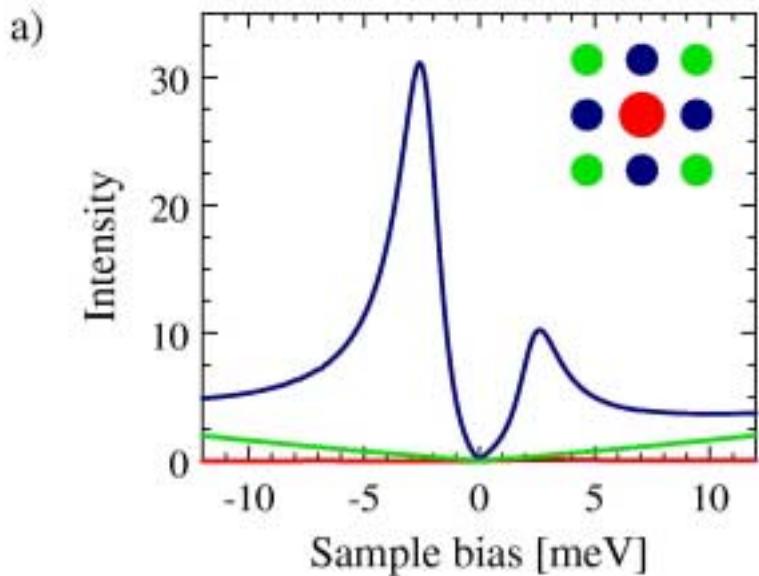
S. H. Pan *et al* Nature **403**, 746 (2000)

Theory: $S=1/2$ local moment coupled to Bogoliubov quasiparticles of a d -wave superconductor



A. Polkovnikov, S. Sachdev, and M. Vojta,
cond-mat/0007431, Phys. Rev. Lett. (in press).

Theory: Impurity scattering of Bogoliubov quasiparticles



A.V. Balatsky, M. I. Salkola, and A. Rosengren,
Phys. Rev. B **51**, 15547 (1995)
M. I. Salkola, A.V. Balatsky, and D. J. Scalapino,
Phys. Rev. Lett. **77**, 1841 (1996).
A. Polkovnikov, S. Sachdev, and M. Vojta, cond-mat/0007431
Phys. Rev. Lett. (in press)



Conclusions

1. Strong experimental evidence for $S=1/2$ moment near Zn and Li impurities in the underdoped high temperature superconductor.
2. Quantitative computations of STM tunneling and neutron scattering resonance linewidths compare well with experiments
3. Supports a reference paramagnetic Mott insulator with confinement – such a state requires $S=1$ spin resonance, broken translational symmetry (stripe order), and moments near non-magnetic impurities.
4. Charge stripes with antiferromagnetic order are site-centered and have anti-phase domain walls.

J. Zaanen and O. Gunnarsson, Phys. Rev. B **40**, 7391 (1989)

H. Schulz, J. de Physique **50**, 2833 (1989).

K. Machida, Physica **158C**, 192 (1989).

V.J. Emery and S.A. Kivelson, Physica C **235-240**, 189 (1994).

Evidence for bond-centered stripes in paramagnetic phase with superconductivity.

N. Read & S. Sachdev, Phys. Rev. Lett. **62**, 1694 (1989)
S. Sachdev & N. Read, Int. J. Mod. Phys. B **5**, 219 (1991).

