# Quantum entanglement and the phases of matter

University of Toronto March 22, 2012

PHYSICS

VE RI

TAS

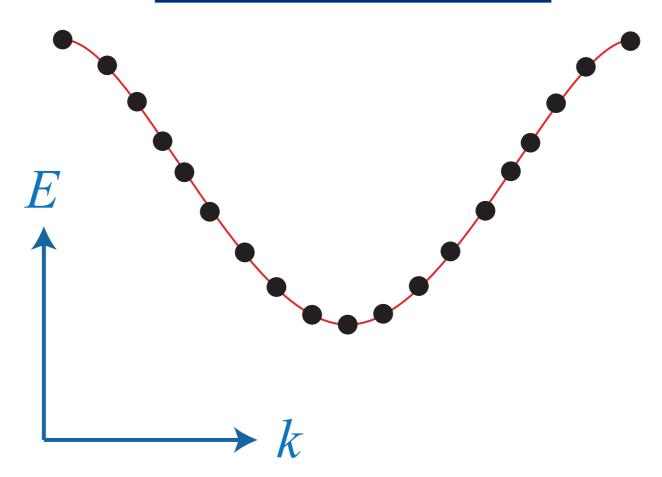
HARVARD

sachdev.physics.harvard.edu

many-electron quantum states are adiabatically connected to independent electron states

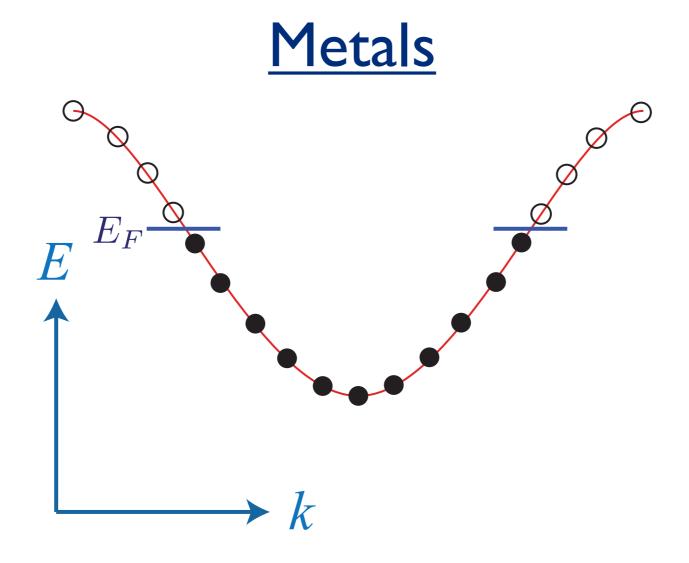
many-electron quantum states are adiabatically connected to independent electron states

#### Band insulators



An even number of electrons per unit cell

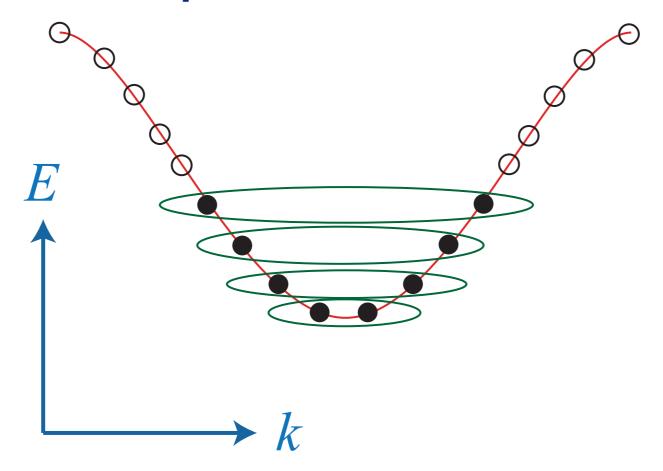
many-electron quantum states are adiabatically connected to independent electron states



An odd number of electrons per unit cell

many-electron quantum states are adiabatically connected to independent electron states

#### <u>Superconductors</u>



Sommerfeld-Bloch theory of metals, insulators, and superconductors: many-electron quantum states are adiabatically connected to independent electron states

#### Modern phases of quantum matter

Not adiabatically connected to independent electron states:

many-particle quantum entanglement

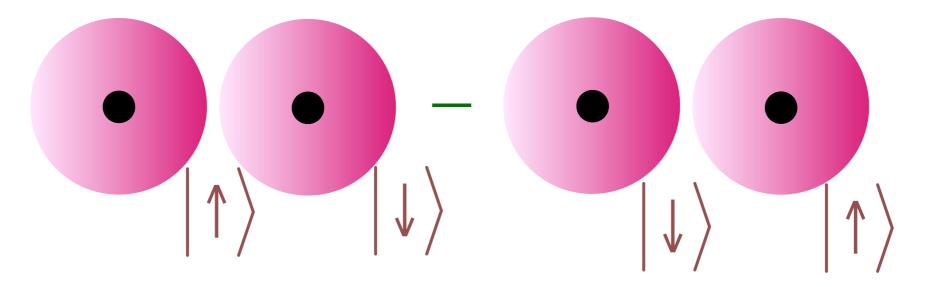
Hydrogen atom:

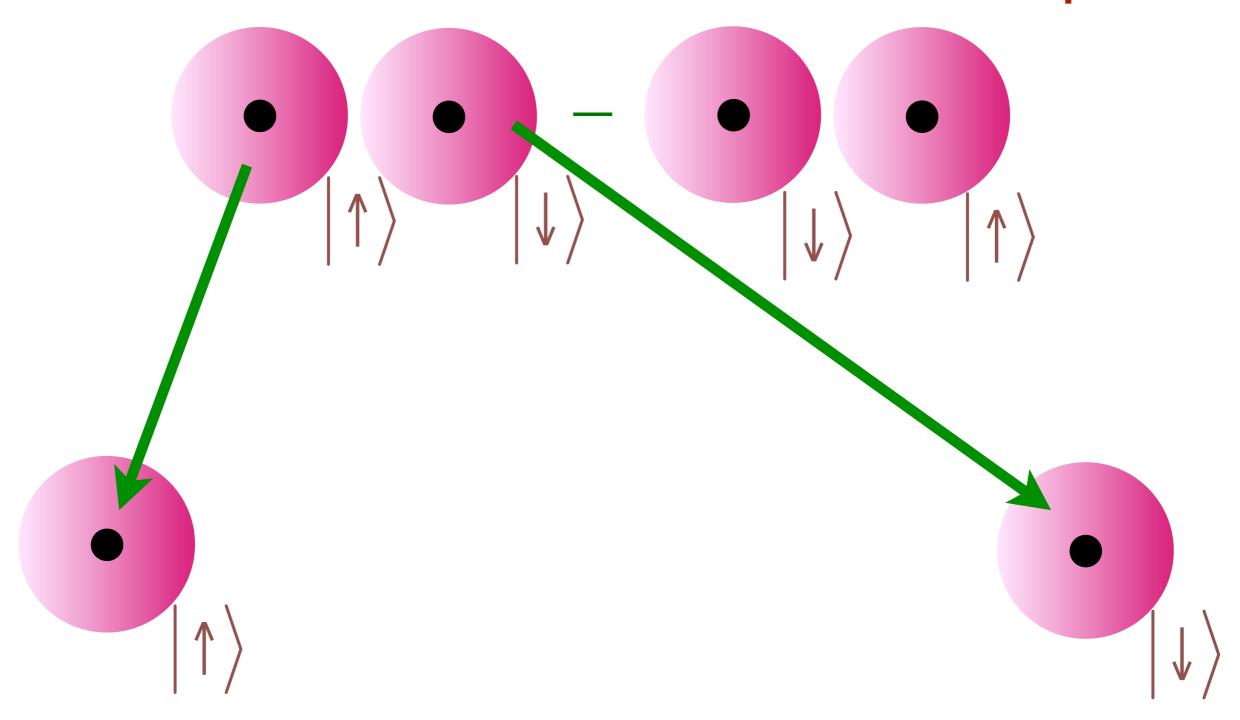
Hydrogen atom:

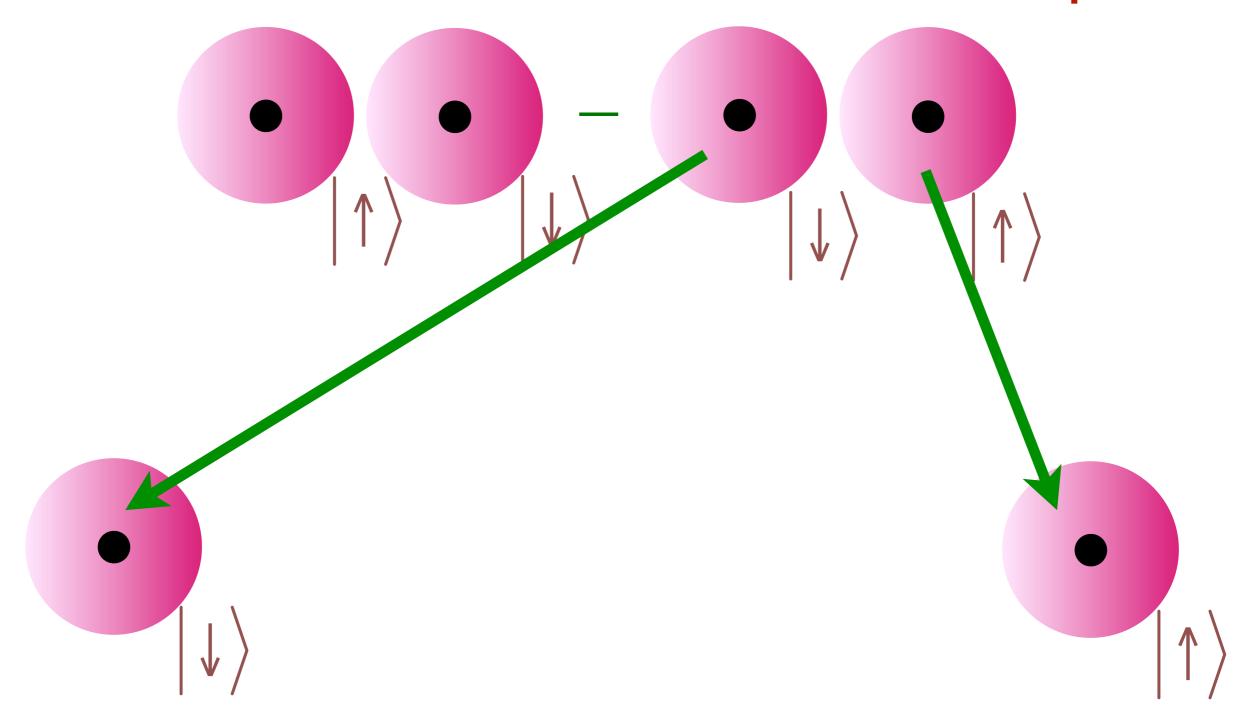


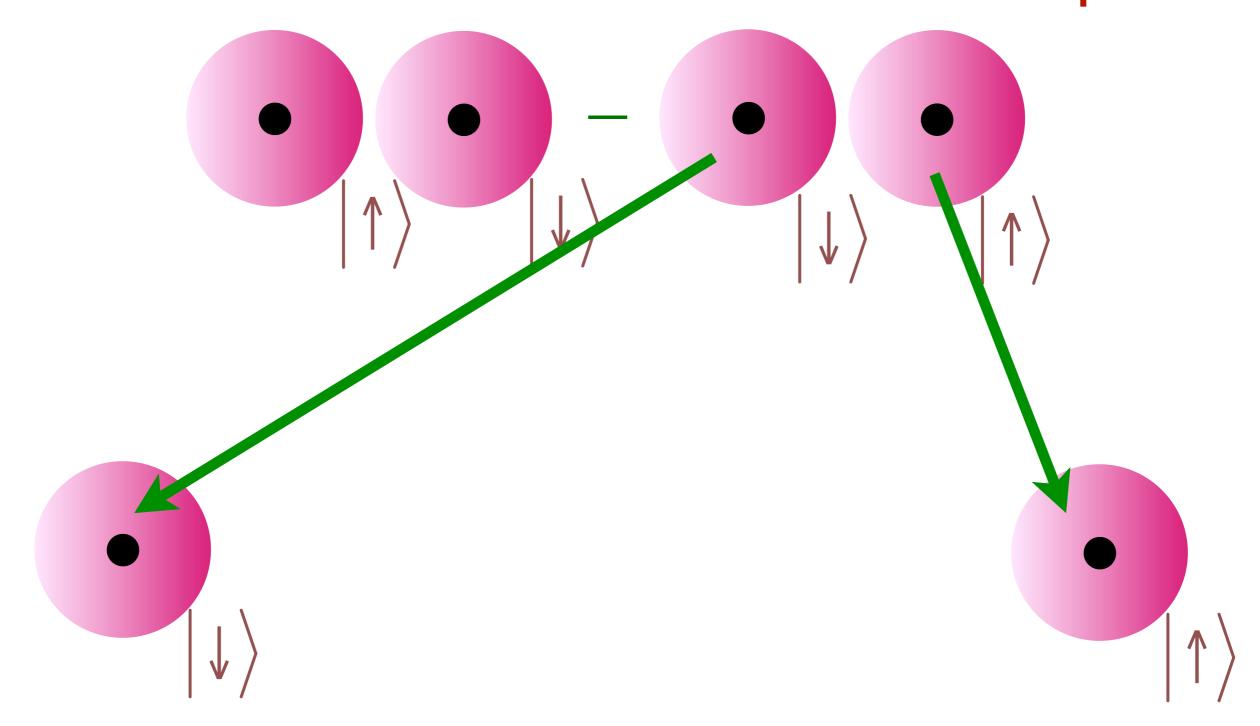
Hydrogen molecule:

Superposition of two electron states leads to non-local correlations between spins









Einstein-Podolsky-Rosen "paradox": Non-local correlations between observations arbitrarily far apart

Quantum critical points of electrons in crystals

String theory and black holes

Quantum critical points of electrons in crystals

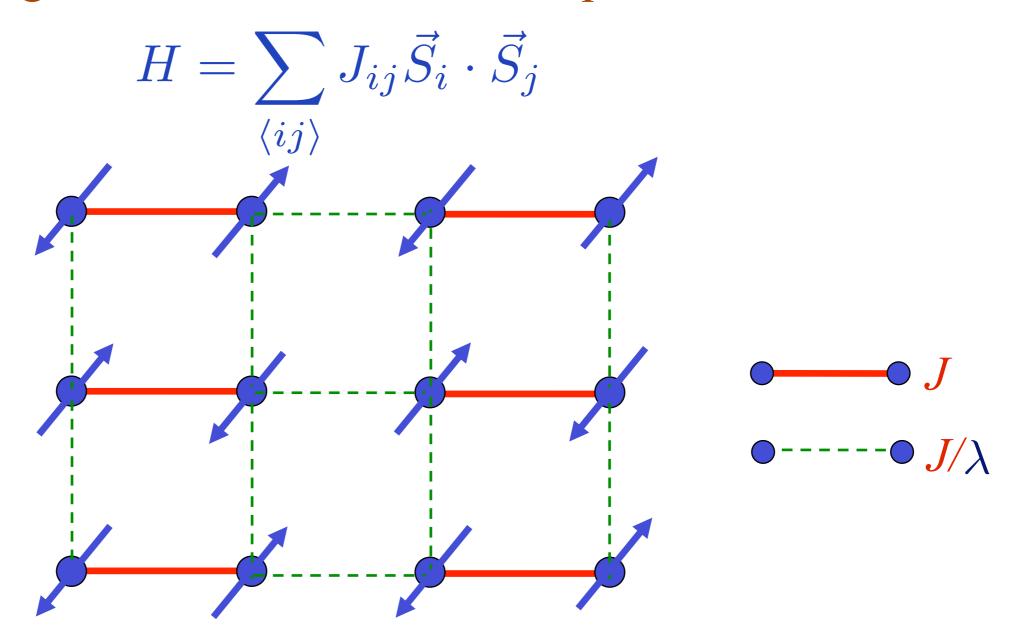
String theory and black holes

$$H = \sum_{\langle ij \rangle} J_{ij} \vec{S}_i \cdot \vec{S}_j$$
S=1/2 spins

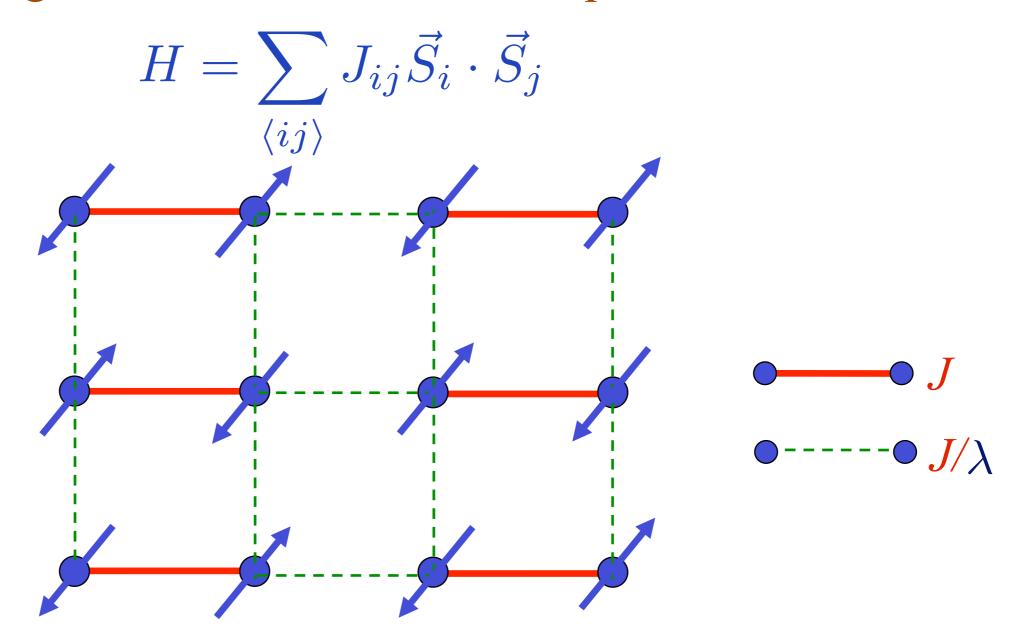
Examine ground state as a function of  $\lambda$ 

At large  $\lambda$  ground state is a "quantum paramagnet" with spins locked in valence bond singlets

Nearest-neighor spins are "entangled" with each other. Can be separated into an Einstein-Podolsky-Rosen (EPR) pair.

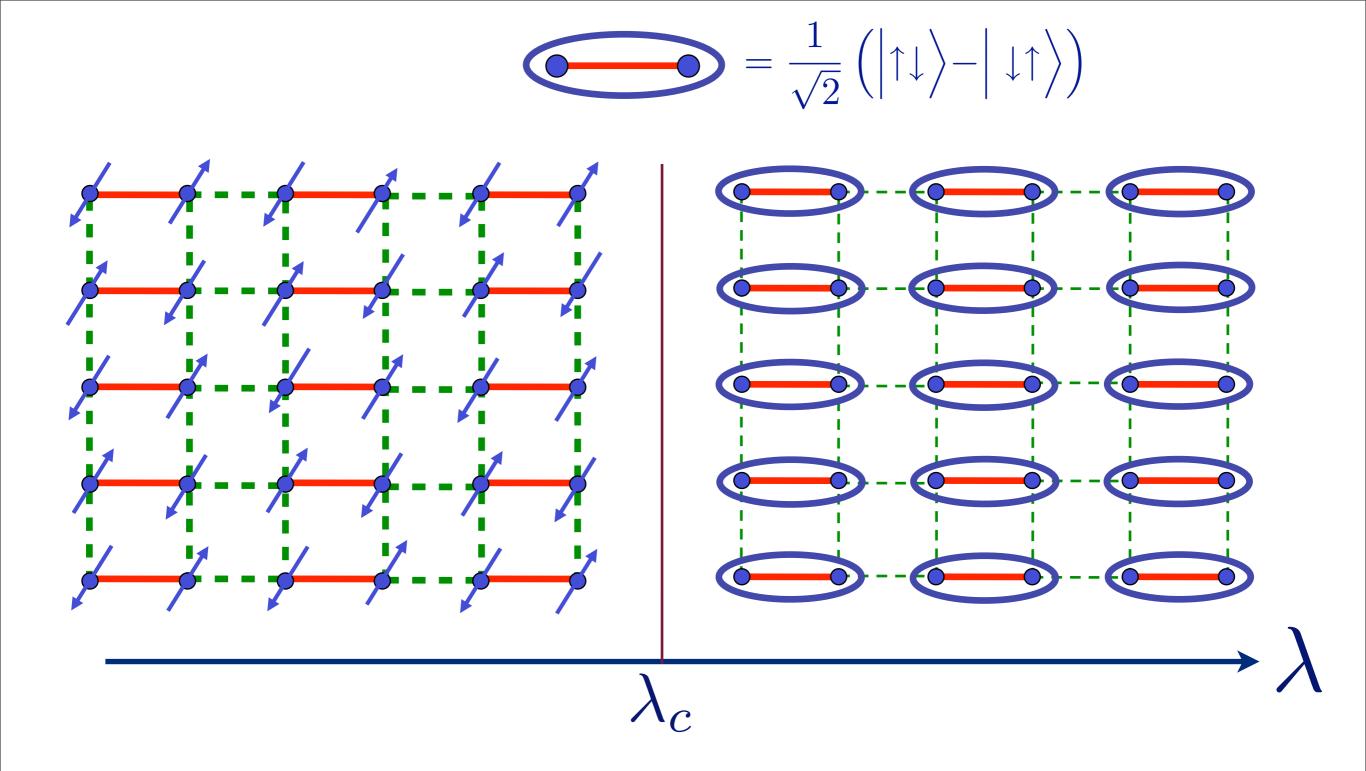


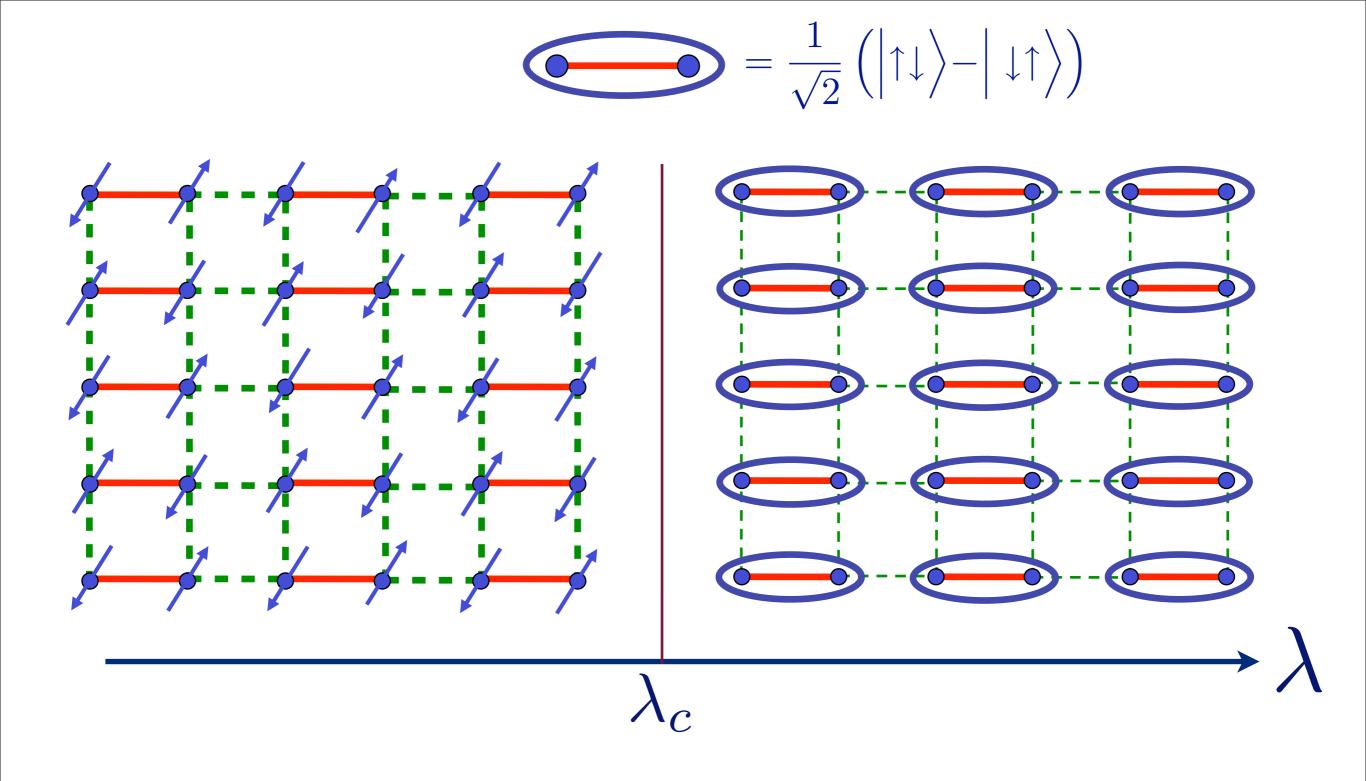
For  $\lambda \approx 1$ , the ground state has antiferromagnetic ("Néel") order, and the spins align in a checkerboard pattern



For  $\lambda \approx 1$ , the ground state has antiferromagnetic ("Néel") order, and the spins align in a checkerboard pattern

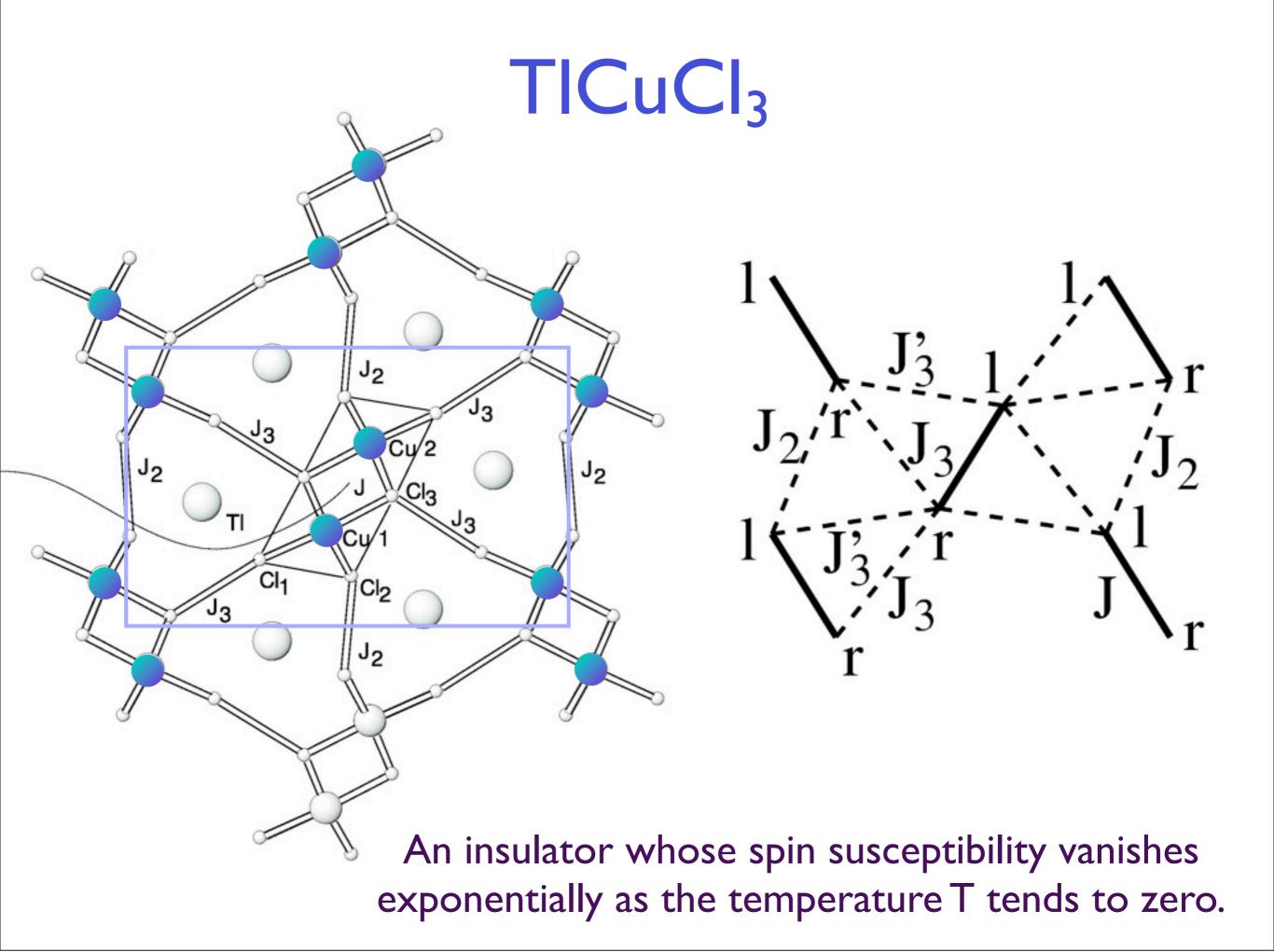
#### No EPR pairs

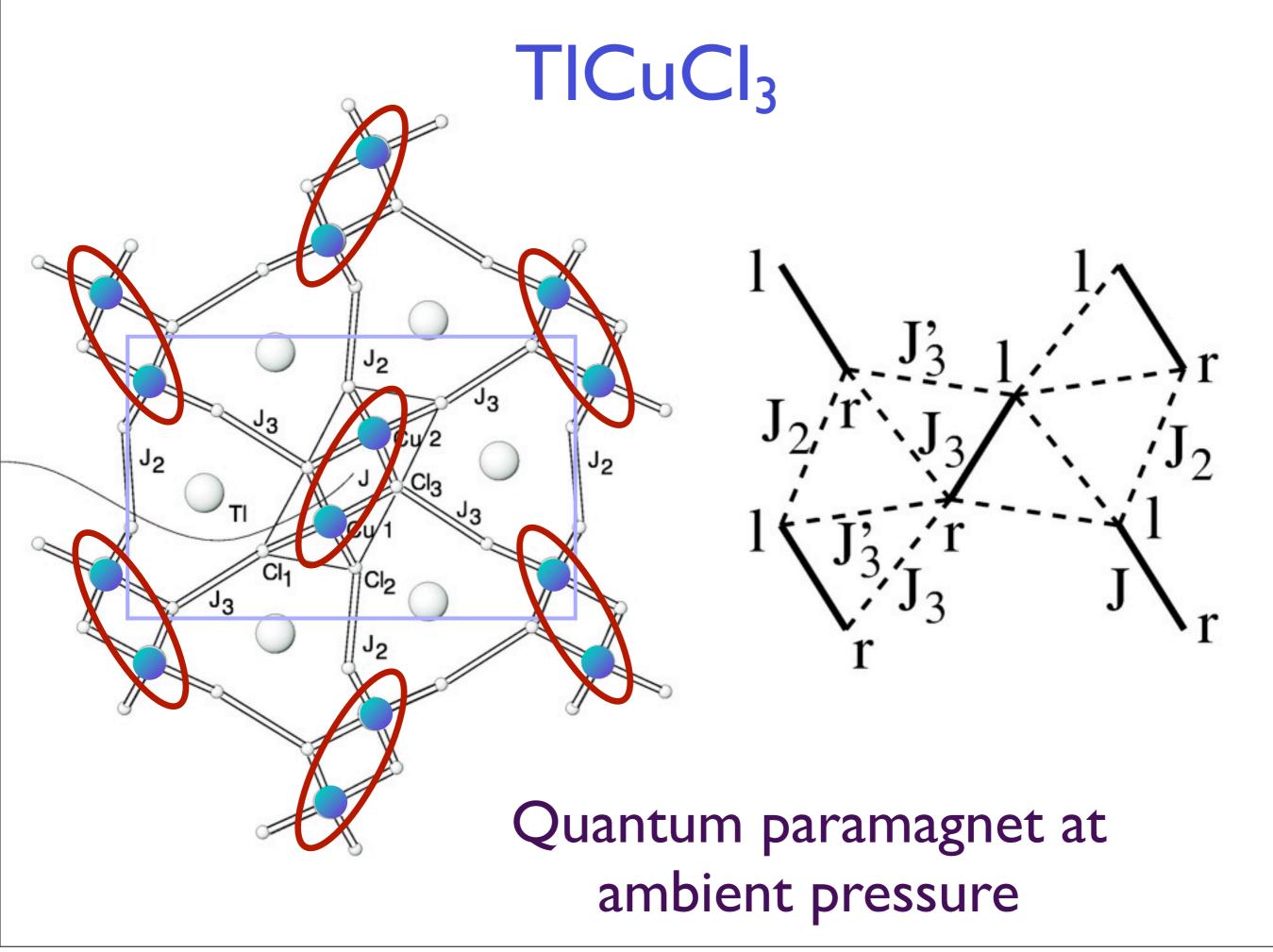


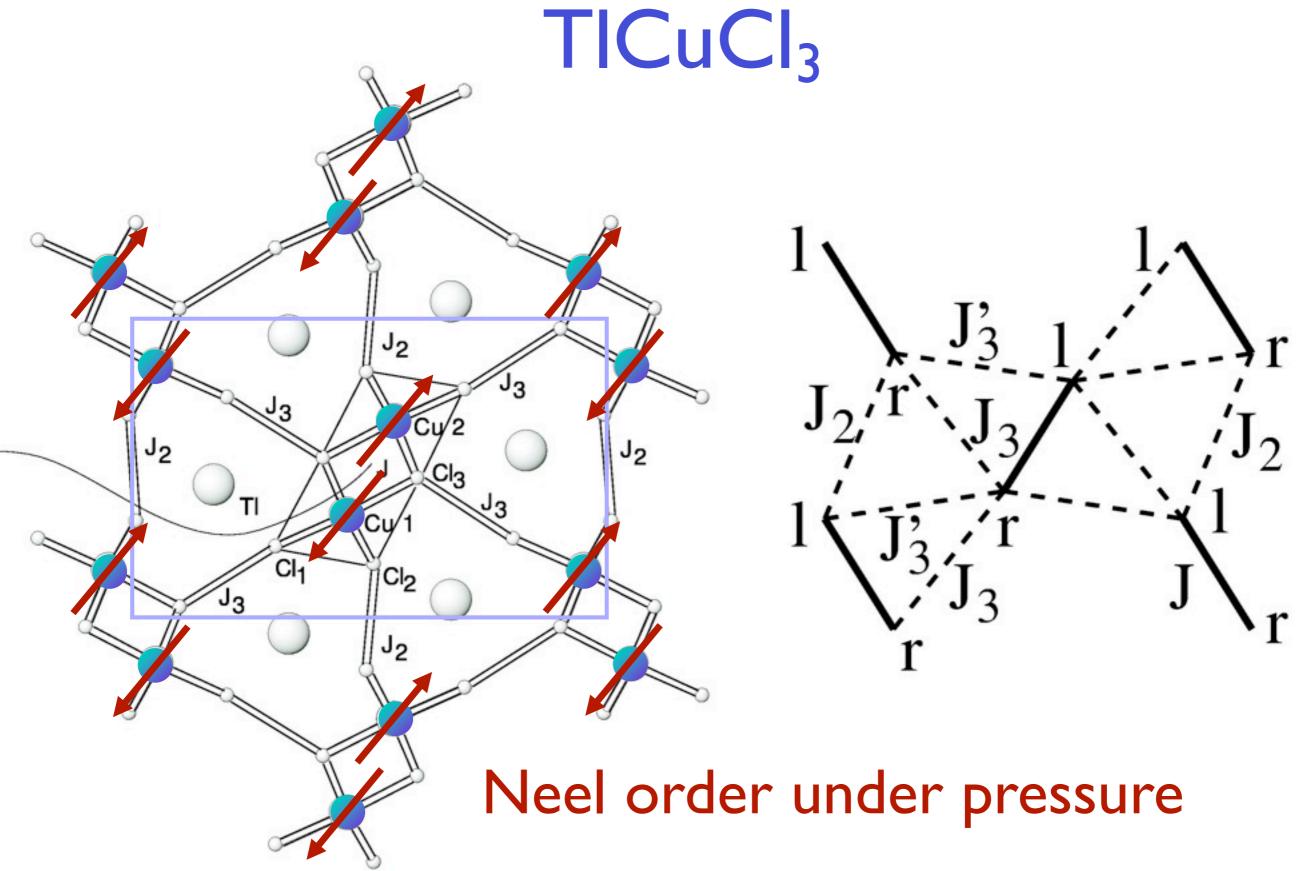




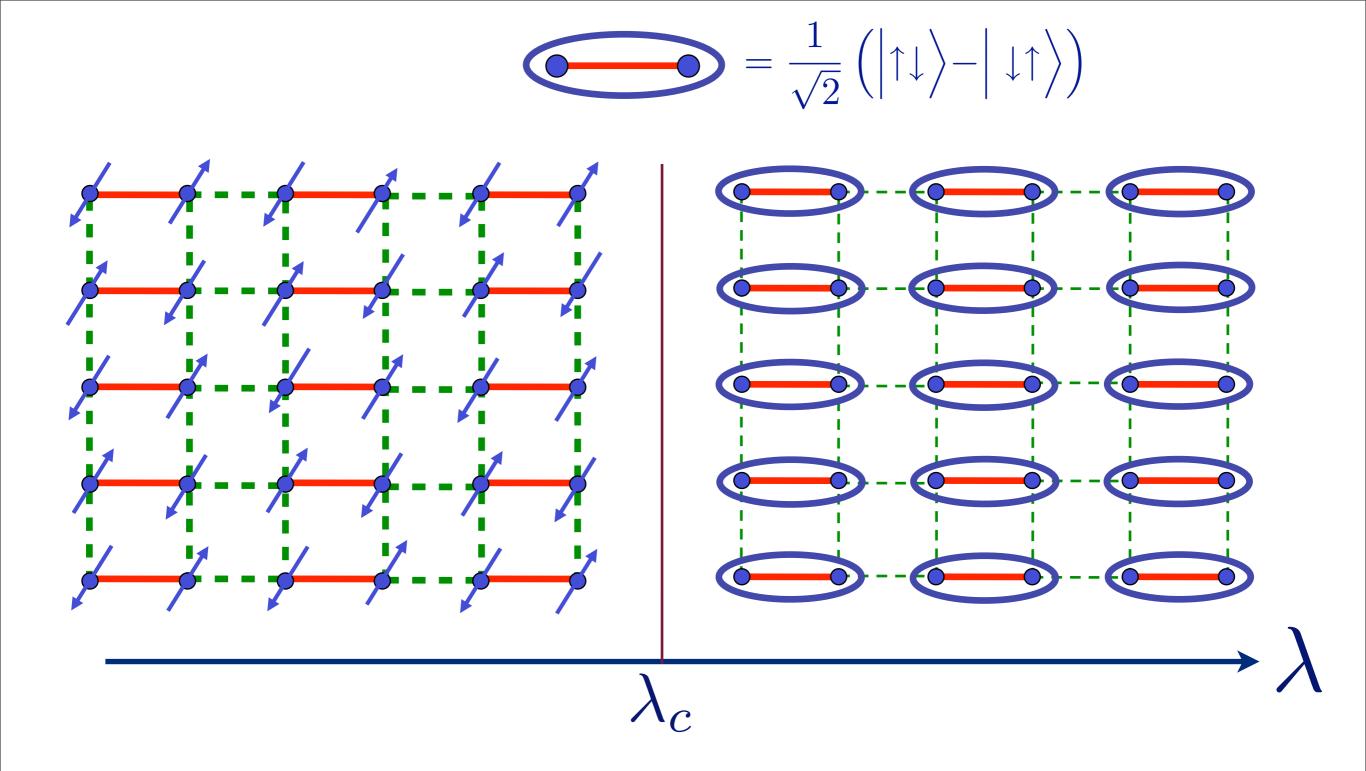
A. Oosawa, K. Kakurai, T. Osakabe, M. Nakamura, M. Takeda, and H. Tanaka, Journal of the Physical Society of Japan, 73, 1446 (2004).



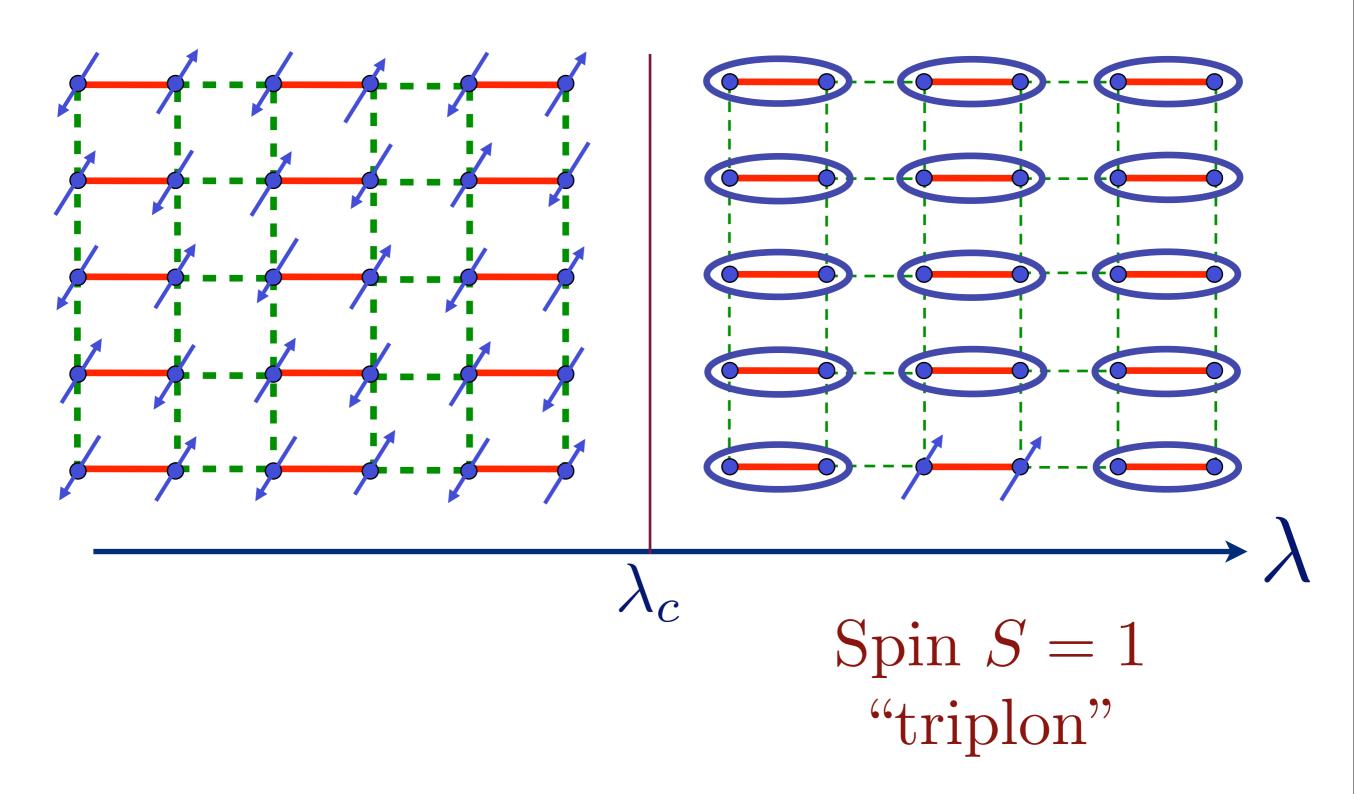




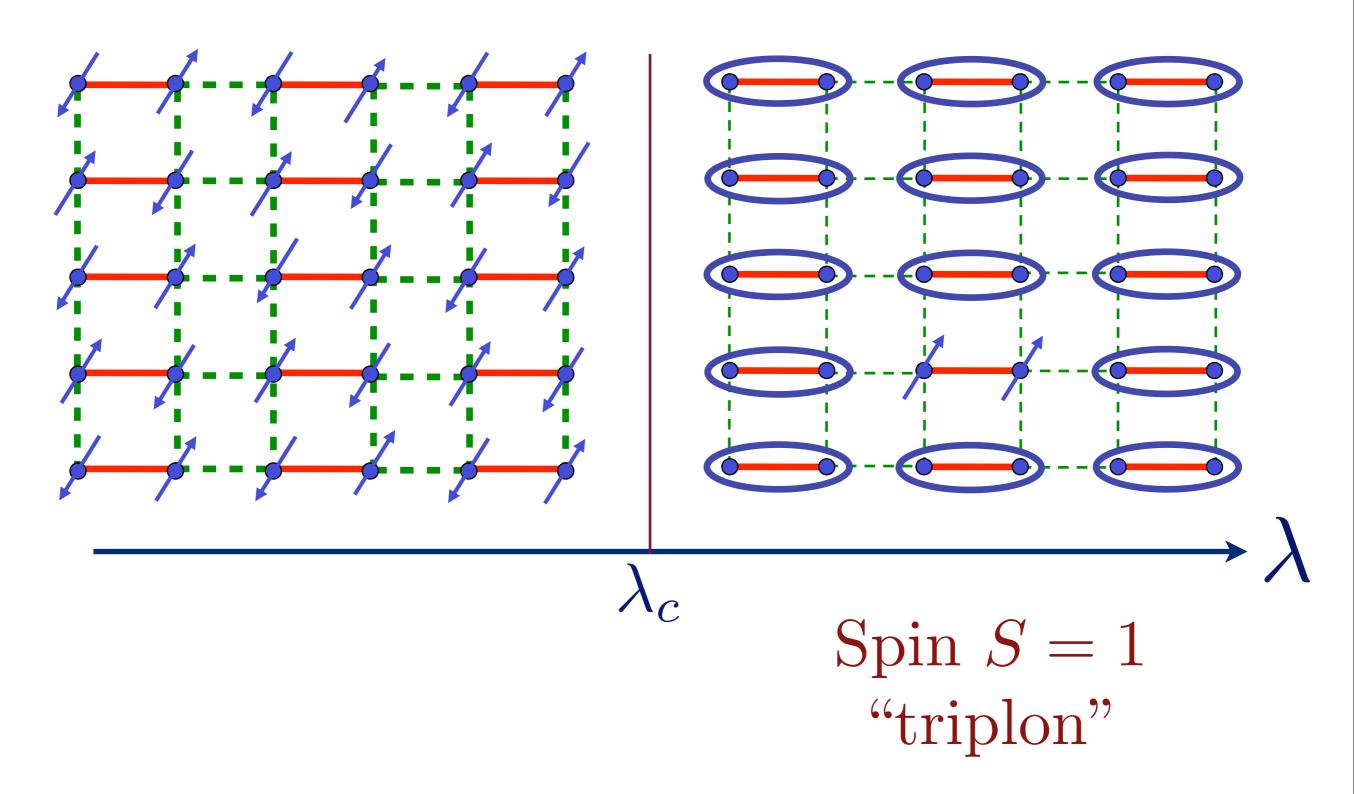
A. Oosawa, K. Kakurai, T. Osakabe, M. Nakamura, M. Takeda, and H. Tanaka, Journal of the Physical Society of Japan, 73, 1446 (2004).



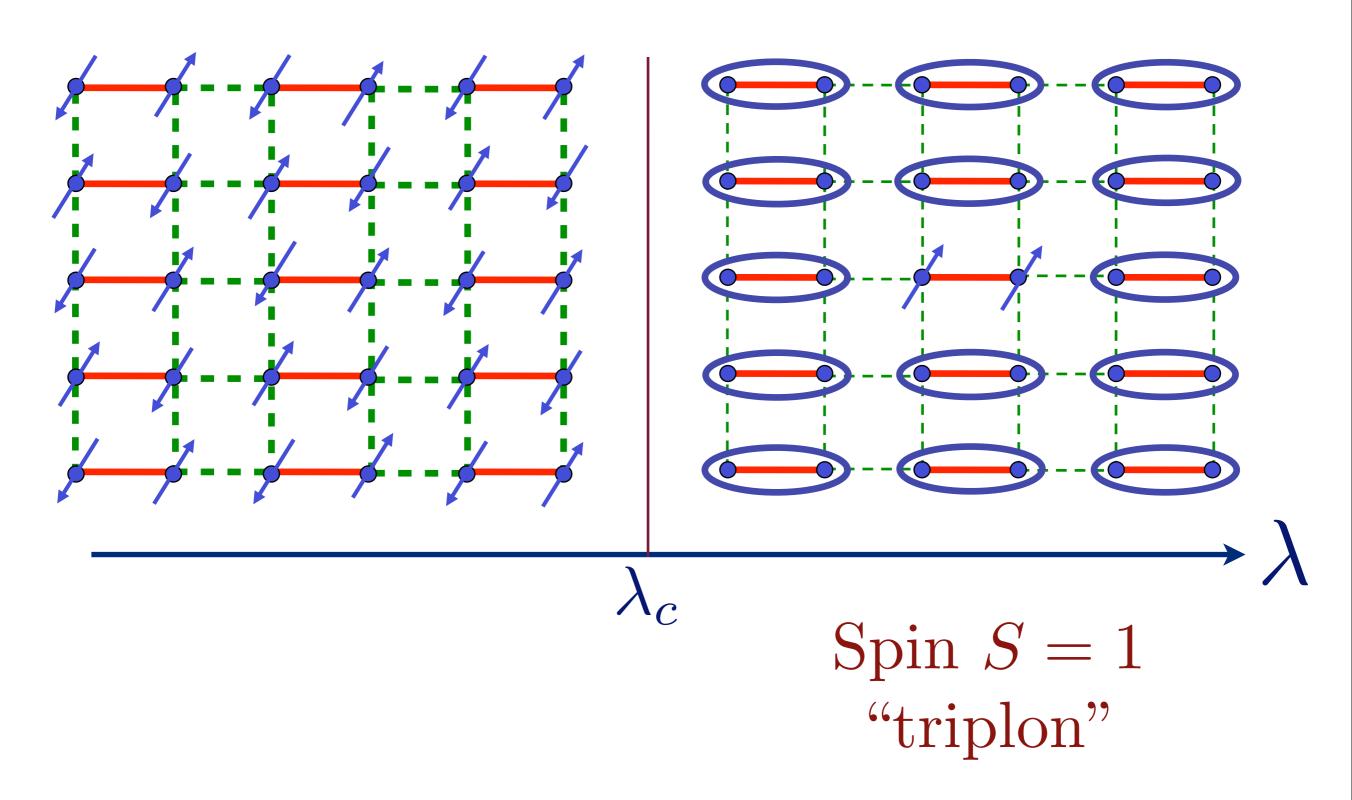
Excitation spectrum in the paramagnetic phase



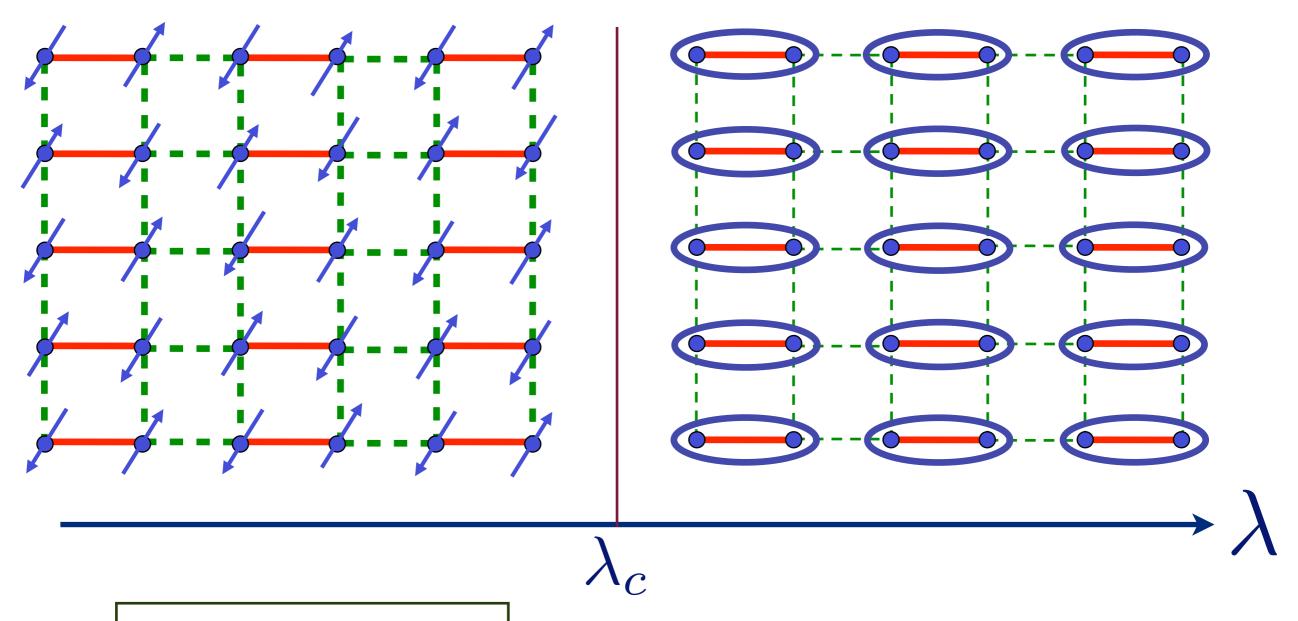
Excitation spectrum in the paramagnetic phase



Excitation spectrum in the paramagnetic phase

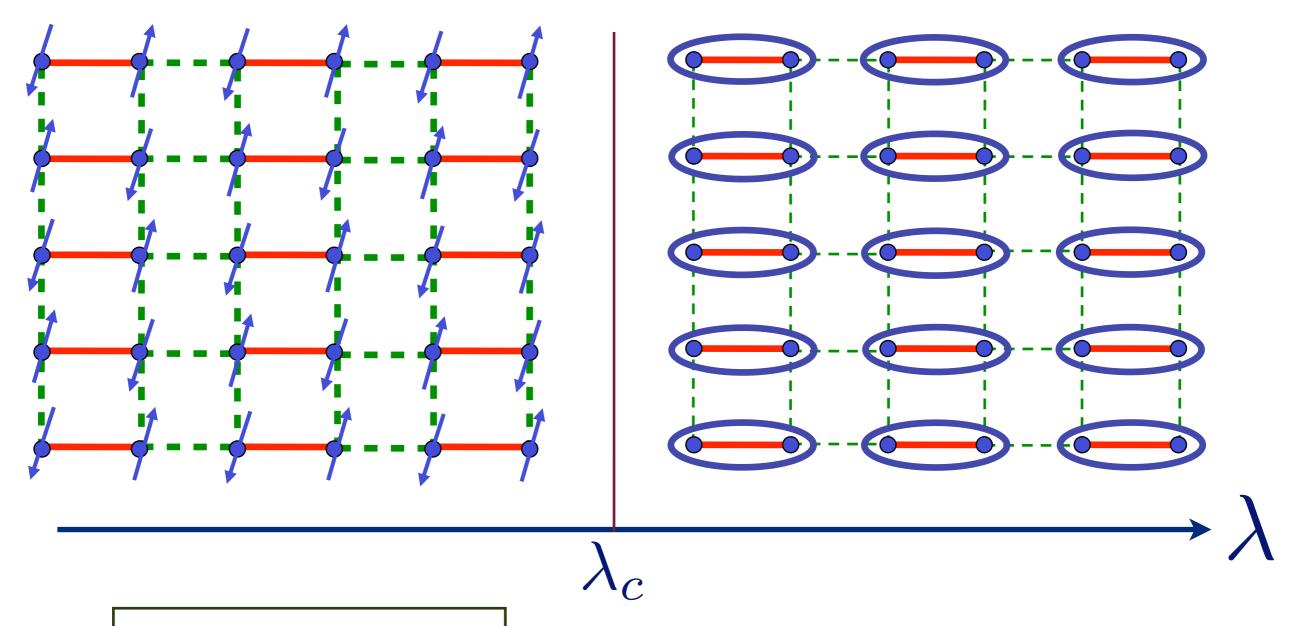


#### Excitation spectrum in the Néel phase



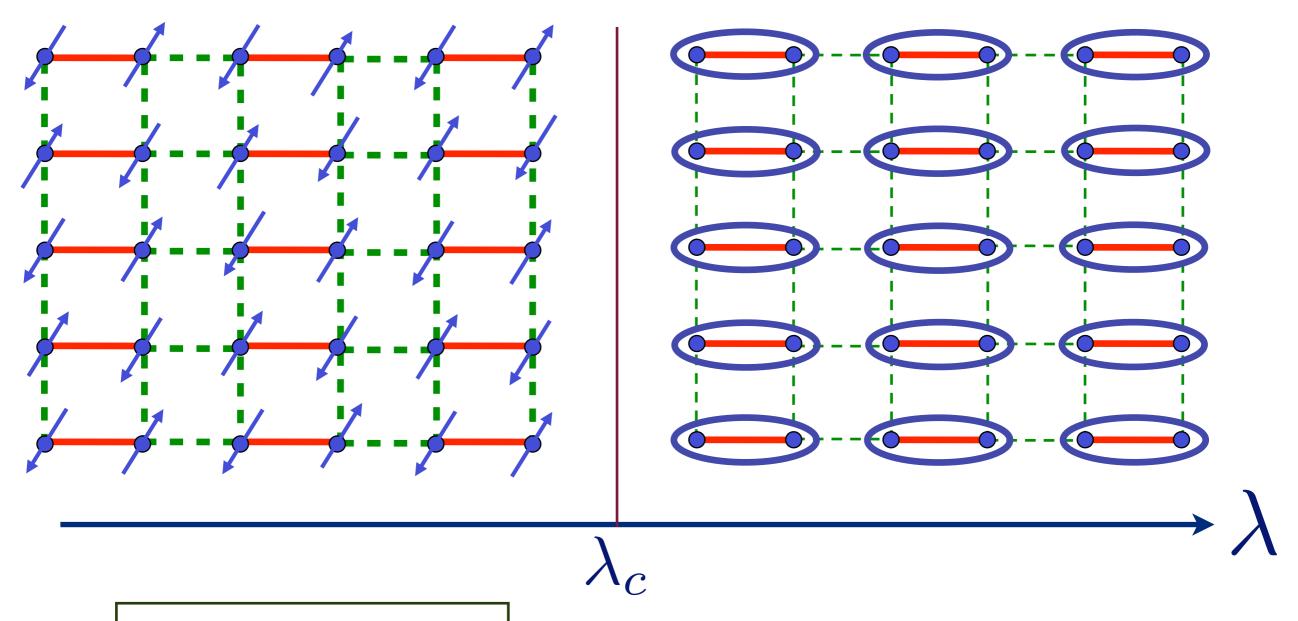
Spin waves

#### Excitation spectrum in the Néel phase



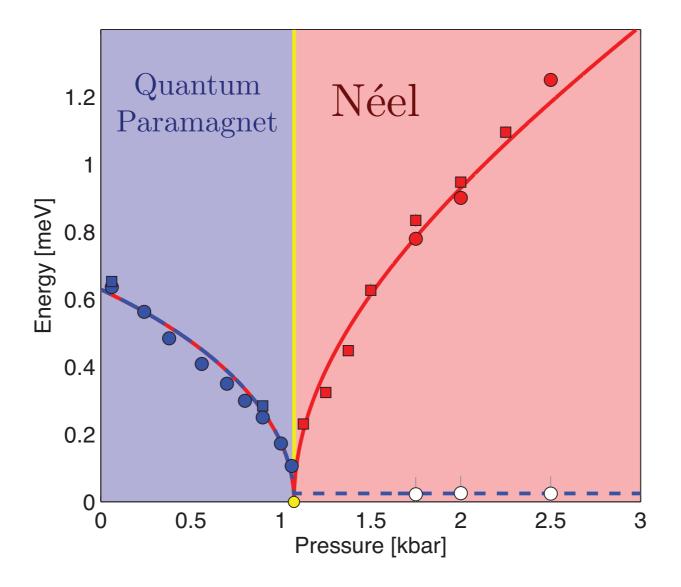
Spin waves

#### Excitation spectrum in the Néel phase



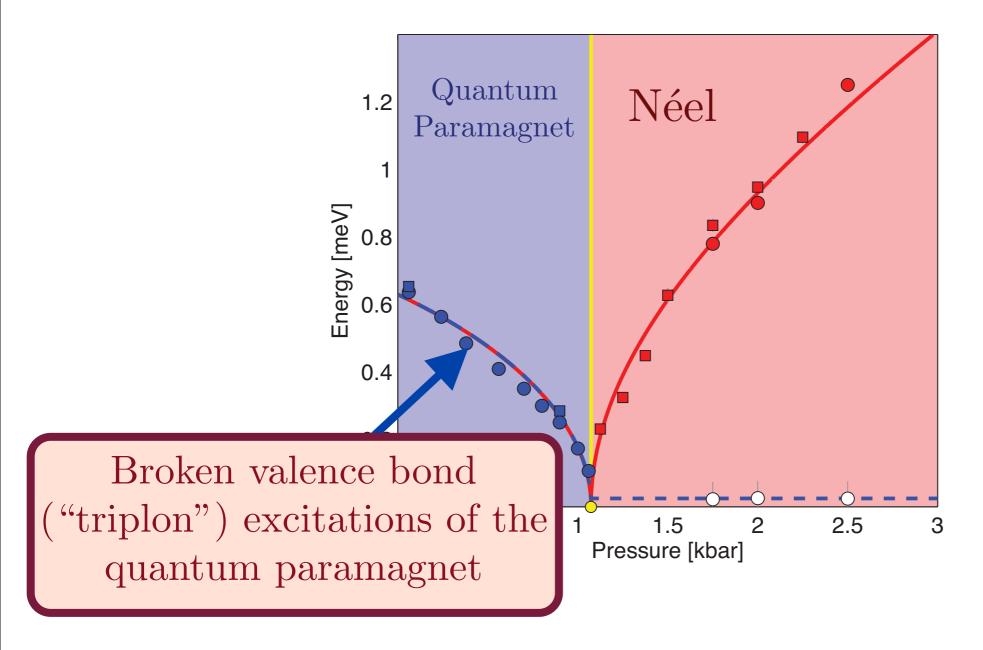
Spin waves

#### Excitations of TICuCl<sub>3</sub> with varying pressure



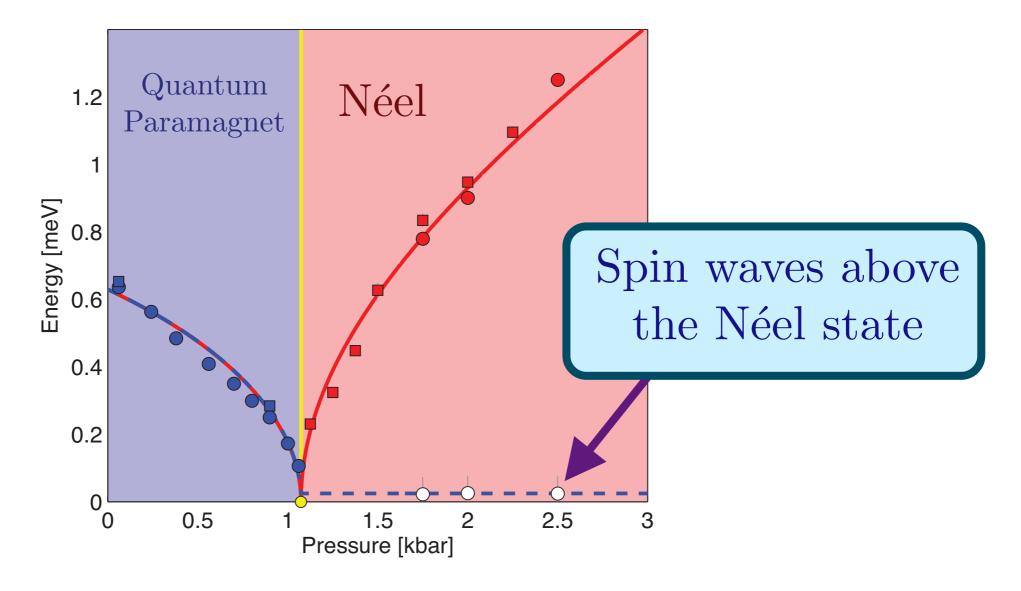
Christian Ruegg, Bruce Normand, Masashige Matsumoto, Albert Furrer, Desmond McMorrow, Karl Kramer, Hans-Ulrich Gudel, Severian Gvasaliya, Hannu Mutka, and Martin Boehm, *Phys. Rev. Lett.* **100**, 205701 (2008)

### Excitations of TICuCl<sub>3</sub> with varying pressure



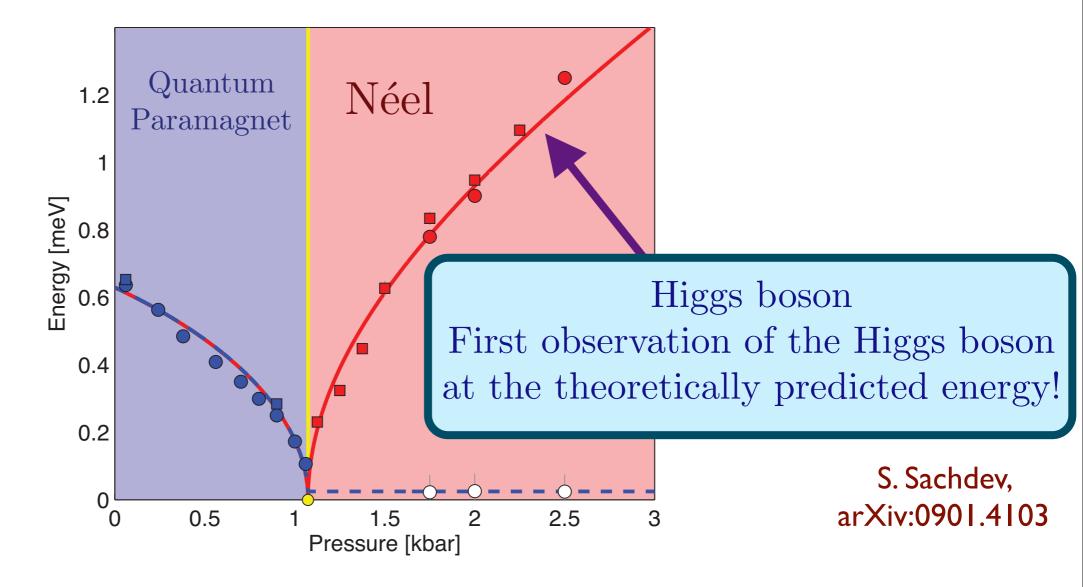
Christian Ruegg, Bruce Normand, Masashige Matsumoto, Albert Furrer, Desmond McMorrow, Karl Kramer, Hans-Ulrich Gudel, Severian Gvasaliya, Hannu Mutka, and Martin Boehm, *Phys. Rev. Lett.* **100**, 205701 (2008)

## Excitations of TICuCl<sub>3</sub> with varying pressure

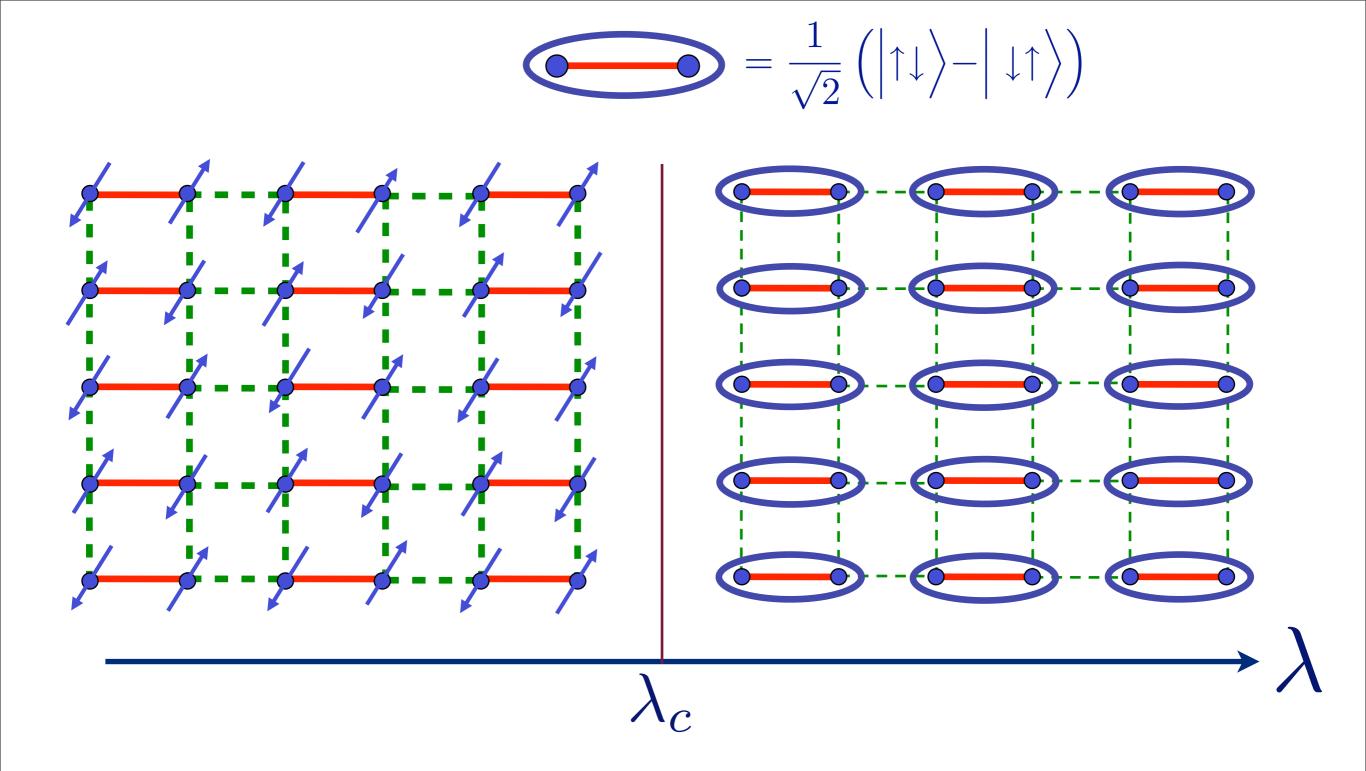


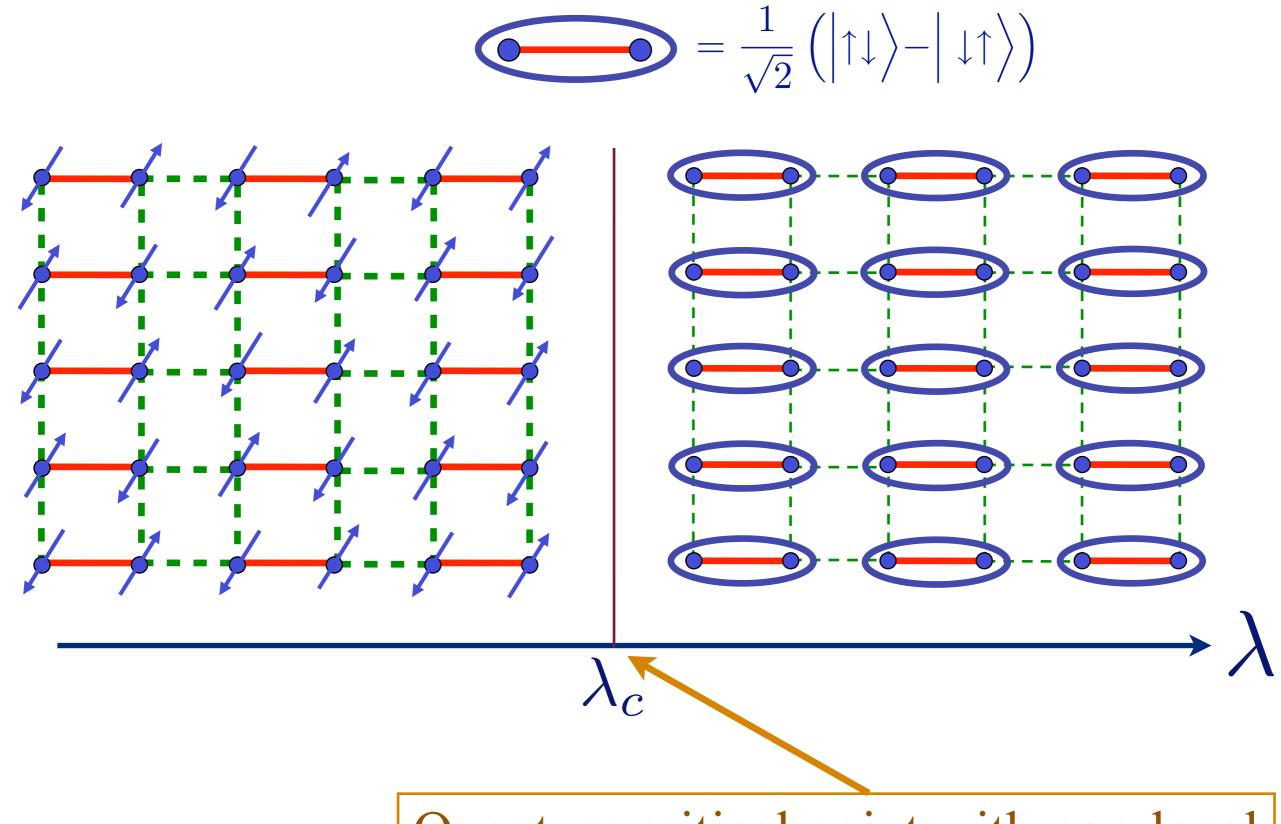
Christian Ruegg, Bruce Normand, Masashige Matsumoto, Albert Furrer, Desmond McMorrow, Karl Kramer, Hans-Ulrich Gudel, Severian Gvasaliya, Hannu Mutka, and Martin Boehm, *Phys. Rev. Lett.* **100**, 205701 (2008)

### Excitations of TICuCl<sub>3</sub> with varying pressure



Christian Ruegg, Bruce Normand, Masashige Matsumoto, Albert Furrer, Desmond McMorrow, Karl Kramer, Hans-Ulrich Gudel, Severian Gvasaliya, Hannu Mutka, and Martin Boehm, *Phys. Rev. Lett.* **100**, 205701 (2008)



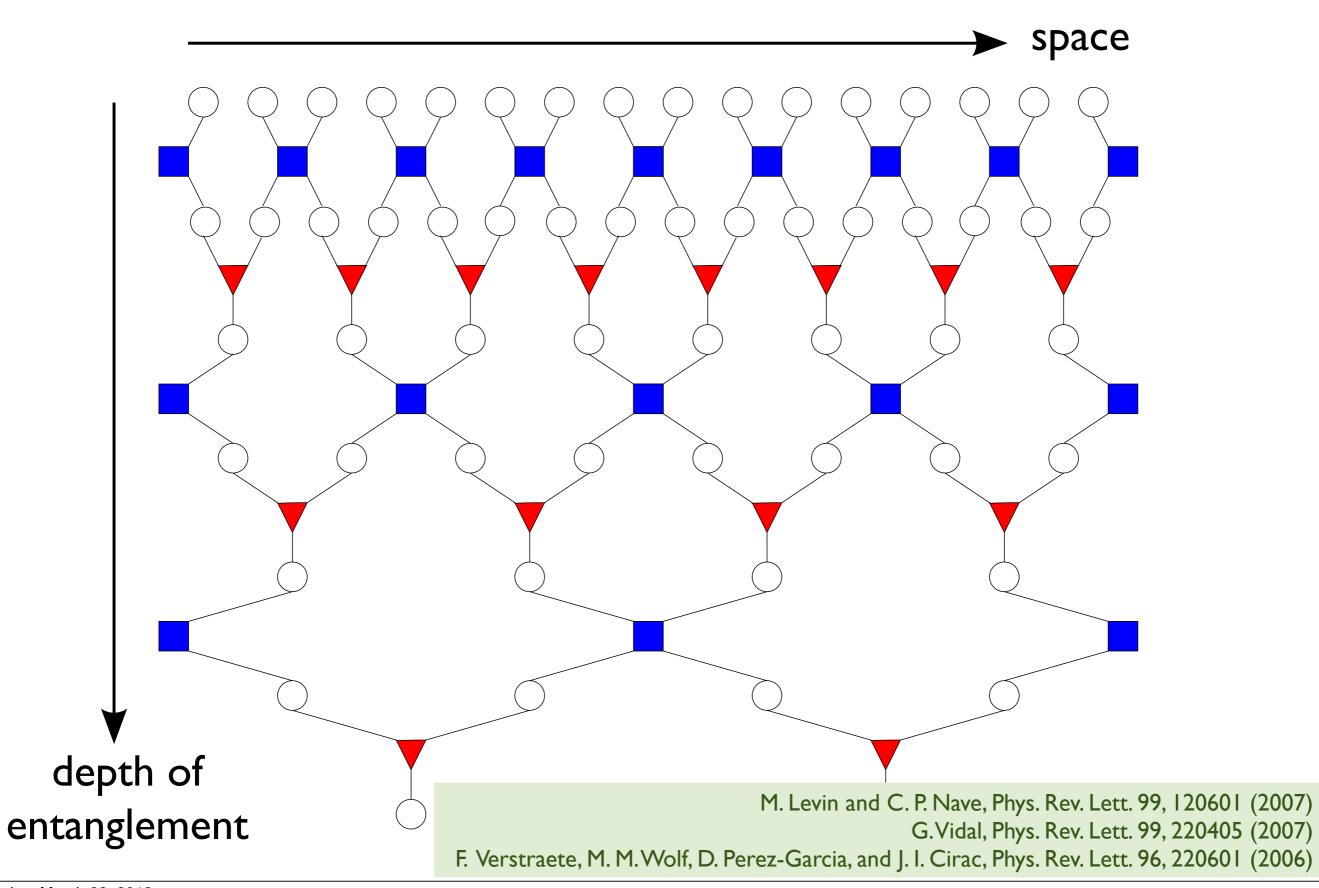


Quantum critical point with non-local entanglement in spin wavefunction

A. W. Sandvik and D. J. Scalapino, Phys. Rev. Lett. **72**, 2777 (1994).

## Tensor network representation of entanglement at quantum critical point

#### **D**-dimensional



• Long-range entanglement

- Long-range entanglement
- The low energy excitations are described by a theory which has the same structure as Einstein's theory of special relativity, but with the spin-wave velocity playing the role of the velocity of light.

- Long-range entanglement
- The low energy excitations are described by a theory which has the same structure as Einstein's theory of special relativity, but with the spin-wave velocity playing the role of the velocity of light.
- The theory of the critical point has an even larger symmetry corresponding to conformal transformations of spacetime: we refer to such a theory as a **CFT3**

- Long-range entanglement
- The low energy excitations are described by a theory which has the same structure as Einstein's theory of special relativity, but with the spin-wave velocity playing the role of the velocity of light.
- The theory of the critical point has an even larger symmetry corresponding to conformal transformations of spacetime: we refer to such a theory as a **CFT3**

Quantum superposition and entanglement

Quantum critical points of electrons in crystals

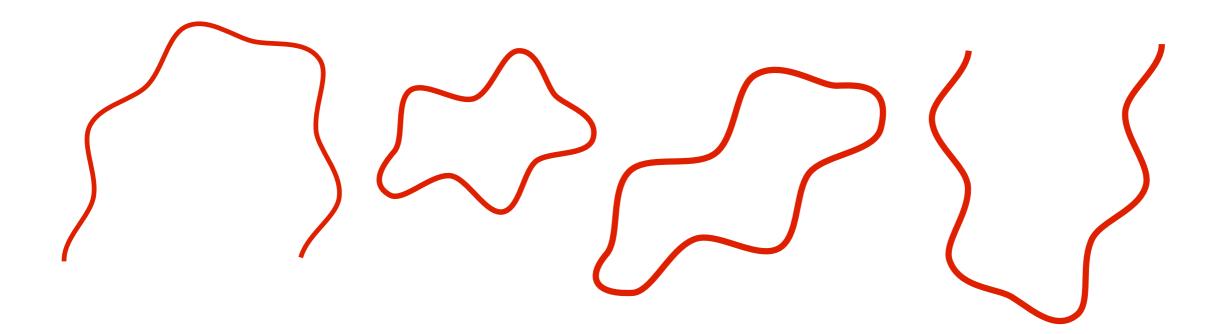
Quantum superposition and entanglement

Quantum critical points of electrons in crystals

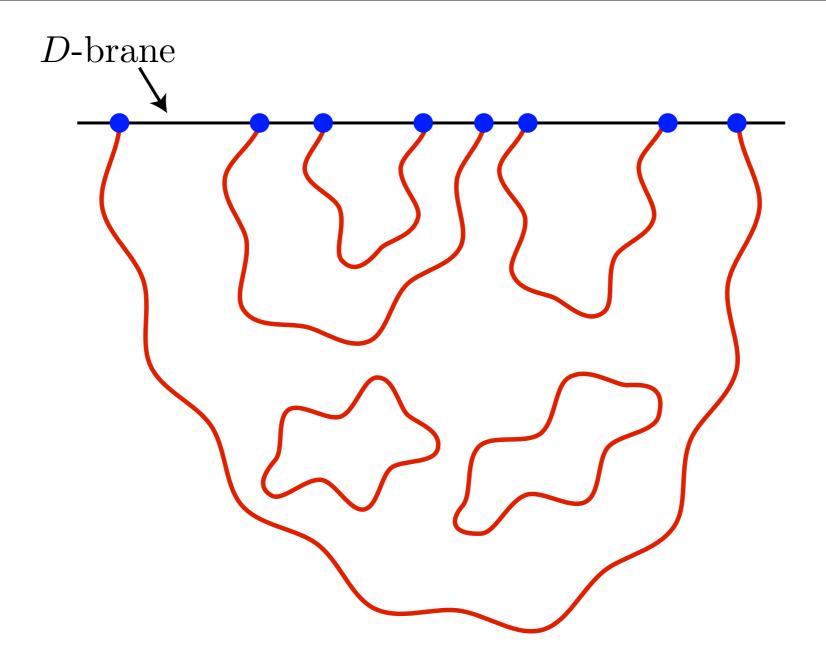
Quantum superposition and entanglement

Quantum critical points of electrons in crystals

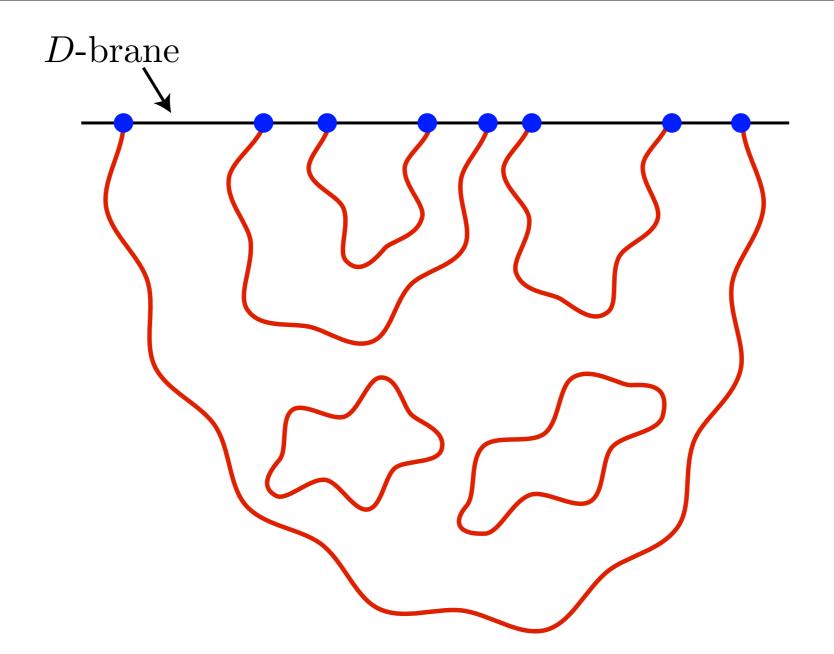
#### String theory



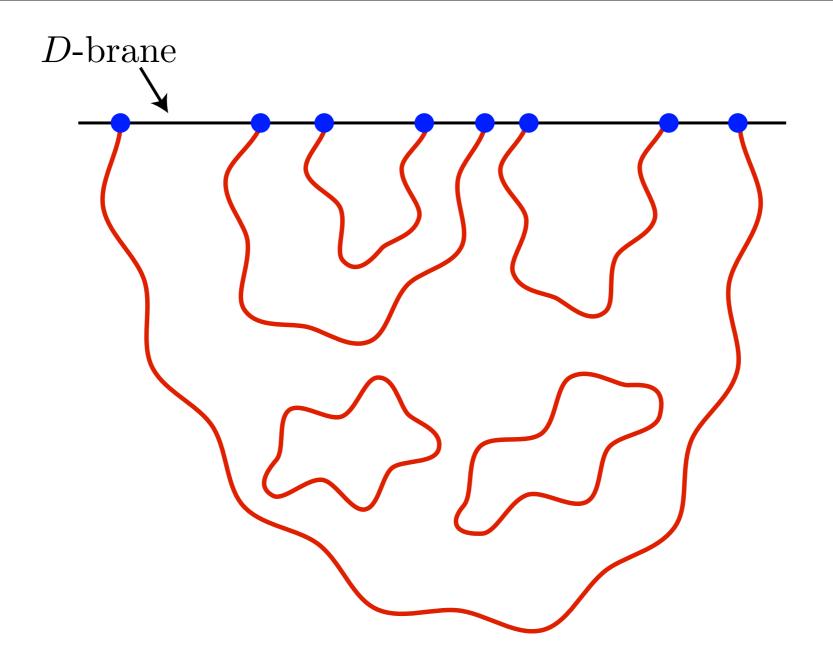
- Allows unification of the standard model of particle physics with gravity.
- Low-lying string modes correspond to gauge fields, gravitons, quarks . . .



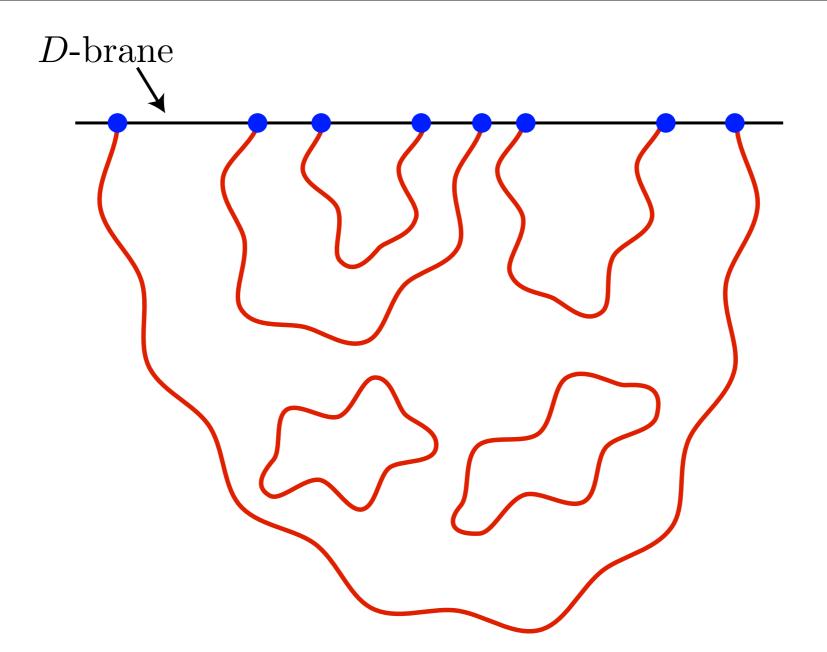
ullet A D-brane is a d-dimensional surface on which strings can end.



- A *D*-brane is a *d*-dimensional surface on which strings can end.
- The low-energy theory on a *D*-brane has no gravity, similar to theories of entangled electrons of interest to us.



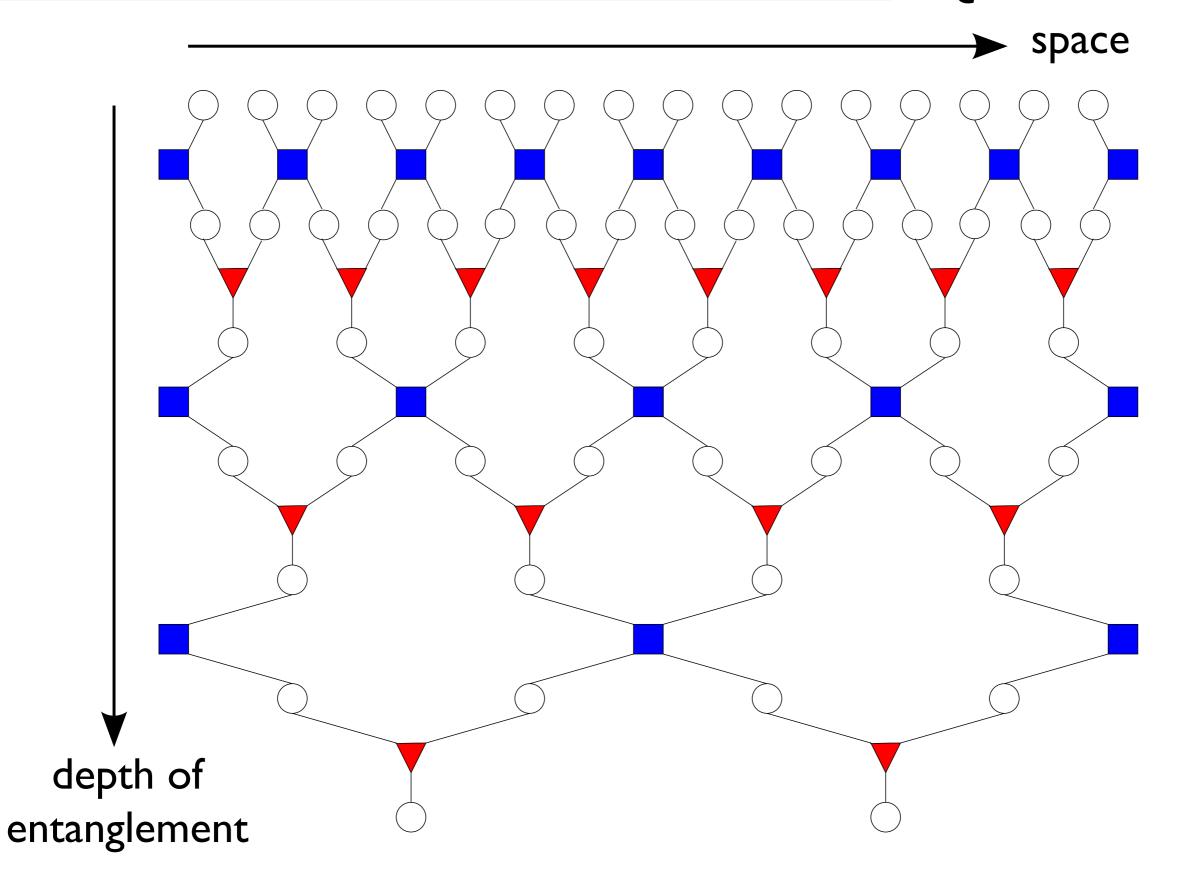
- A D-brane is a d-dimensional surface on which strings can end.
- The low-energy theory on a *D*-brane has no gravity, similar to theories of entangled electrons of interest to us.
- In d = 2, we obtain strongly-interacting **CFT3**s. These are "dual" to string theory on anti-de Sitter space: **AdS4**.



- A D-brane is a d-dimensional surface on which strings can end.
- The low-energy theory on a D-brane has no gravity, similar to theories of entangled electrons of interest to us.
- In d=2, we obtain strongly-interacting **CFT3s**. These are "dual" to string theory on anti-de Sitter space: **AdS4**.

# Tensor network representation of entanglement at quantum critical point

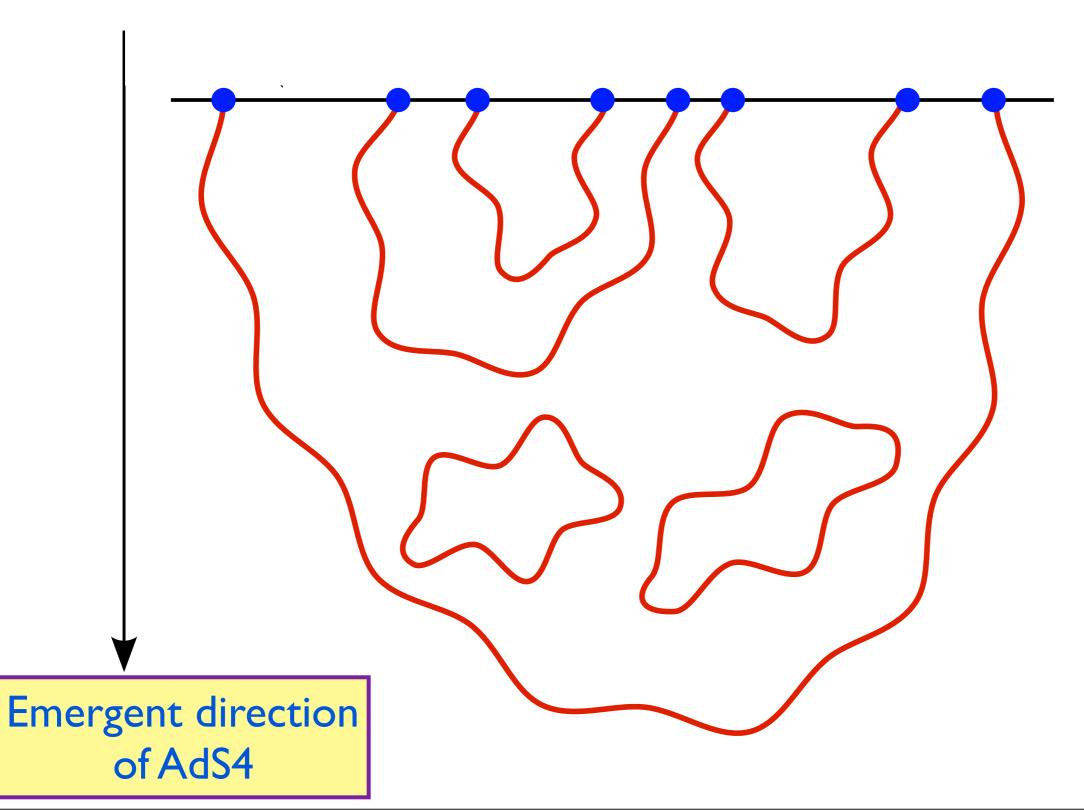
d-dimensional



String theory near a D-brane

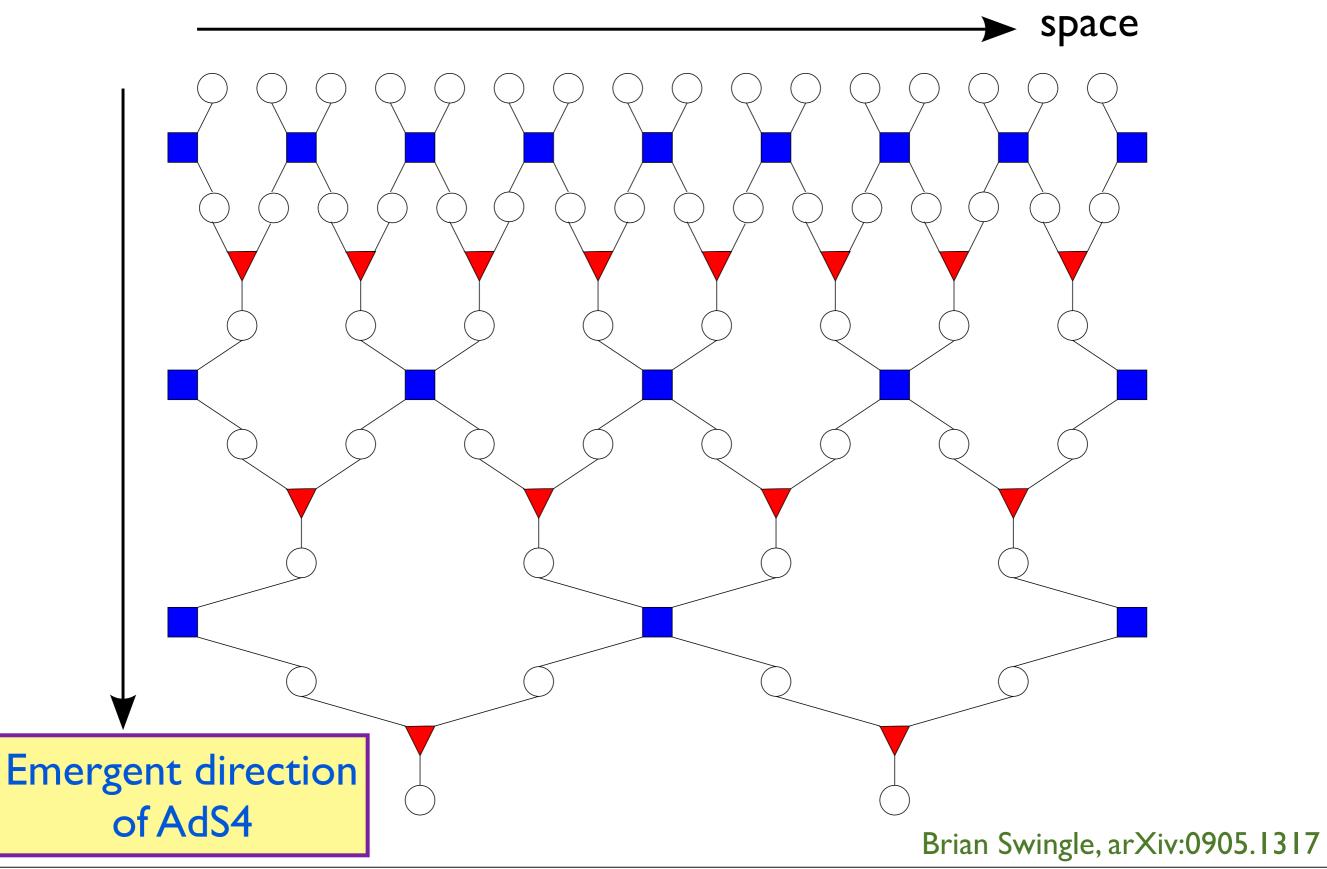
d-dimensional

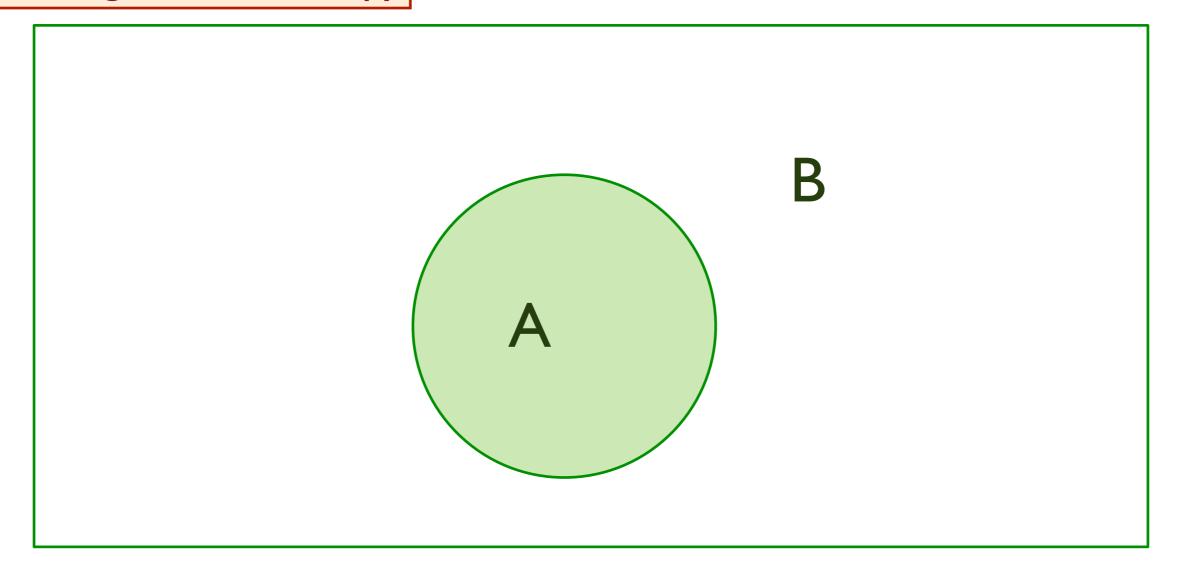
space



# Tensor network representation of entanglement at quantum critical point

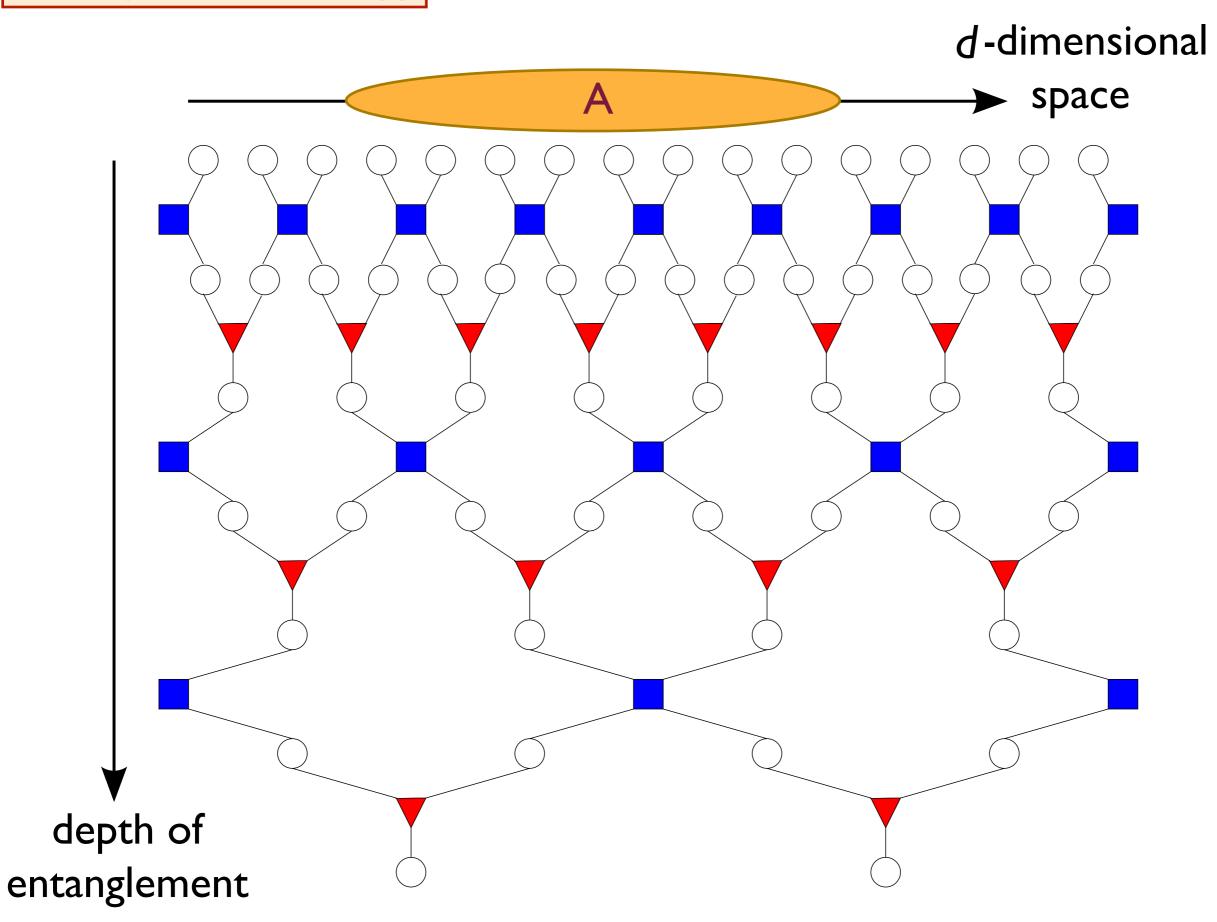
d-dimensional

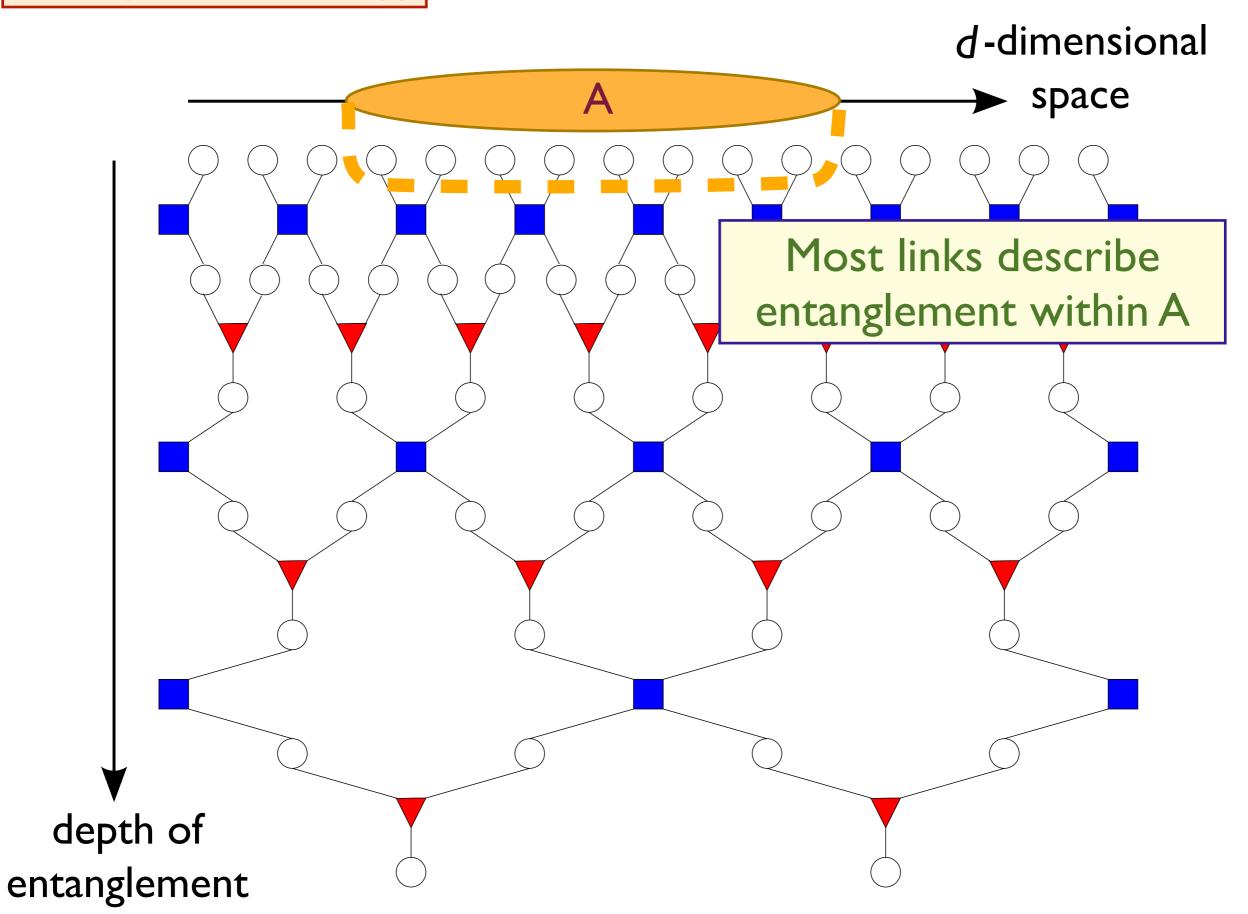


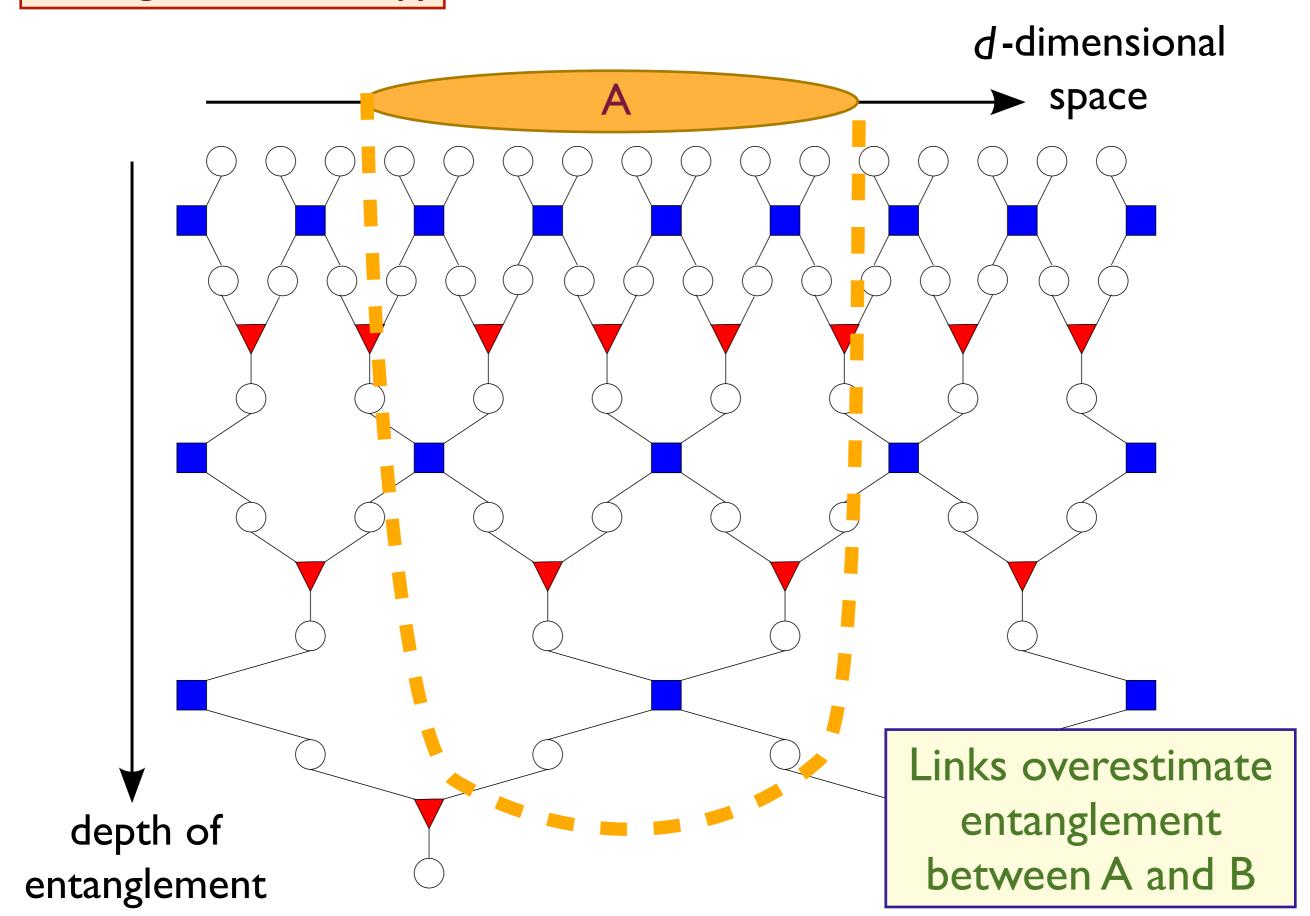


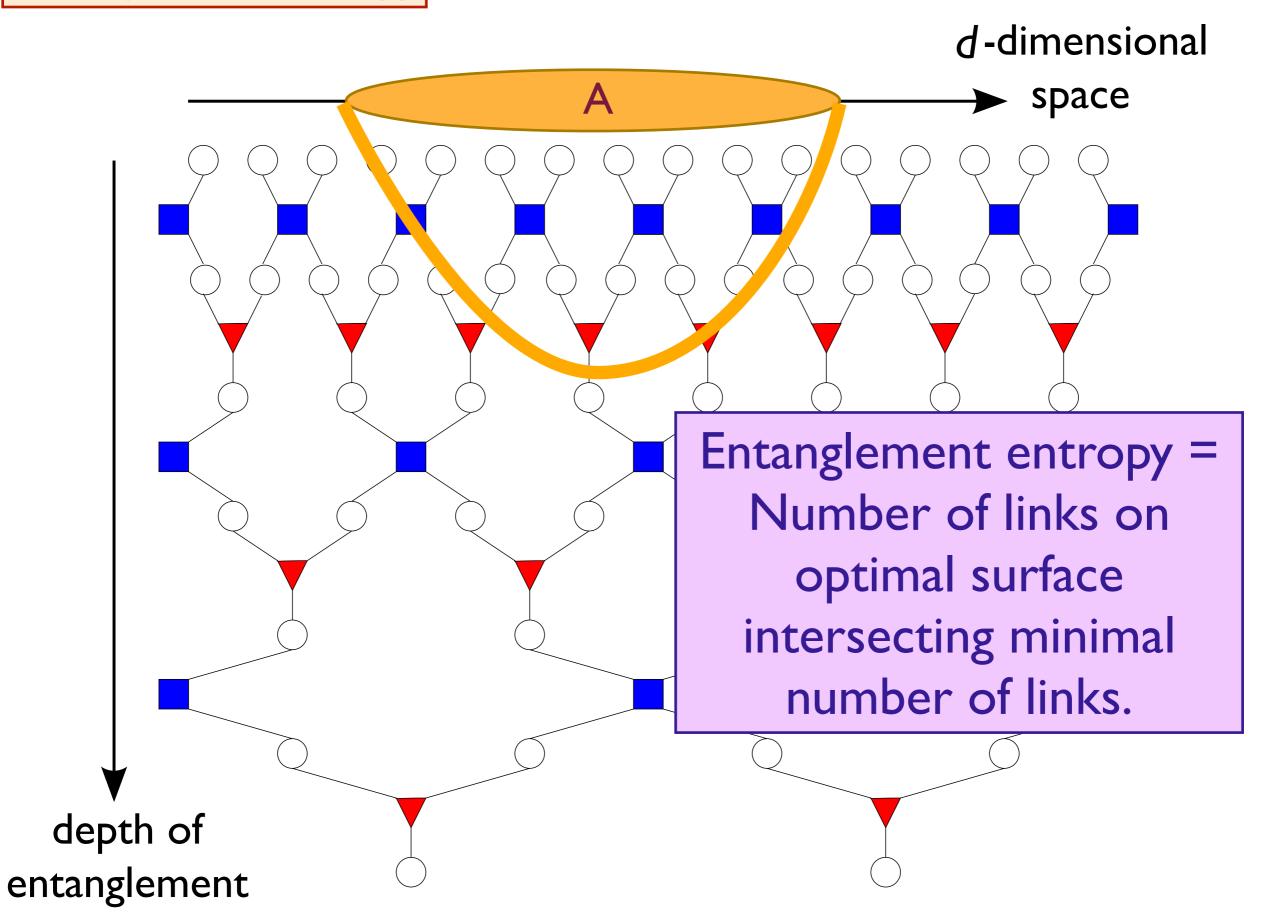
Measure strength of quantum entanglement of region A with region B.

 $\rho_A = \text{Tr}_B \rho = \text{density matrix of region } A$ Entanglement entropy  $S_{EE} = -\text{Tr} \left(\rho_A \ln \rho_A\right)$ 





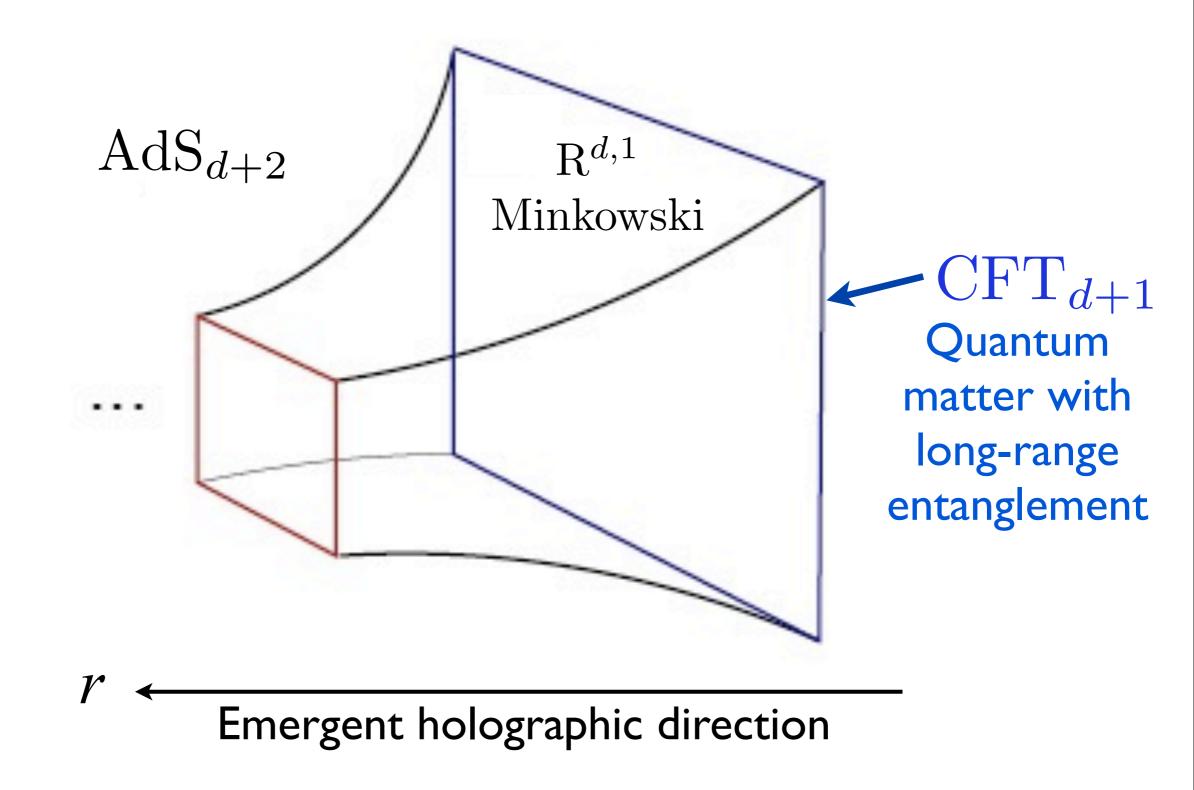




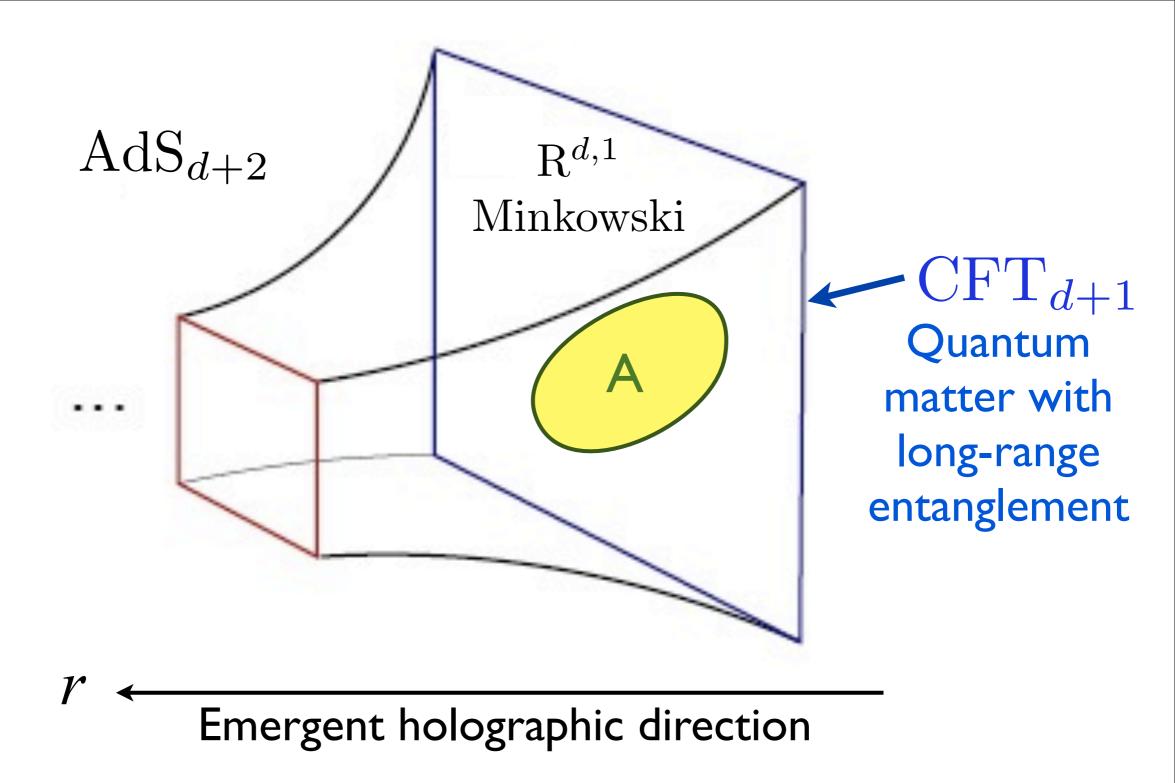
The entanglement entropy of a region A on the boundary equals the minimal area of a surface in the higher-dimensional space whose boundary co-incides with that of A.

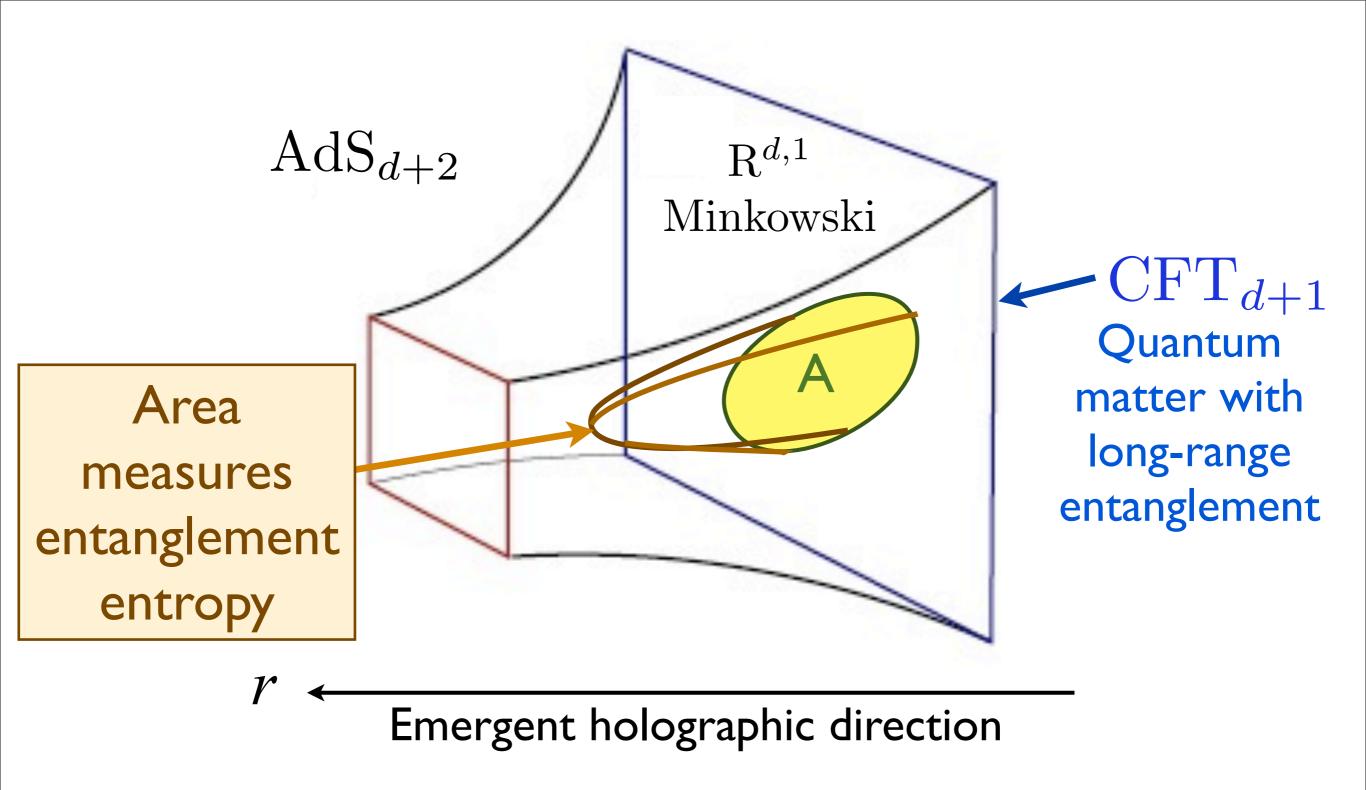
This can be seen both the string and tensor-network pictures

S. Ryu and T. Takayanagi, Phys. Rev. Lett. 96, 18160 (2006). Brian Swingle, arXiv:0905.1317



J. McGreevy, arXiv0909.0518





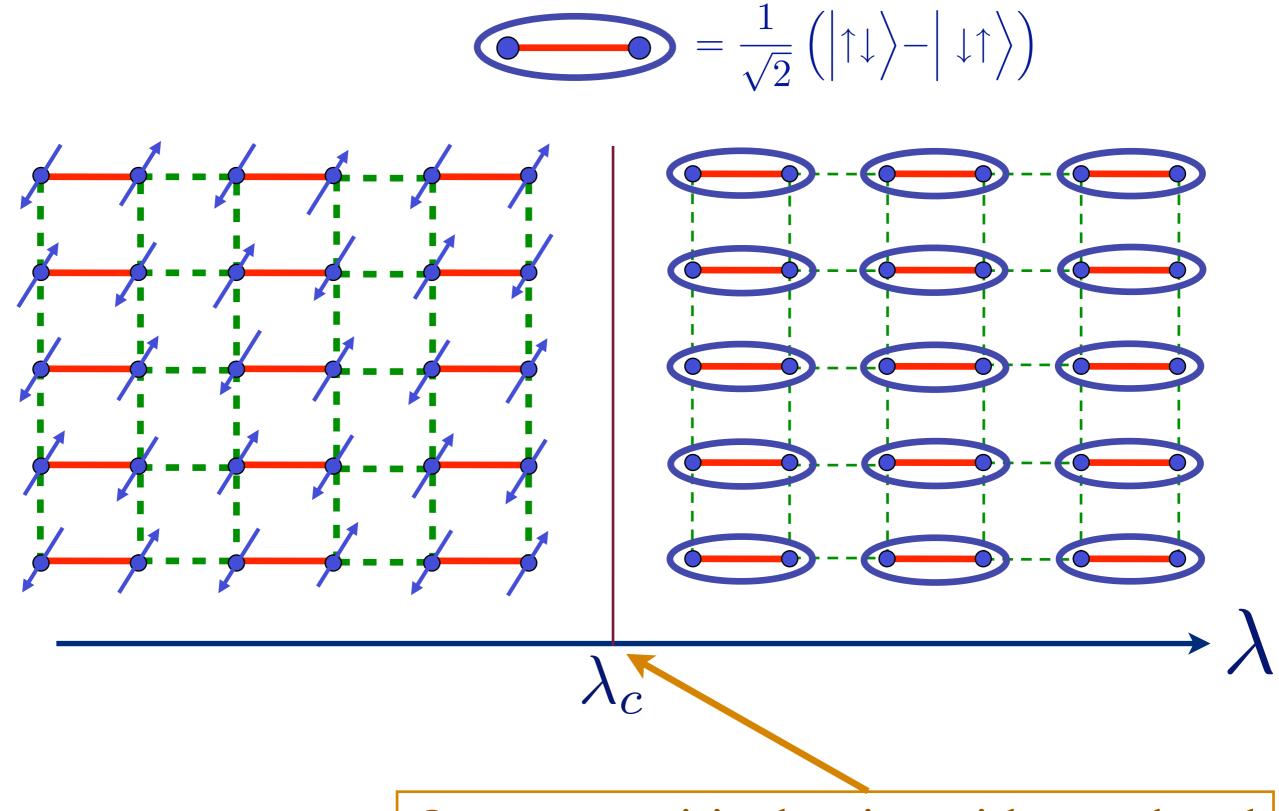
S. Ryu and T. Takayanagi, Phys. Rev. Lett. 96, 18160 (2006).

Quantum superposition and entanglement

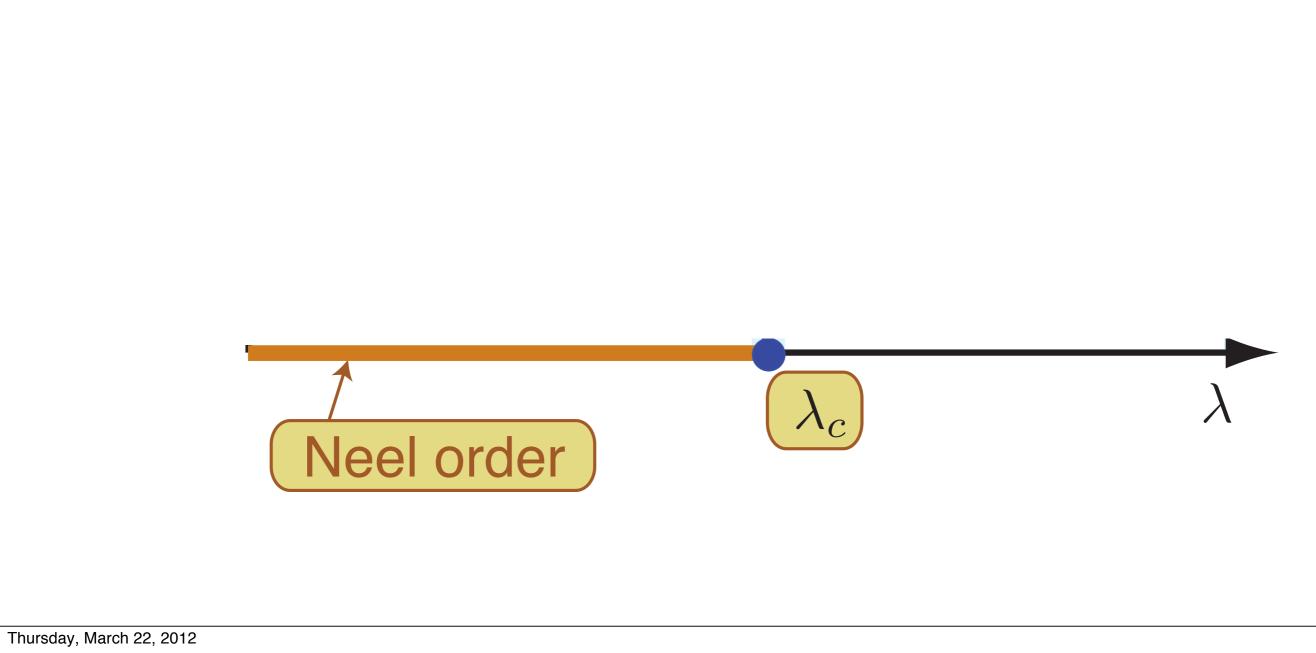
Quantum critical points of electrons in crystals

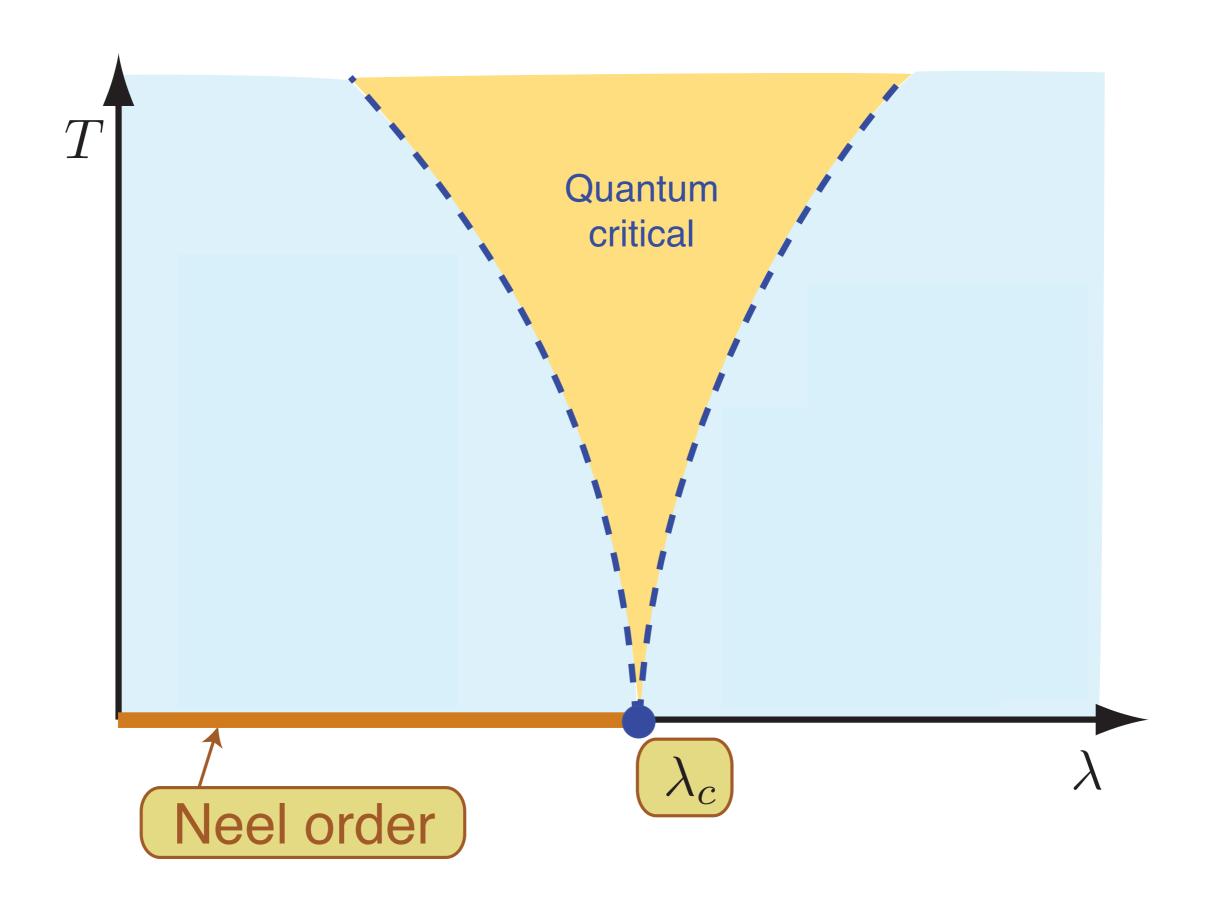
Quantum superposition and entanglement

Quantum critical points of electrons in crystals

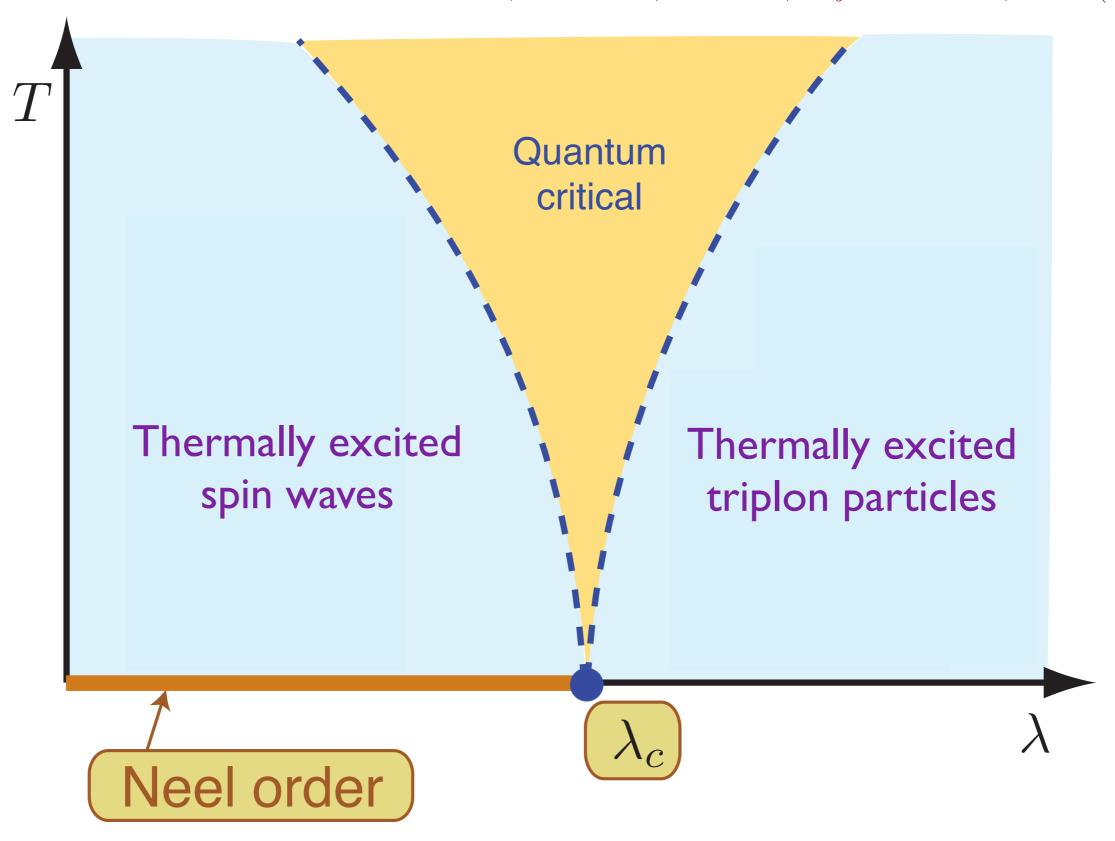


Quantum critical point with non-local entanglement in spin wavefunction

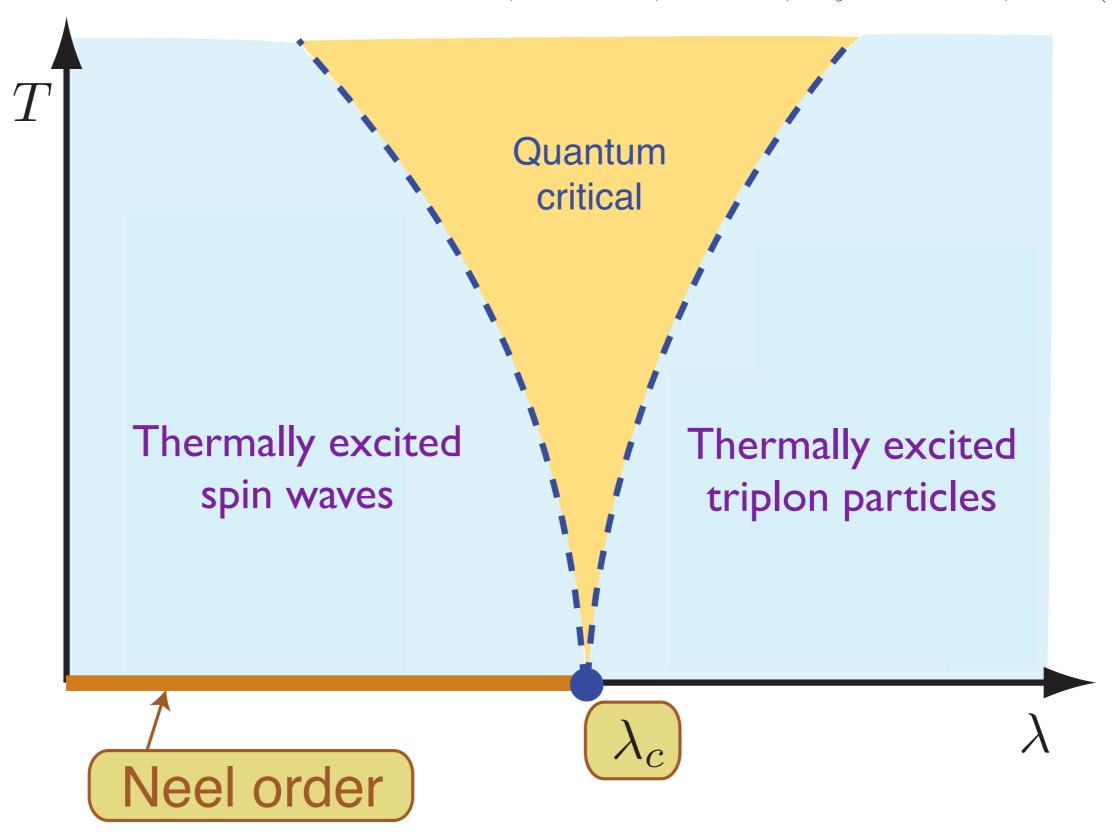




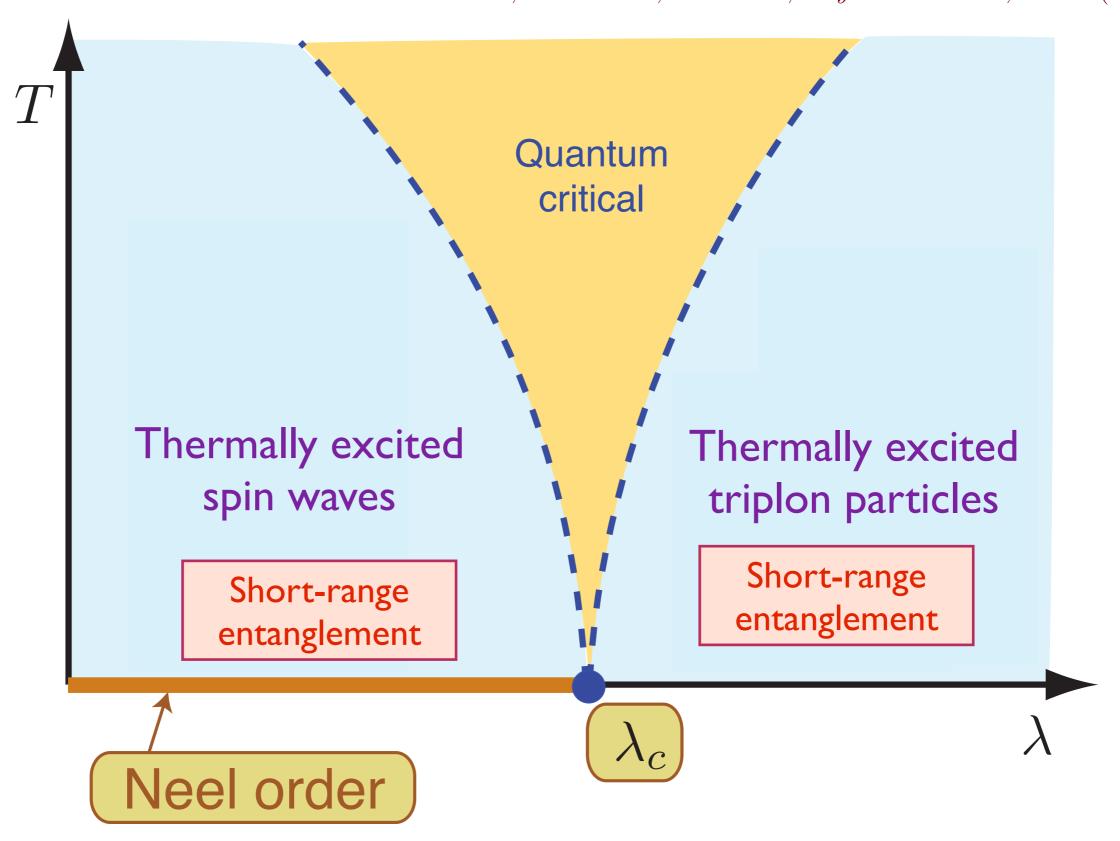
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).



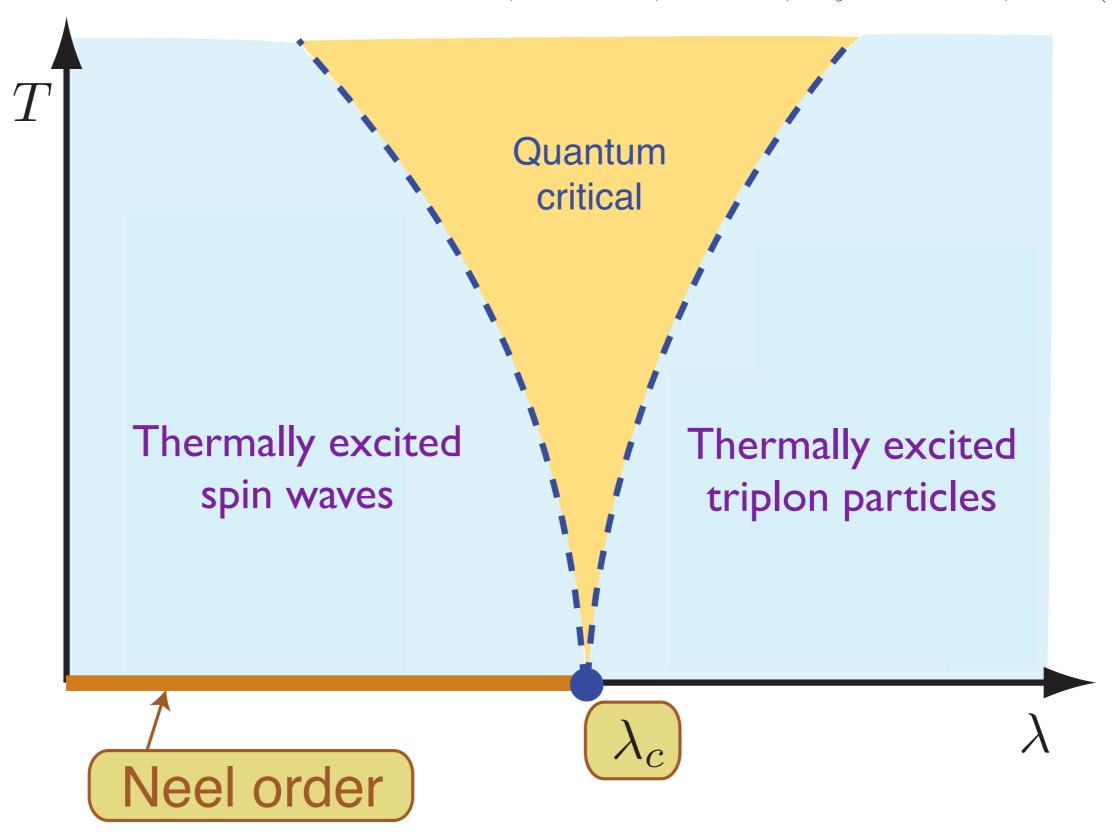
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).



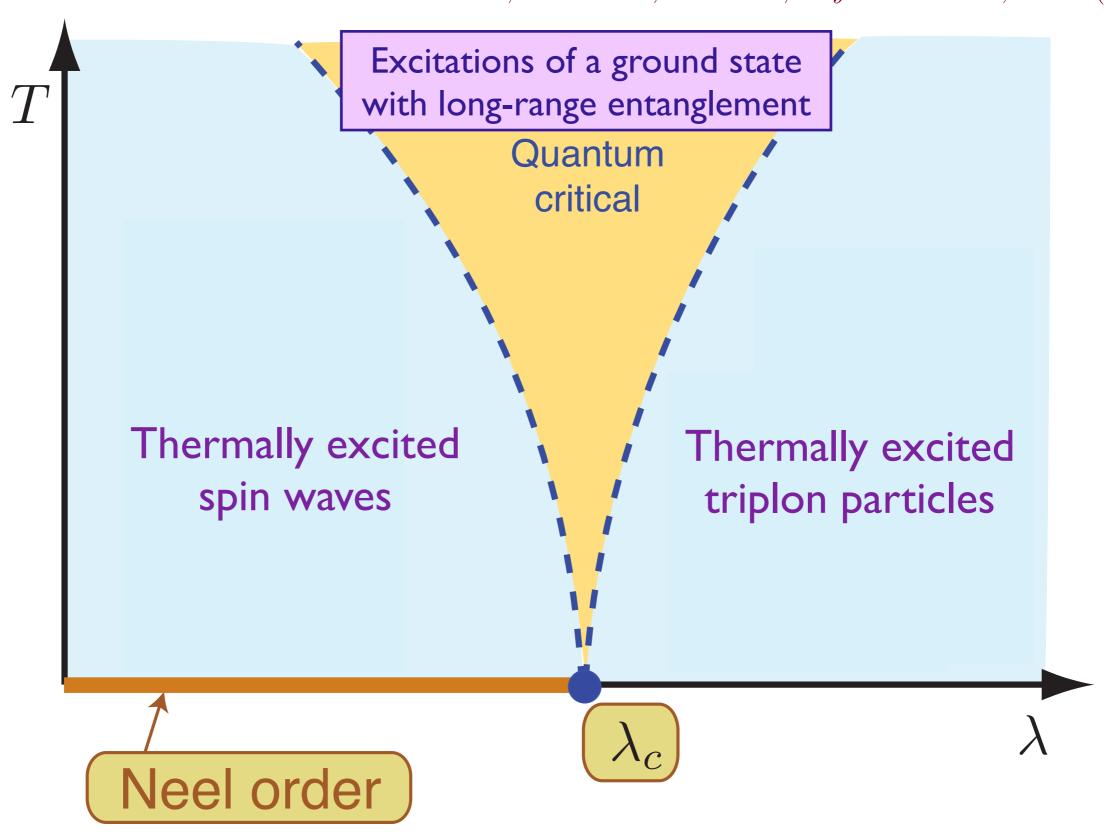
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).



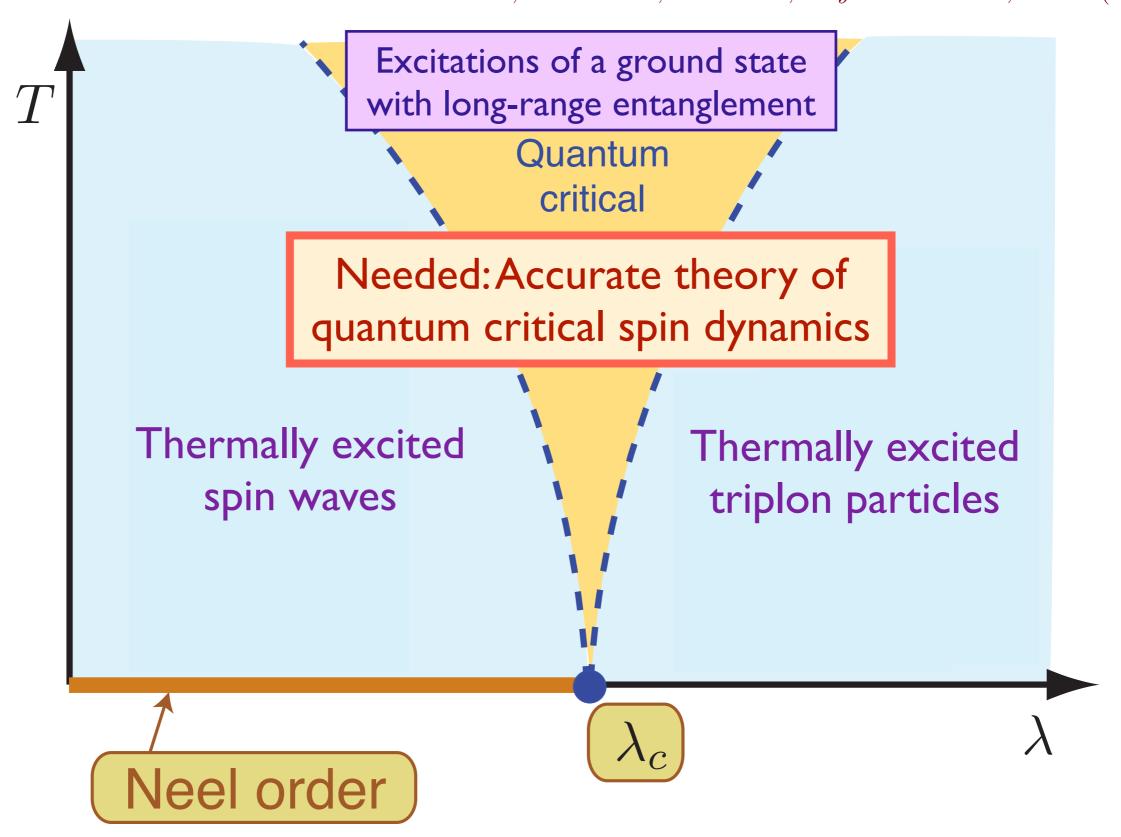
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).

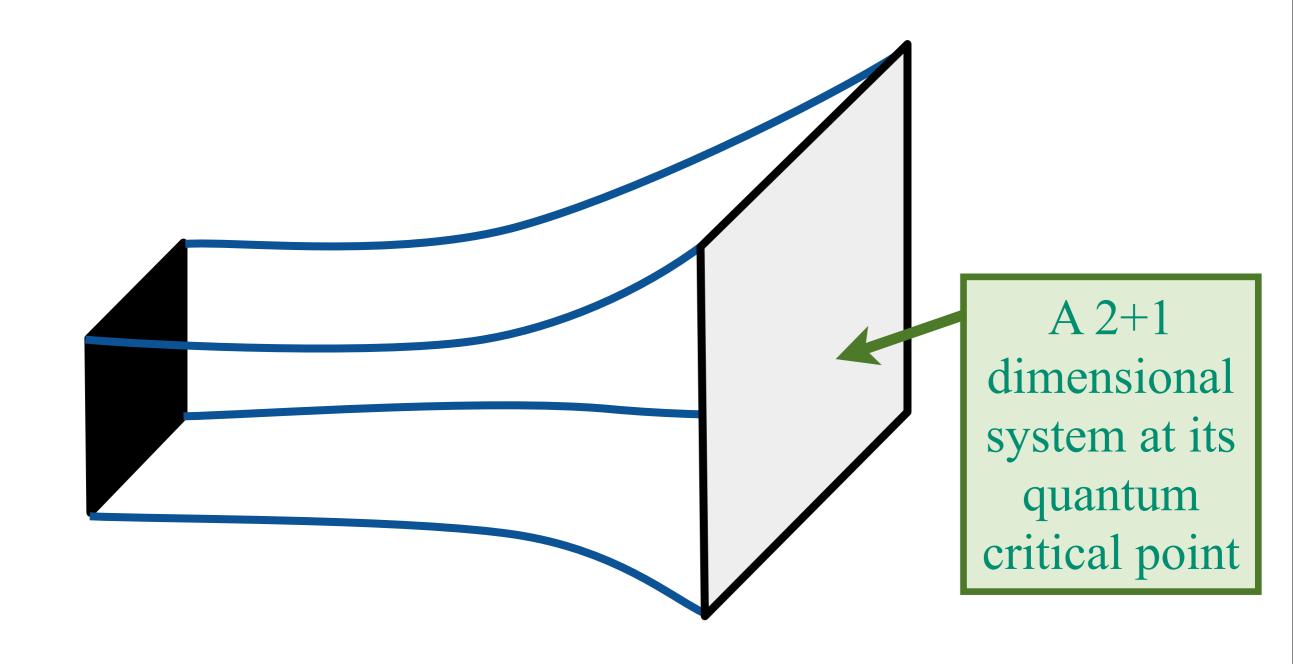


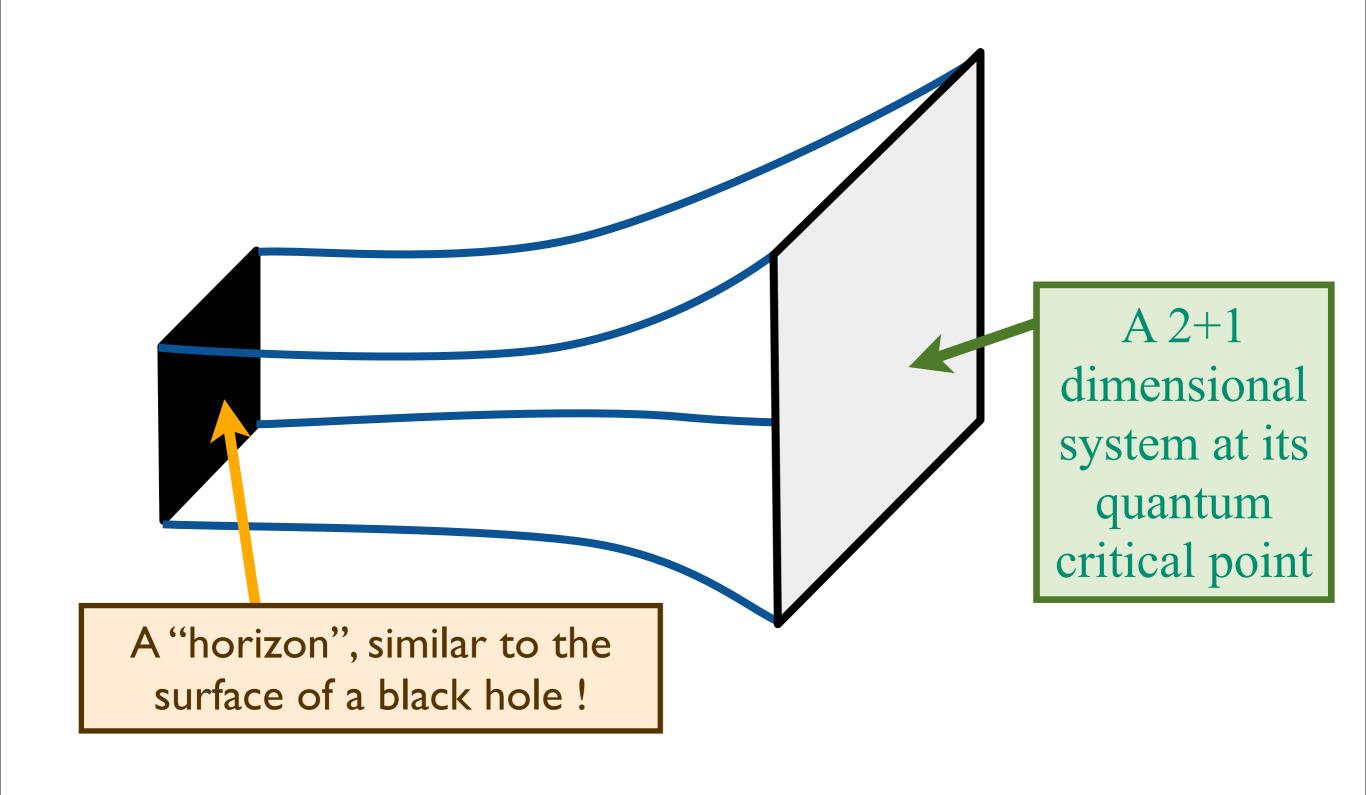
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).



S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).

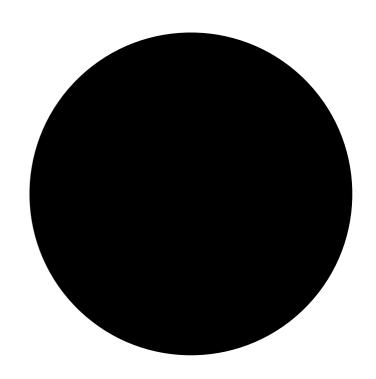






#### **Black Holes**

Objects so massive that light is gravitationally bound to them.

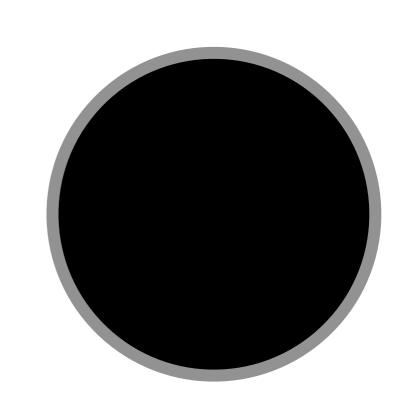


#### **Black Holes**

Objects so massive that light is gravitationally bound to them.

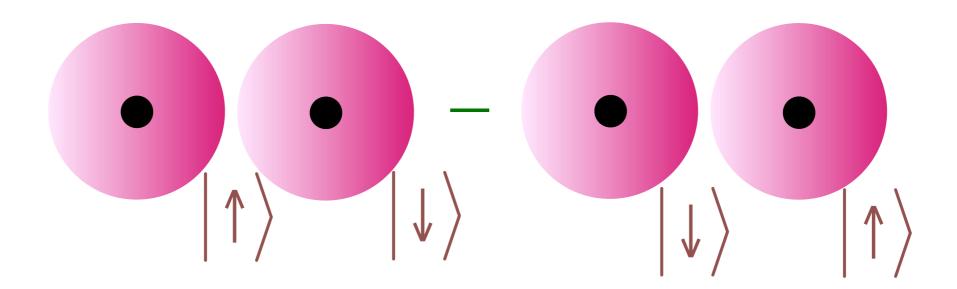
In Einstein's theory, the region inside the black hole horizon is disconnected from the rest of the universe.

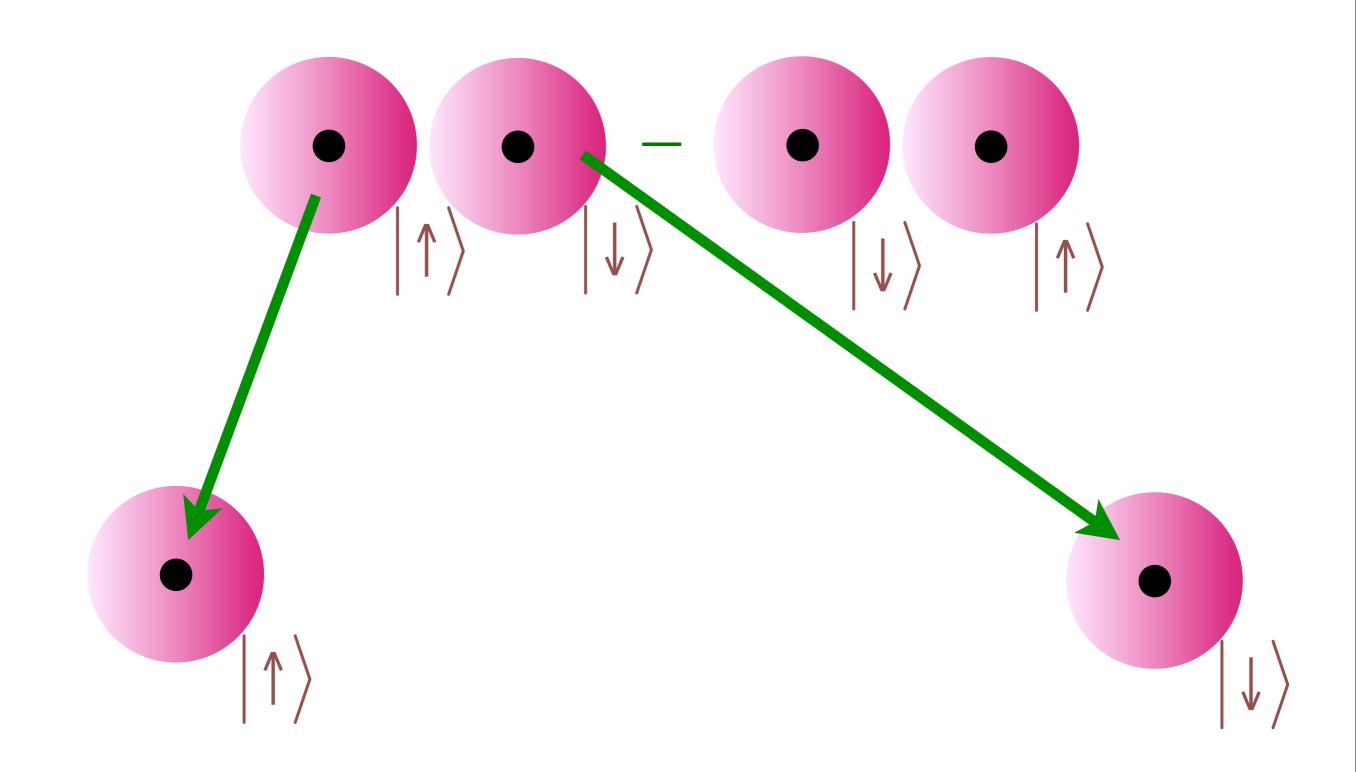
Horizon radius 
$$R = \frac{2GM}{c^2}$$

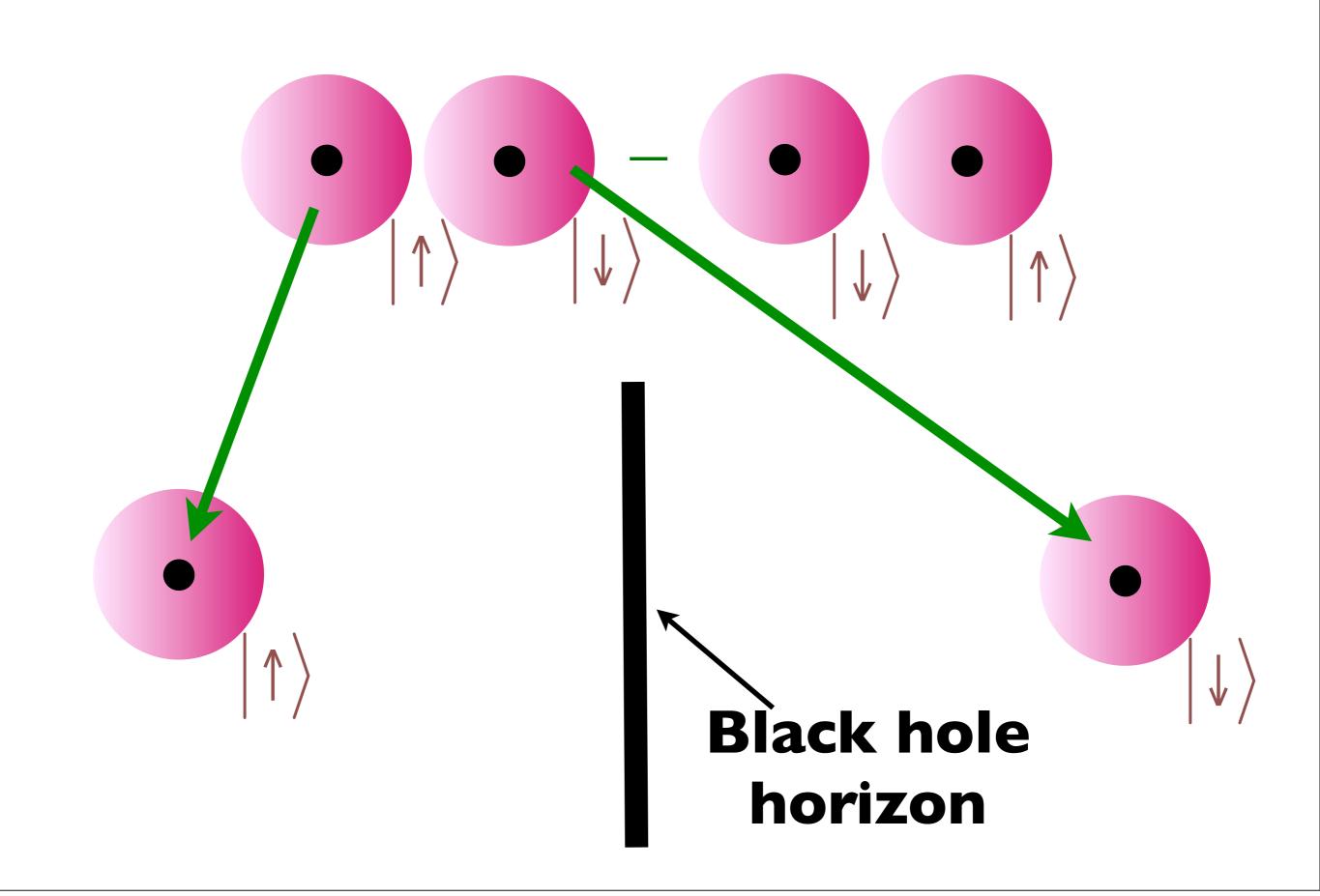


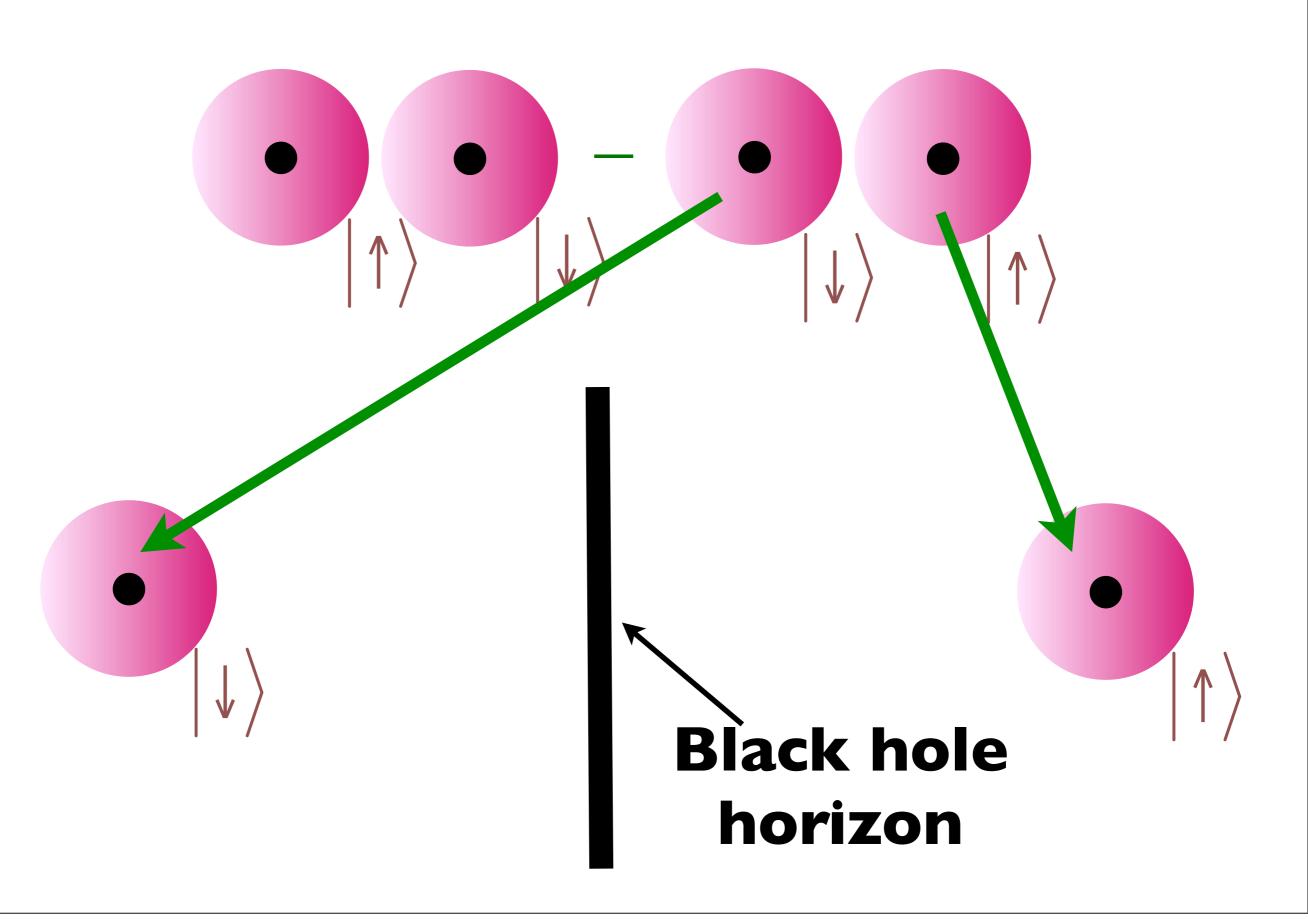
# Black Holes + Quantum theory

Around 1974, Bekenstein and Hawking showed that the application of the quantum theory across a black hole horizon led to many astonishing conclusions

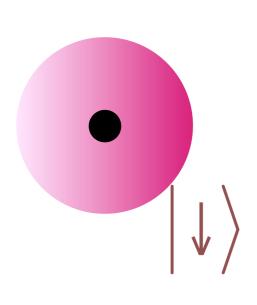


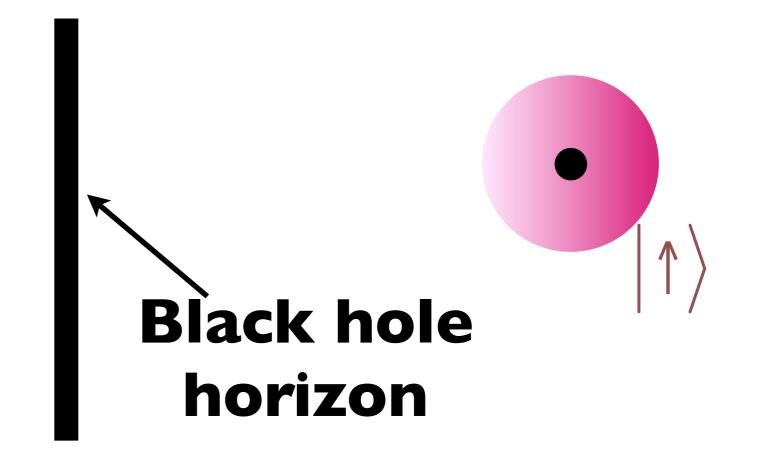




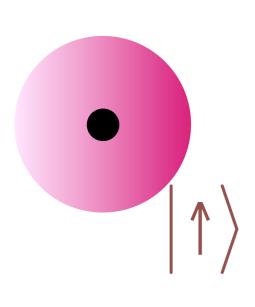


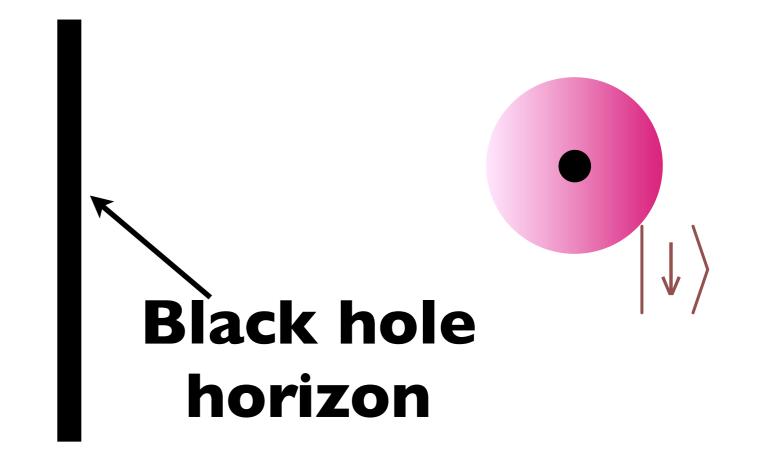
There is a non-local quantum entanglement between the inside and outside of a black hole





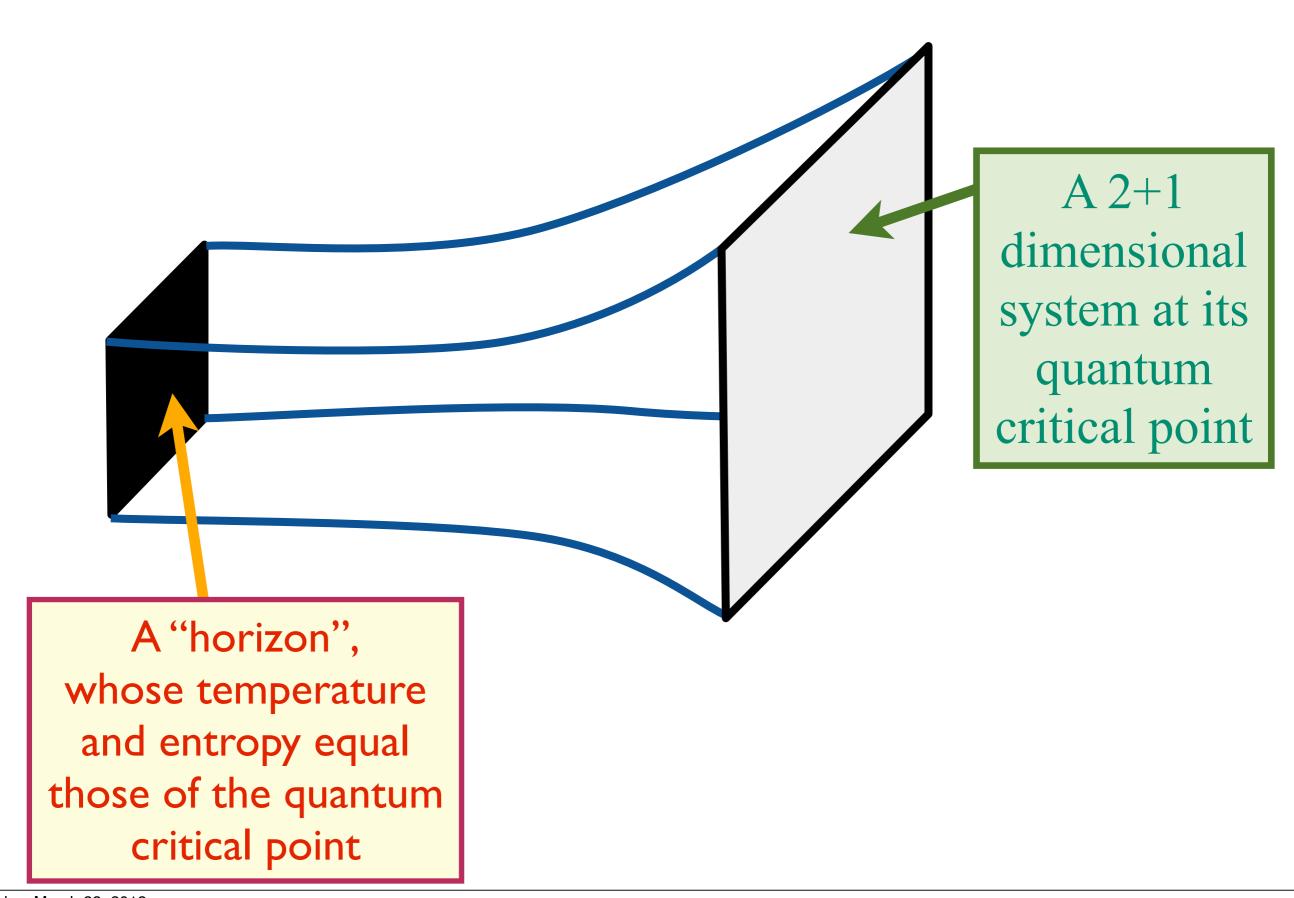
There is a non-local quantum entanglement between the inside and outside of a black hole

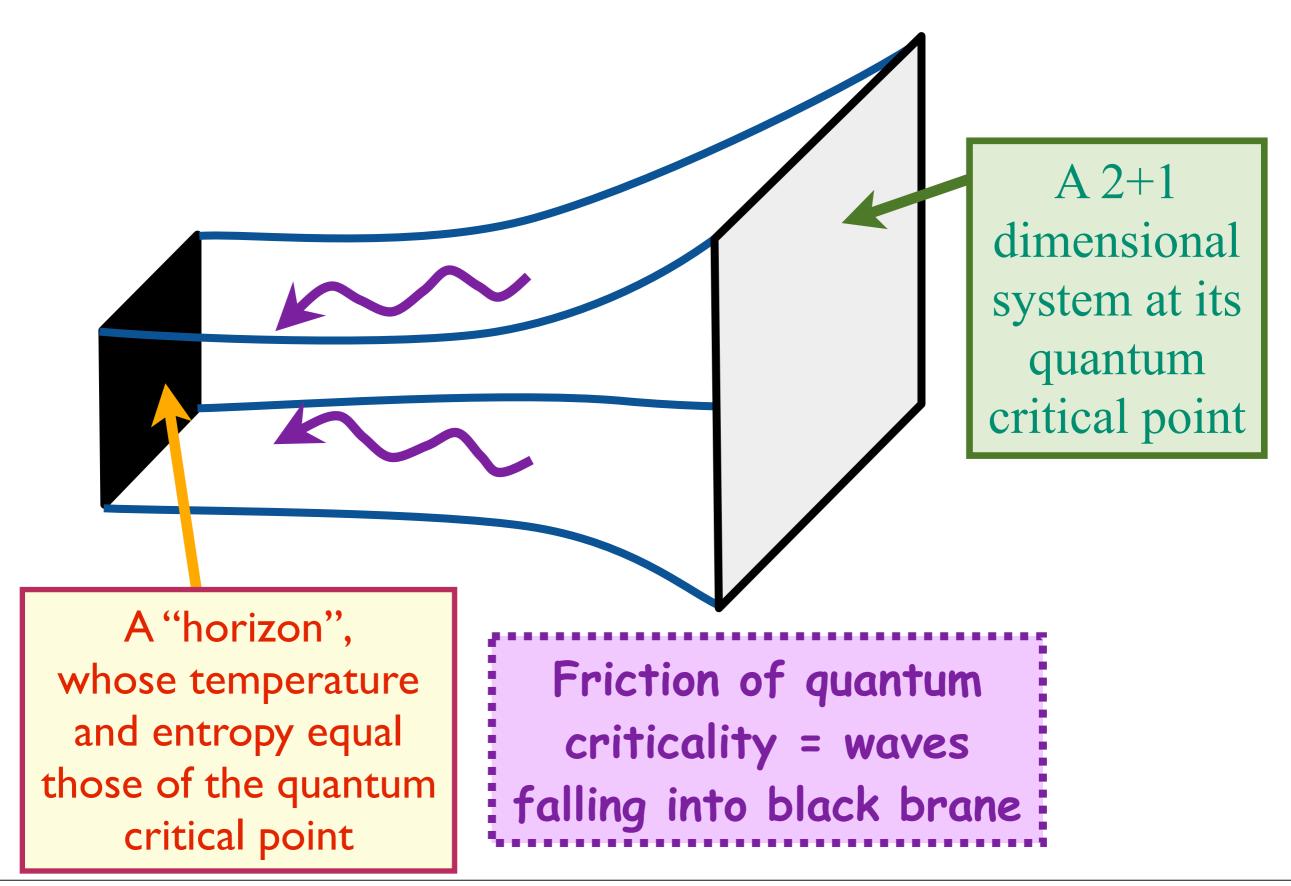


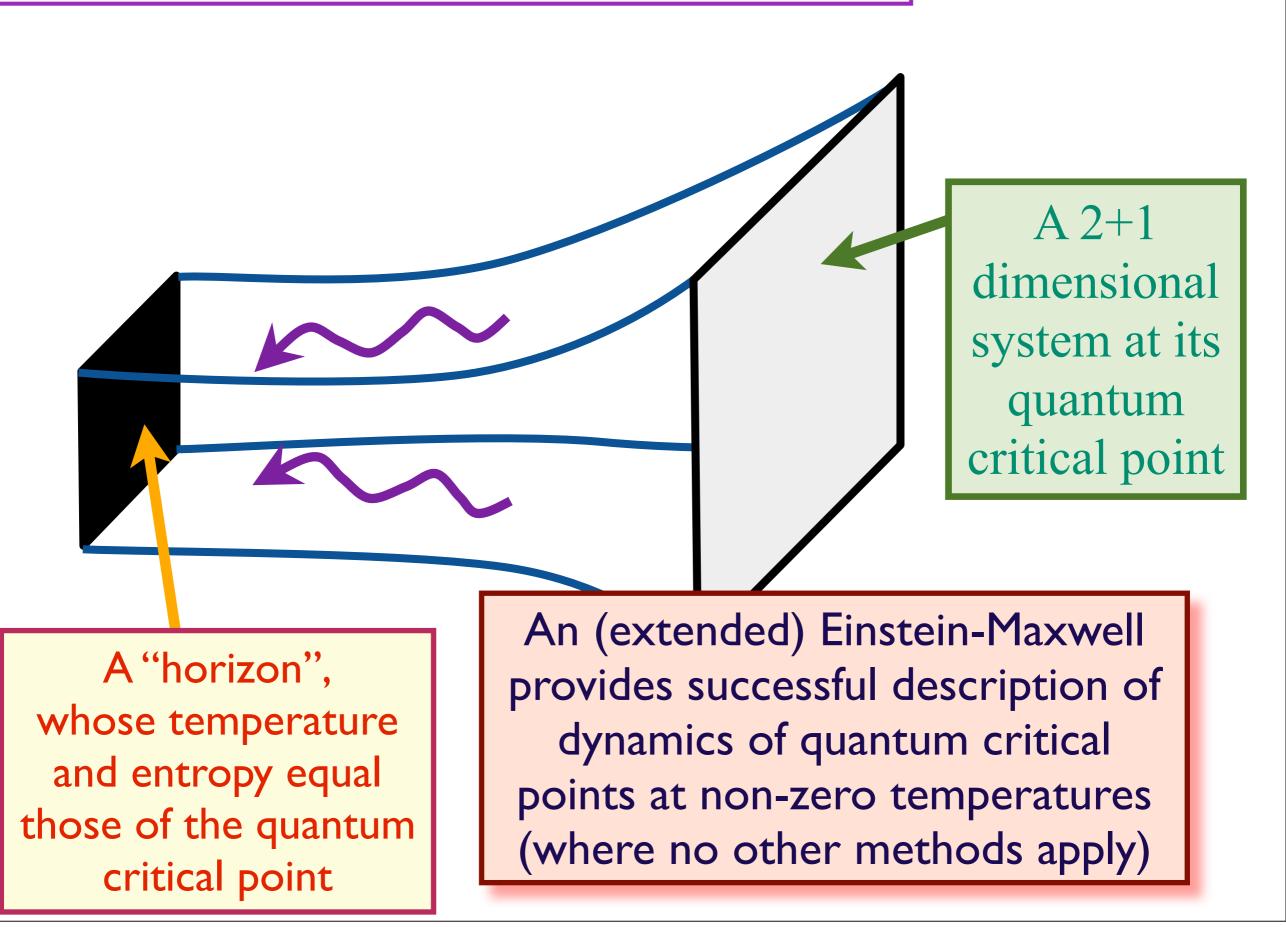


There is a non-local quantum entanglement between the inside and outside of a black hole

This entanglement leads to a black hole temperature (the Hawking temperature) and a black hole entropy (the Bekenstein entropy)







Quantum superposition and entanglement

Quantum critical points of electrons in crystals

String theory and black holes

Quantum superposition and entanglement

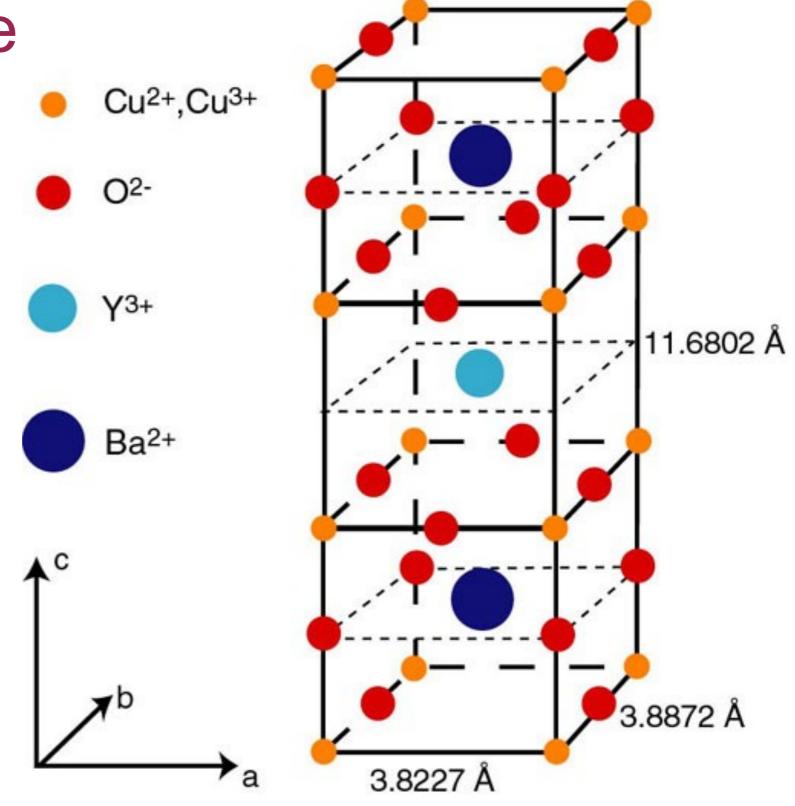
Quantum critical points of electrons in crystals

String theory and black holes

Metals, "strange metals", and high temperature superconductors

Insights from gravitational "duals"

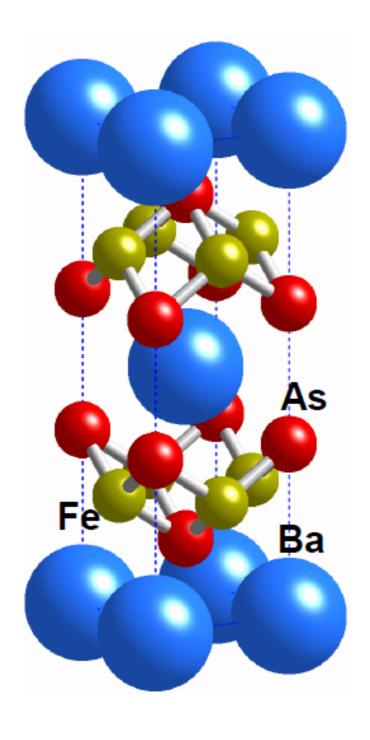
# High temperature superconductors

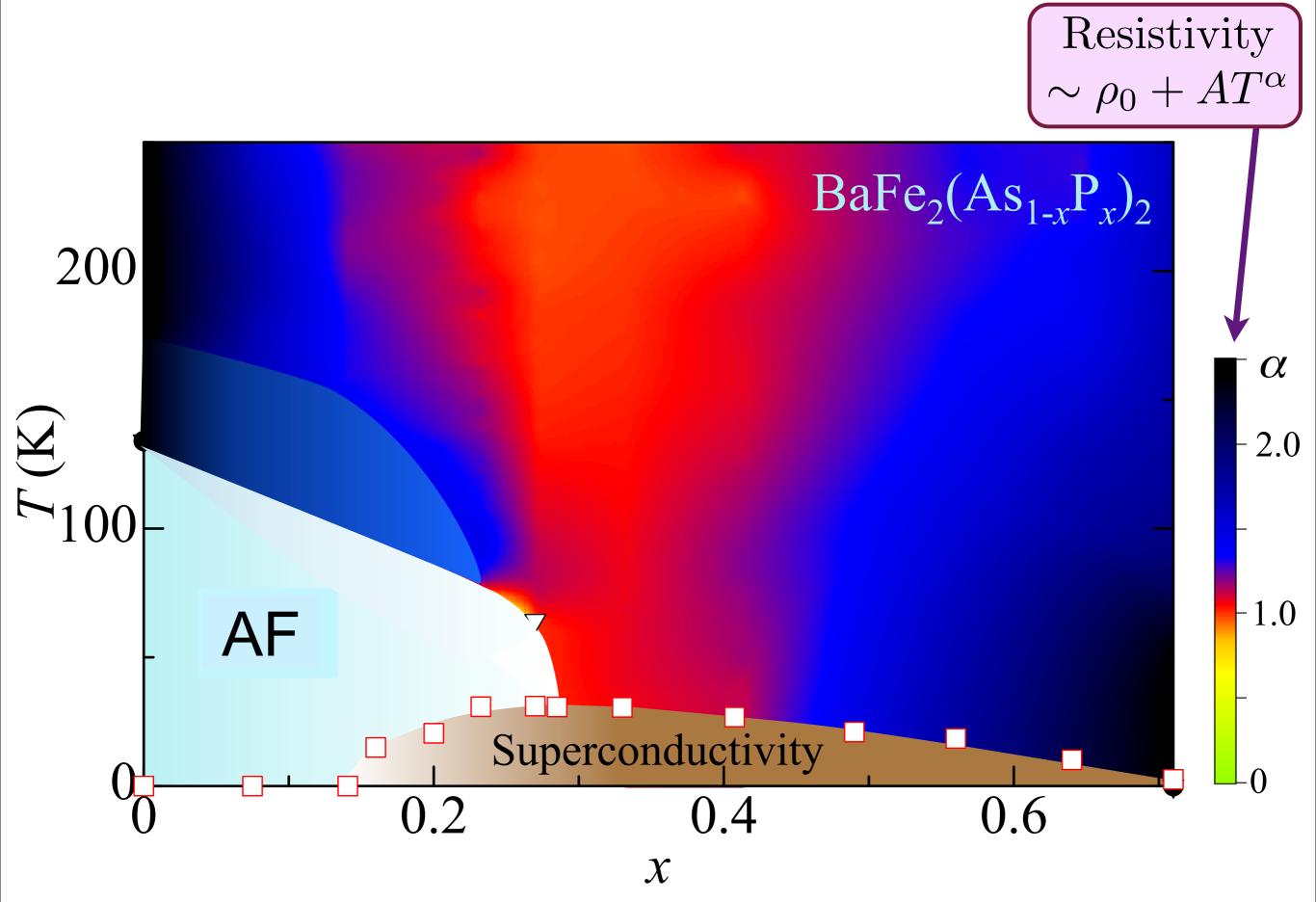


 $YBa_2Cu_3O_{6+x}$ 

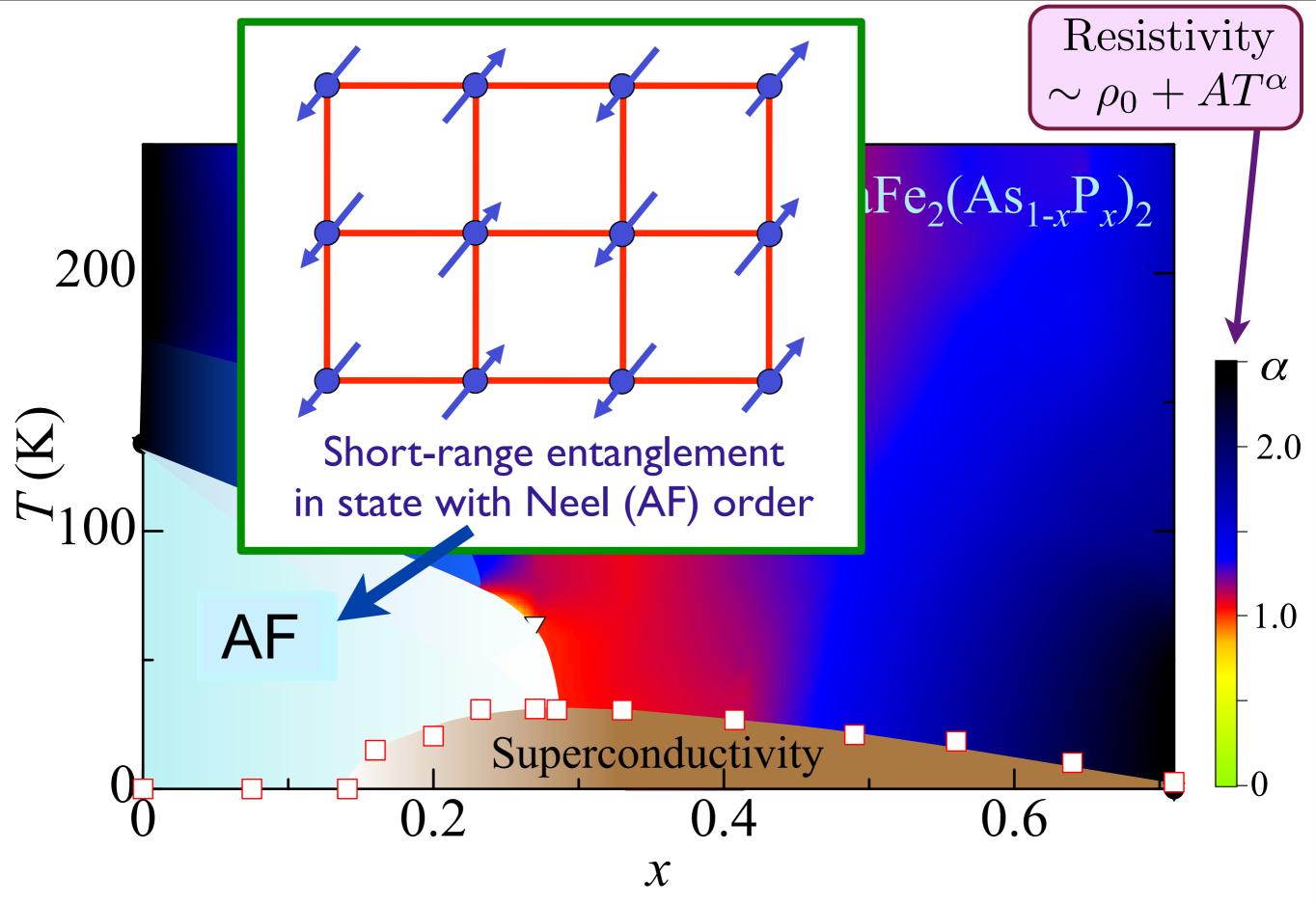
#### Iron pnictides:

a new class of high temperature superconductors

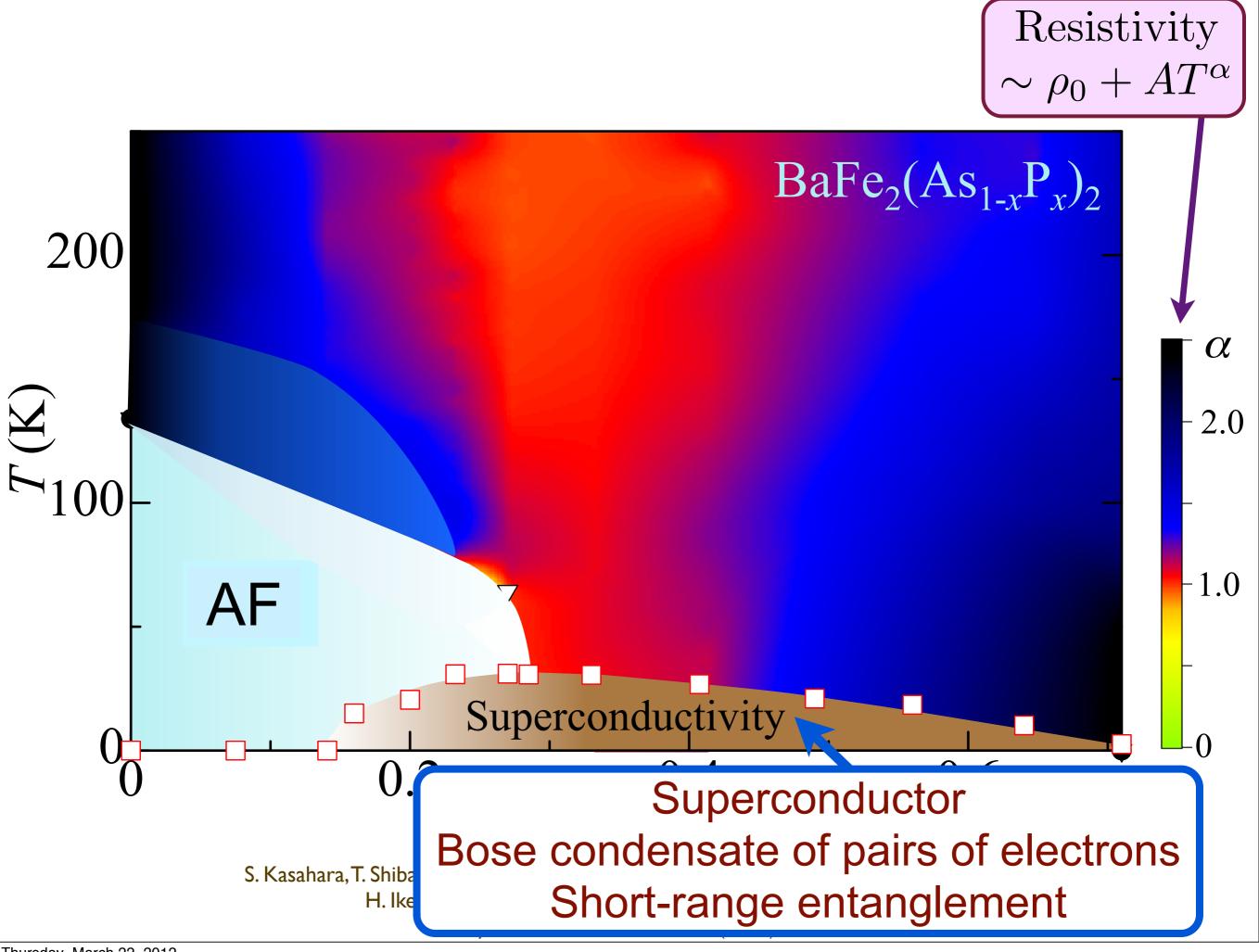


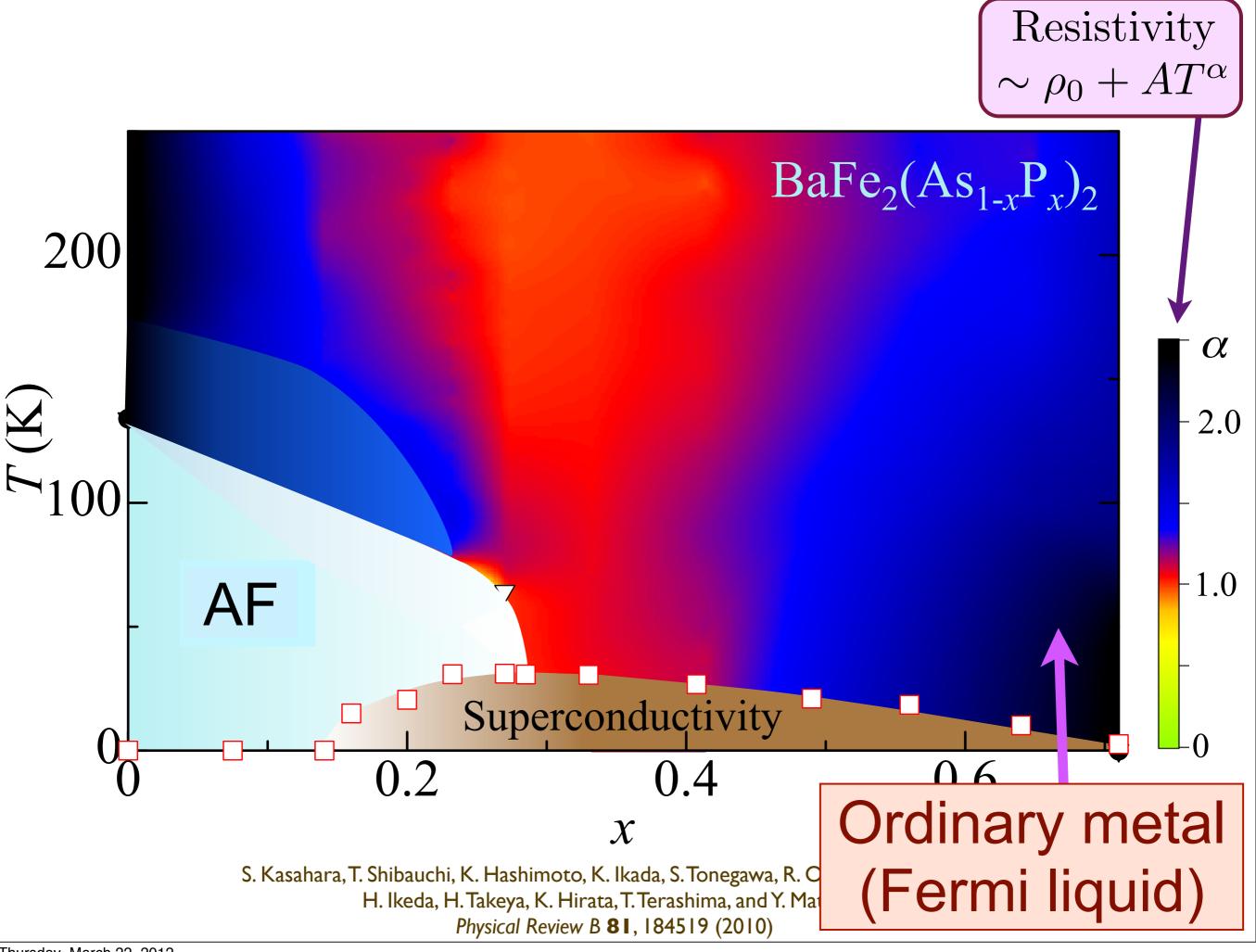


S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)

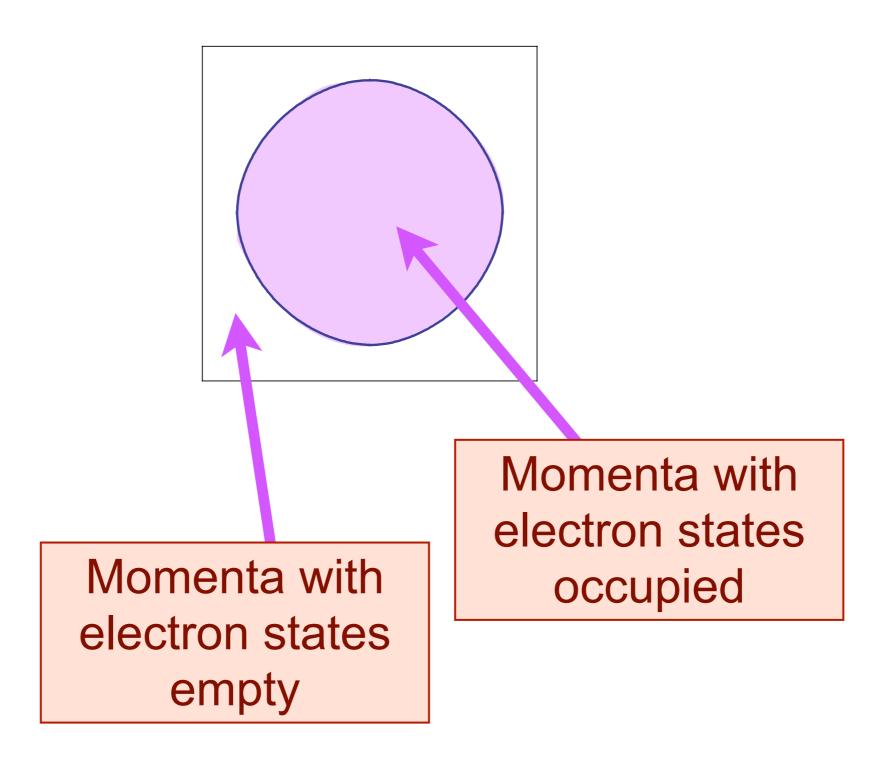


S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)

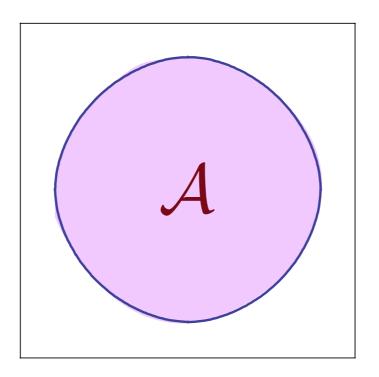




### Sommerfeld-Bloch theory of ordinary metals

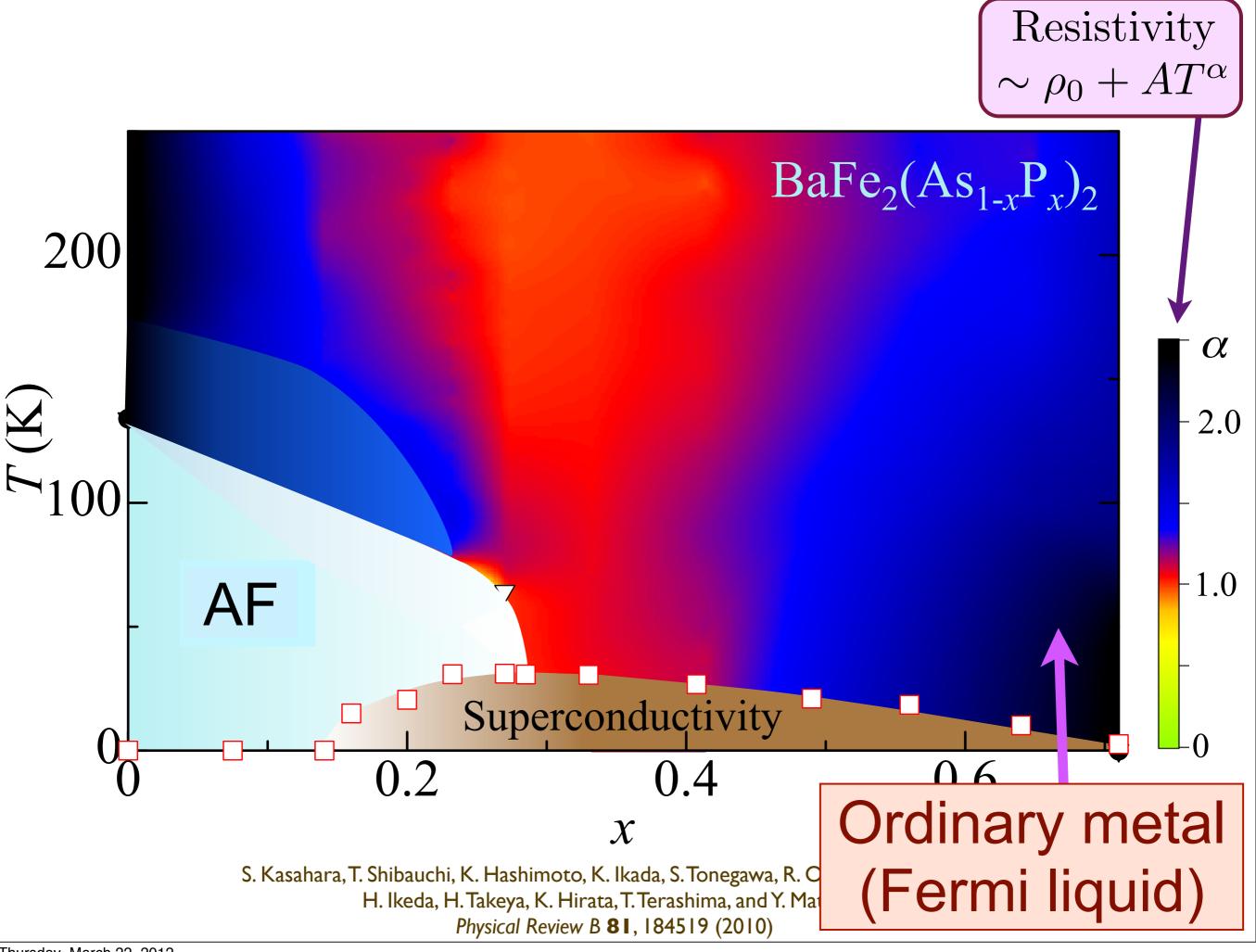


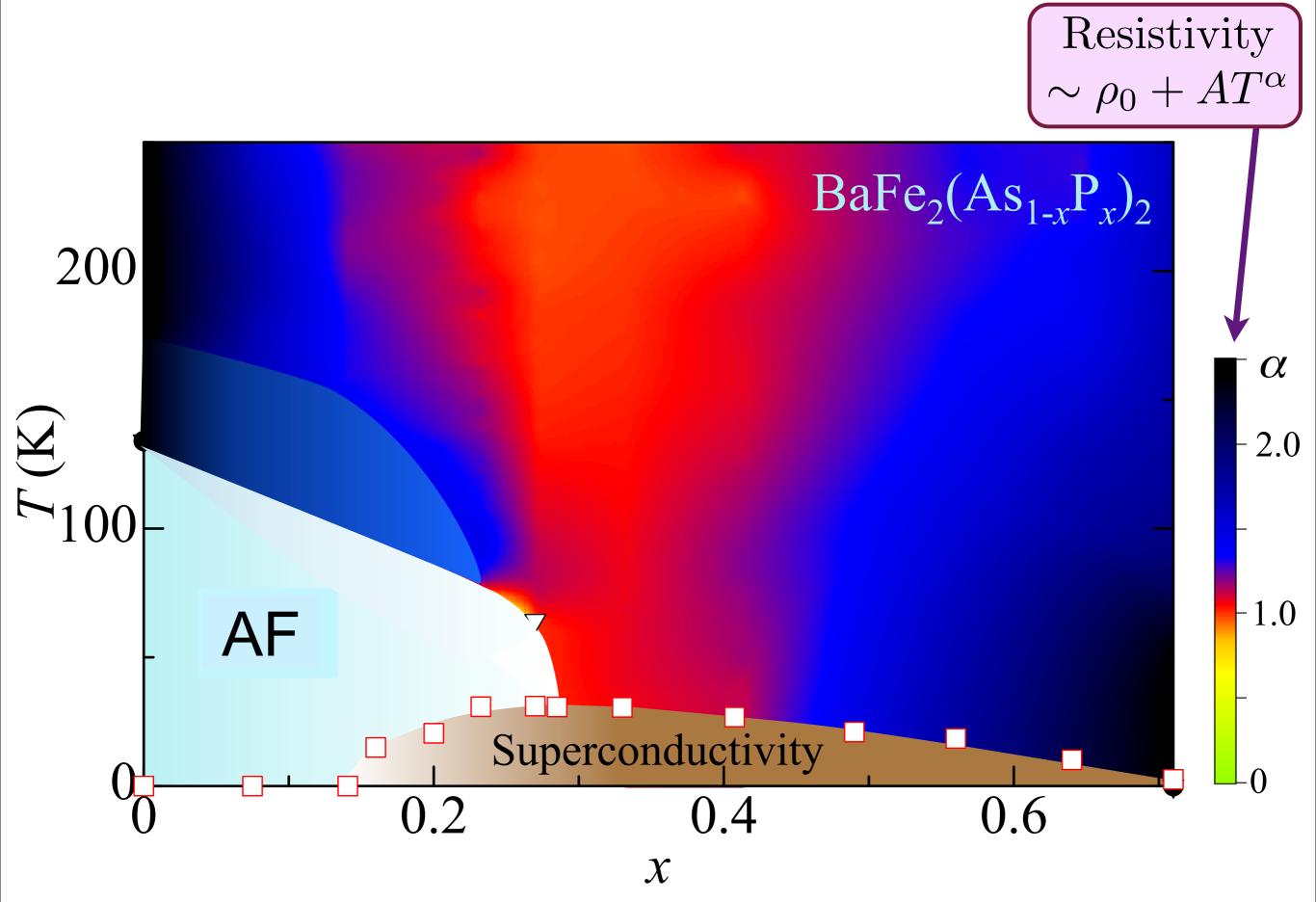
#### Sommerfeld-Bloch theory of ordinary metals



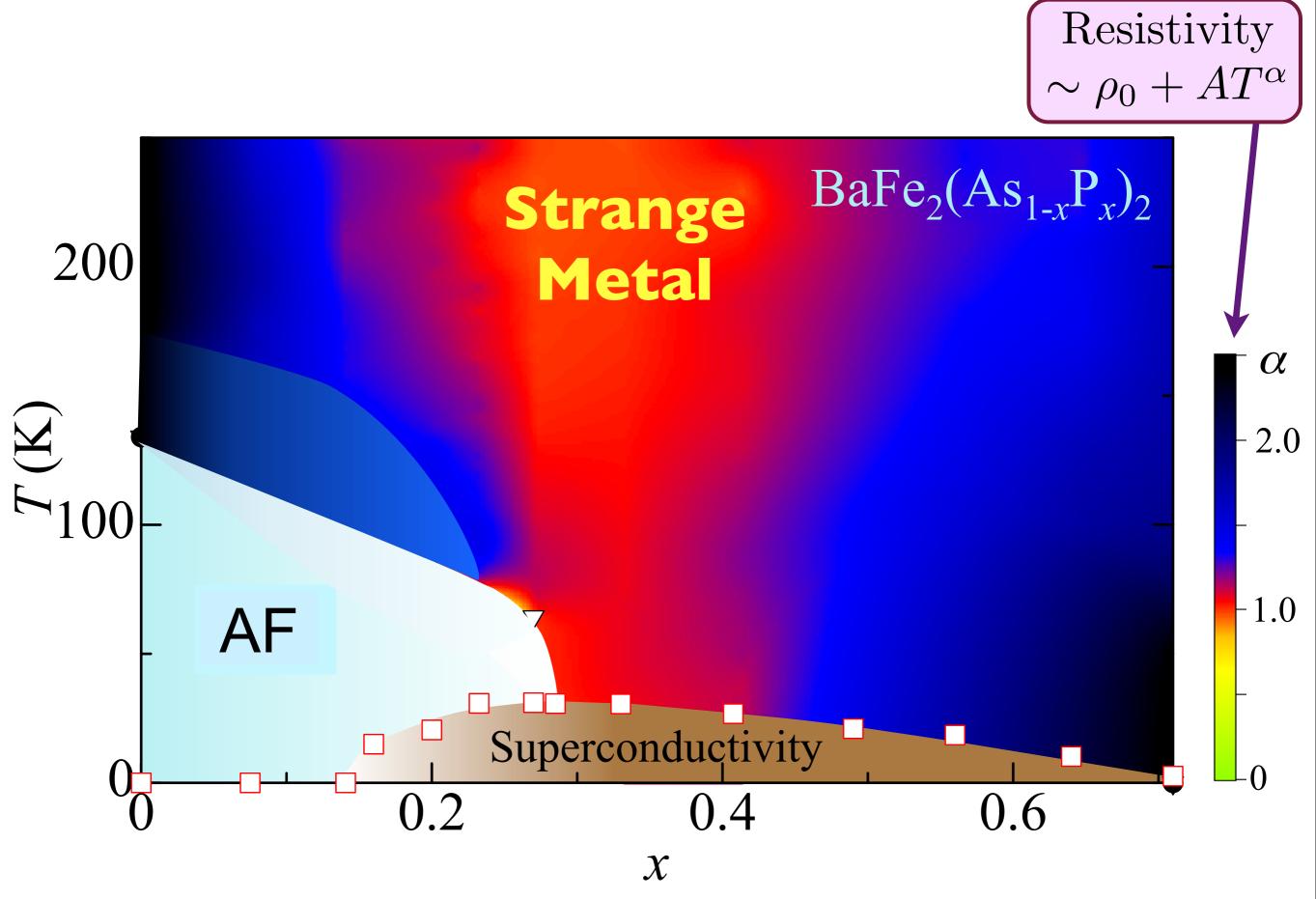
# Key feature of the theory: the **Fermi surface**

- Area enclosed by the Fermi surface  $\mathcal{A} = \mathcal{Q}$ , the electron density
- Excitations near the Fermi surface are responsible for the familiar properties of ordinary metals, such as resistivity  $\sim T^2$ .



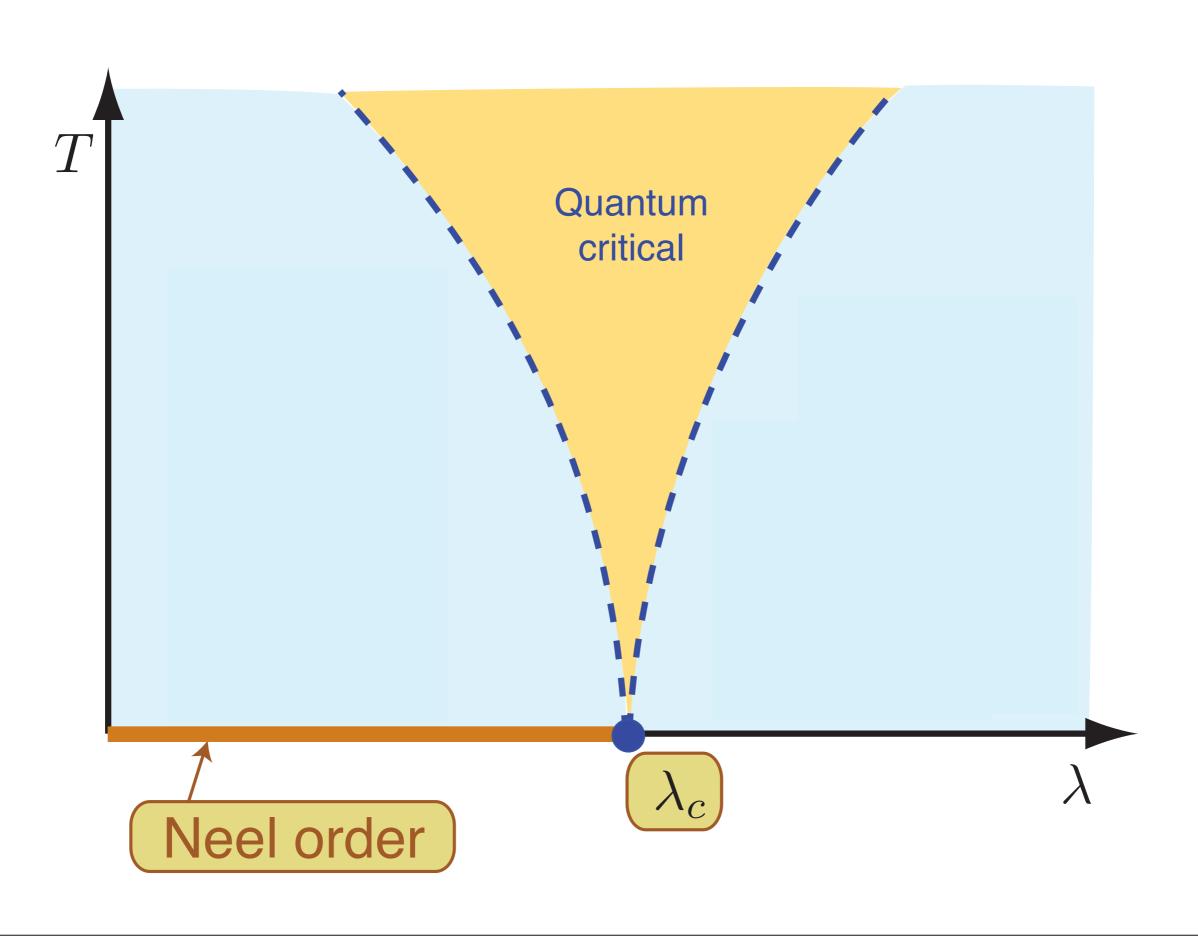


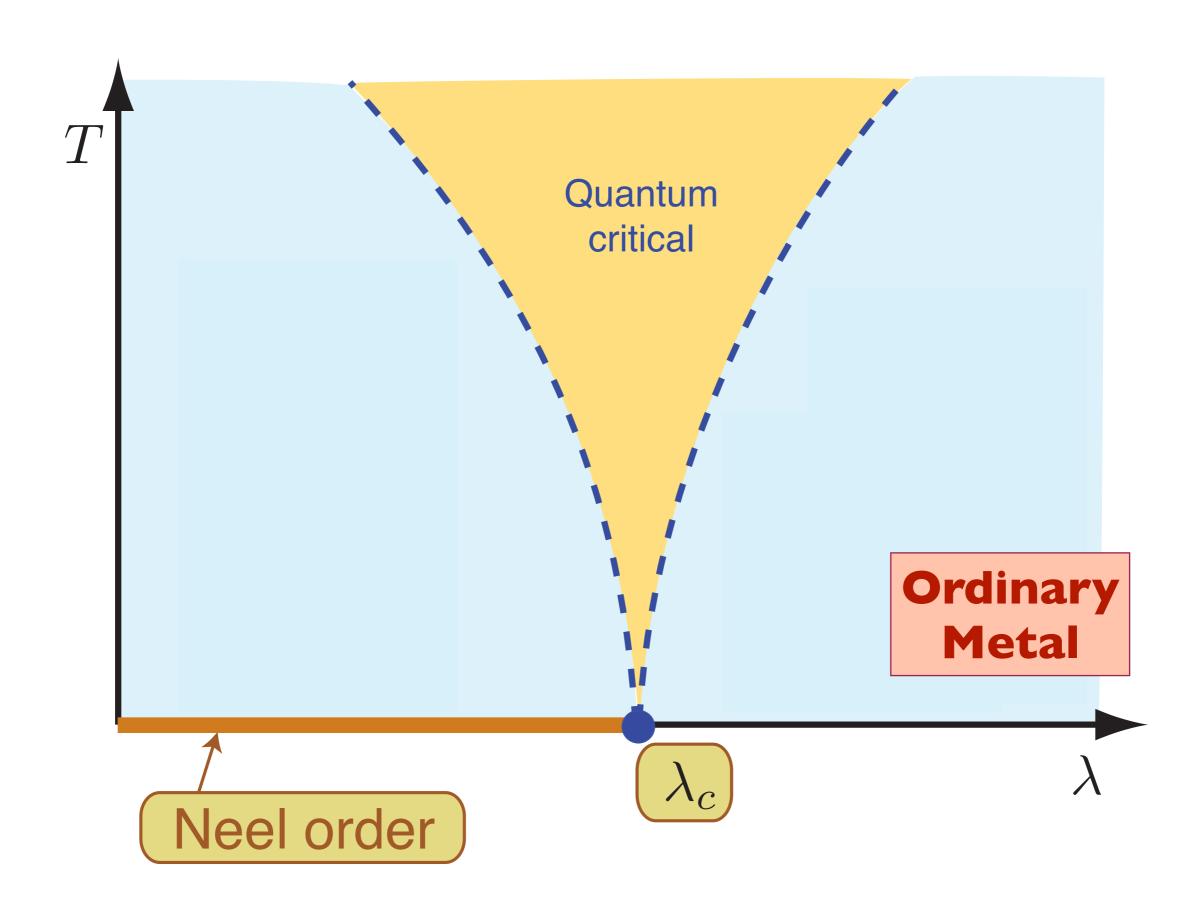
S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)

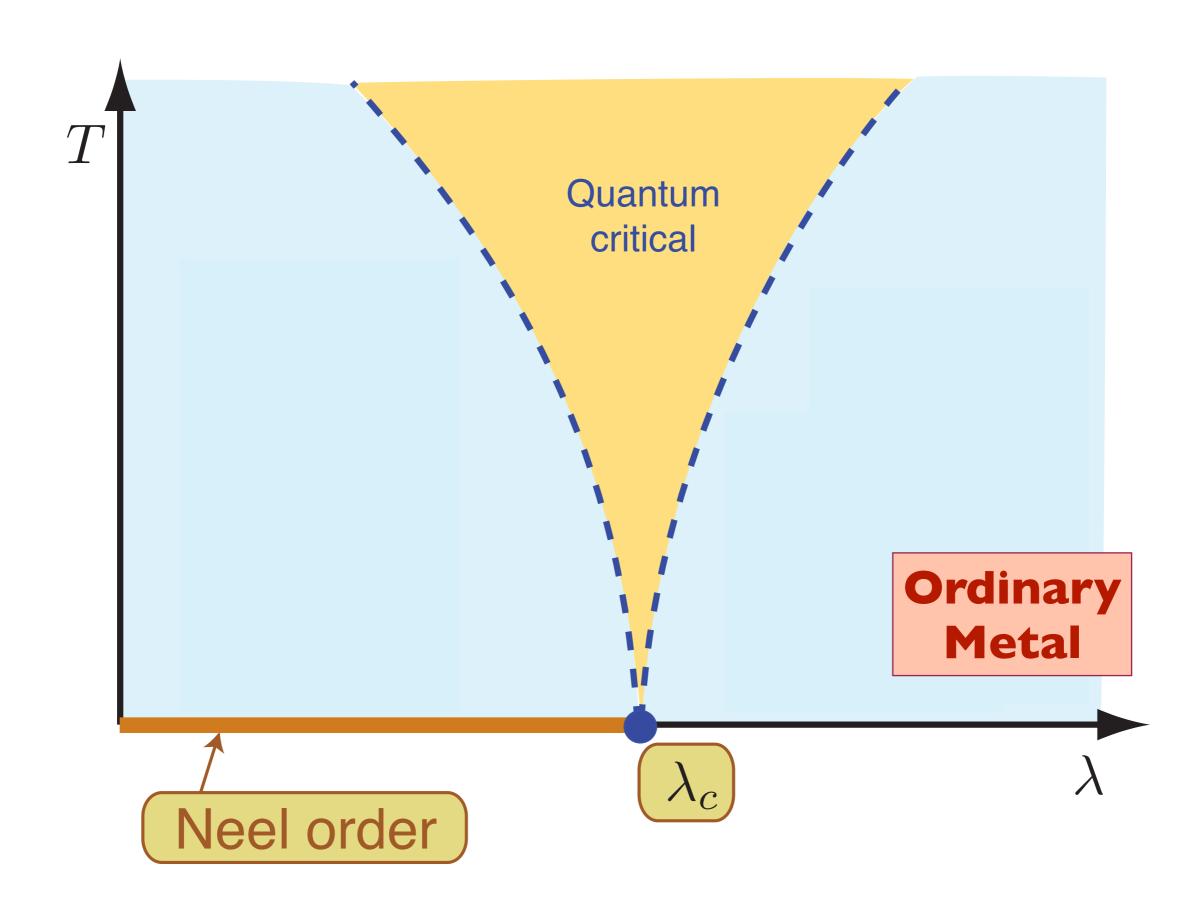


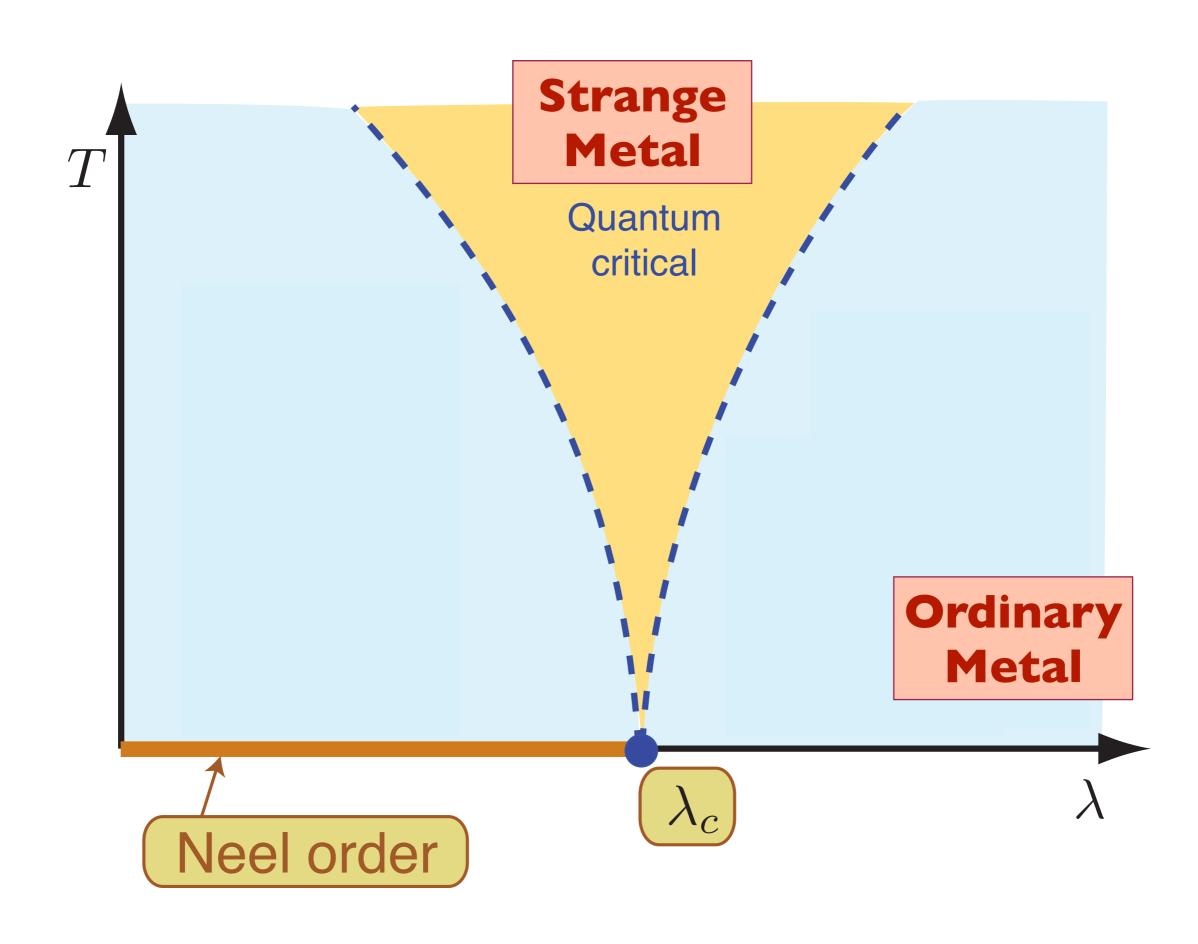
S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)

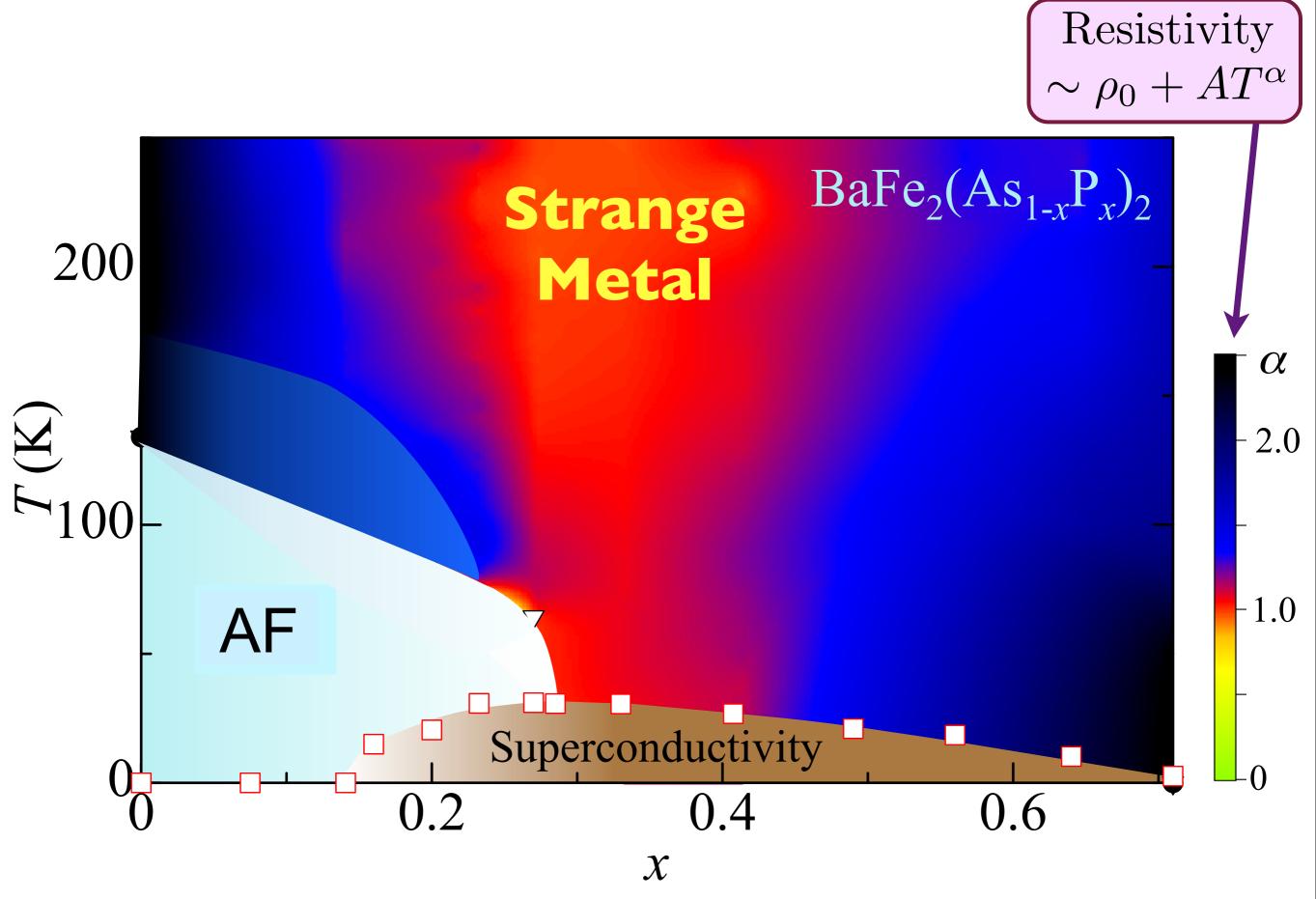
S. Sachdev and J. Ye, *Phys. Rev. Lett.* **69**, 2411 (1992). A. V. Chubukov, S. Sachdev, and J. Ye, *Phys. Rev. B* **49**, 11919 (1994).



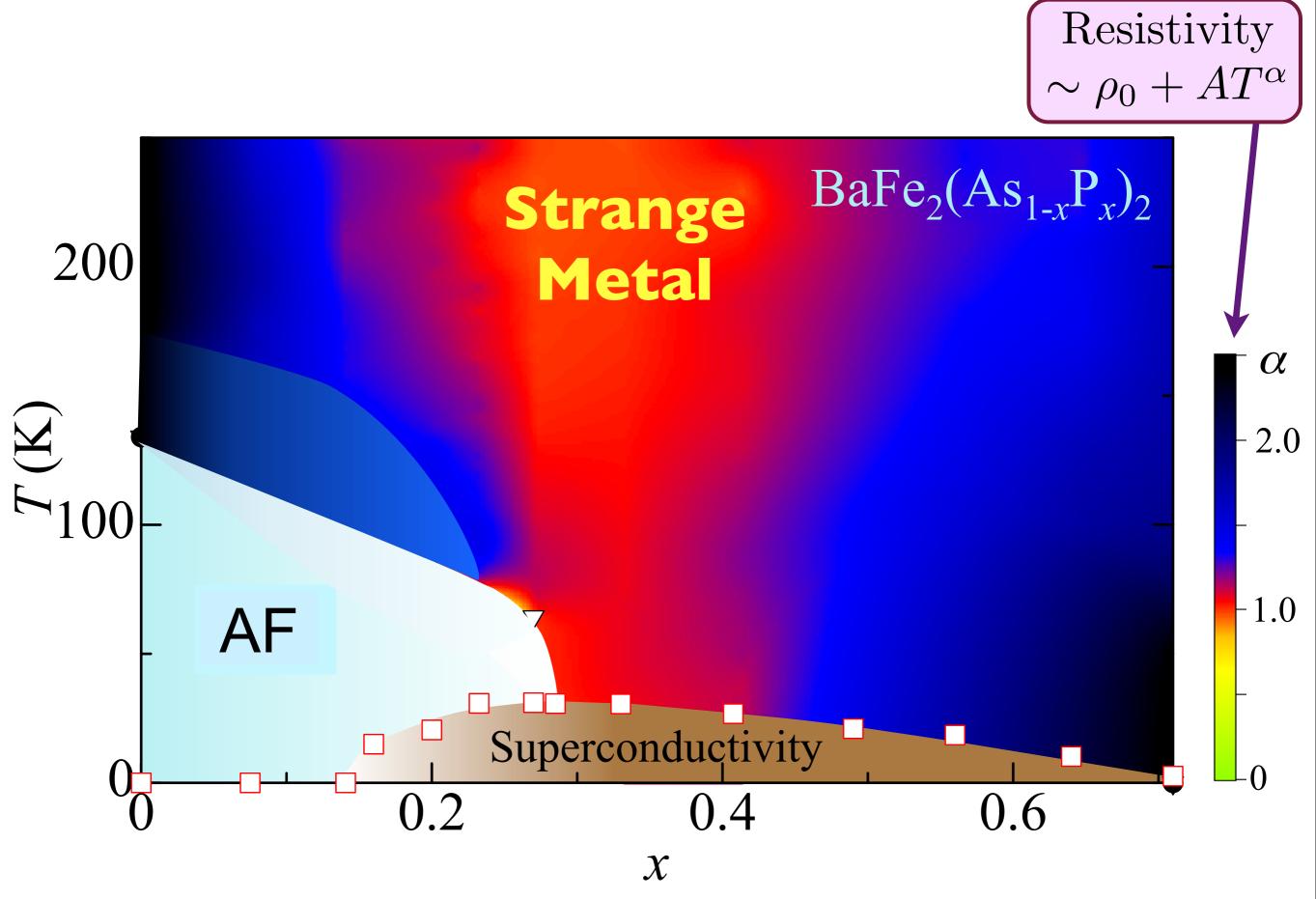




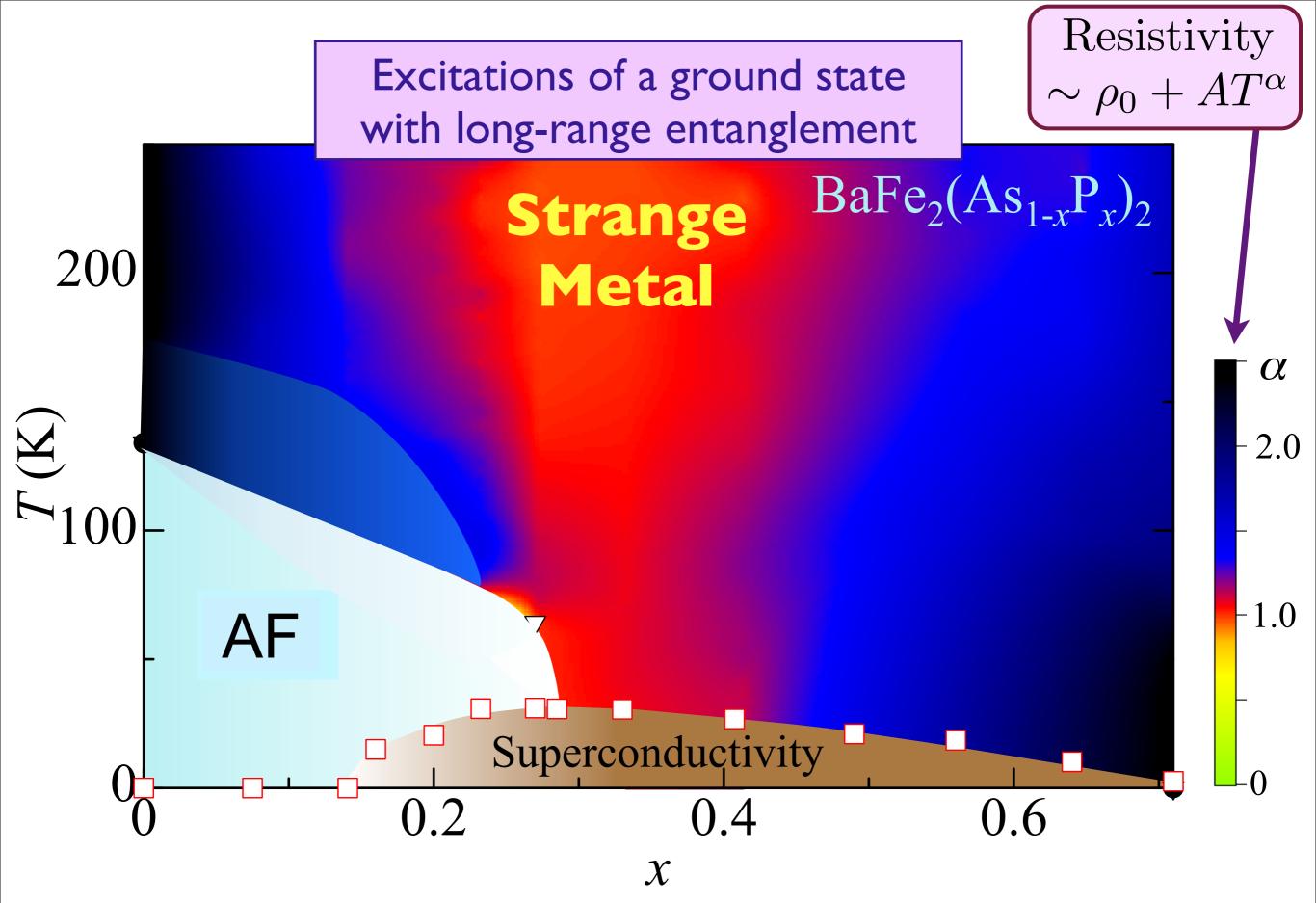




S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)



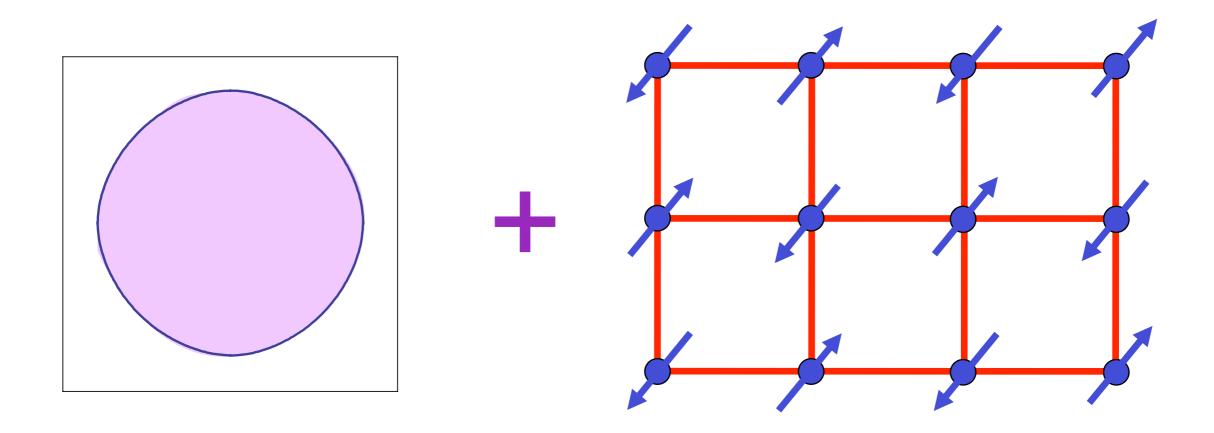
S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)



S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* 81, 184519 (2010)

## Key (difficult) problem:

Describe quantum critical points and phases of systems with Fermi surfaces leading to metals with novel types of long-range entanglement



Describe quantum critical points and phases of metals

Describe quantum critical points and phases of metals

Can we obtain gravitational theories of superconductors and ordinary Sommerfeld-Bloch metals?

Describe quantum critical points and phases of metals

Can we obtain gravitational theories of superconductors and ordinary Sommerfeld-Bloch metals?

#### Yes

T. Nishioka, S. Ryu, and T. Takayanagi, JHEP 1003, 131 (2010) G.T. Horowitz and B. Way, JHEP 1011, 011 (2010) S. Sachdev, Physical Review D 84, 066009 (2011)

Describe quantum critical points and phases of metals

Do the "holographic" gravitational theories also yield metals distinct from ordinary Sommerfeld-Bloch metals?

Describe quantum critical points and phases of metals

Do the "holographic" gravitational theories also yield metals distinct from ordinary Sommerfeld-Bloch metals?

Yes, lots of them, with many "strange" properties!

Describe quantum critical points and phases of metals

How do we discard artifacts, and choose the holographic theories applicable to condensed matter physics?

Describe quantum critical points and phases of metals

How do we discard artifacts, and choose the holographic theories applicable to condensed matter physics?

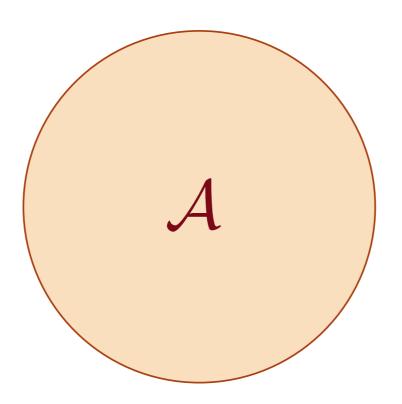
Choose the theories with the proper entropy density

Checks: these theories also have the proper entanglement entropy and Fermi surface size!

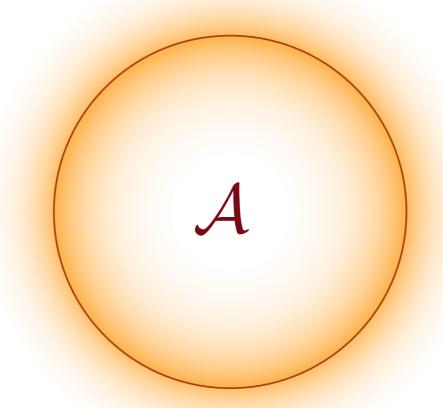
L. Huijse, S. Sachdev, B. Swingle, Physical Review B 85, 035121 (2012)

The simplest example of a "strange metal" is realized by fermions with a Fermi surface coupled to an Abelian or non-Abelian gauge field.

# Fermi surface of an ordinary metal



## Fermions coupled to a gauge field



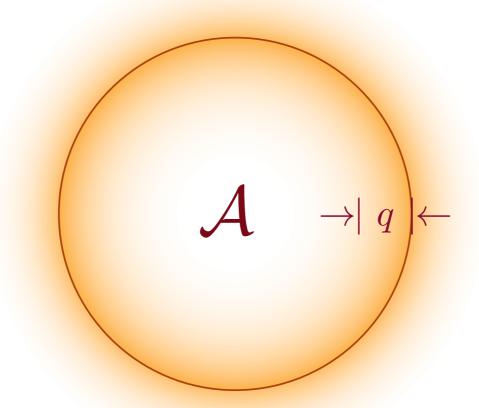
• Area enclosed by the Fermi surface  $\mathcal{A} = \mathcal{Q}$ , the fermion density

S.-S. Lee, Phys. Rev. B **80**, 165102 (2009)

M. A. Metlitski and S. Sachdev, Phys. Rev. B 82, 075127 (2010)

D. F. Mross, J. McGreevy, H. Liu, and T. Senthil, Phys. Rev. B 82, 045121 (2010)

## Fermions coupled to a gauge field

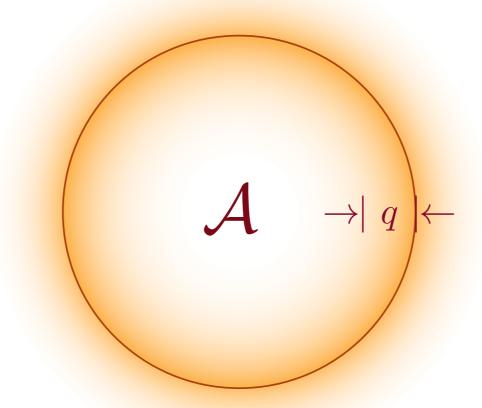


- Area enclosed by the Fermi surface  $\mathcal{A} = \mathcal{Q}$ , the fermion density
- Critical continuum of excitations near the Fermi surface with energy  $\omega \sim |q|^z$ , where  $q = |\mathbf{k}| k_F$  is the distance from the Fermi surface and z is the dynamic critical exponent.

S.-S. Lee, Phys. Rev. B **80**, 165102 (2009) M. A. Metlitski and S. Sachdev, Phys. Rev. B **82**, 075127 (2010)

D. F. Mross, J. McGreevy, H. Liu, and T. Senthil, Phys. Rev. B 82, 045121 (2010)

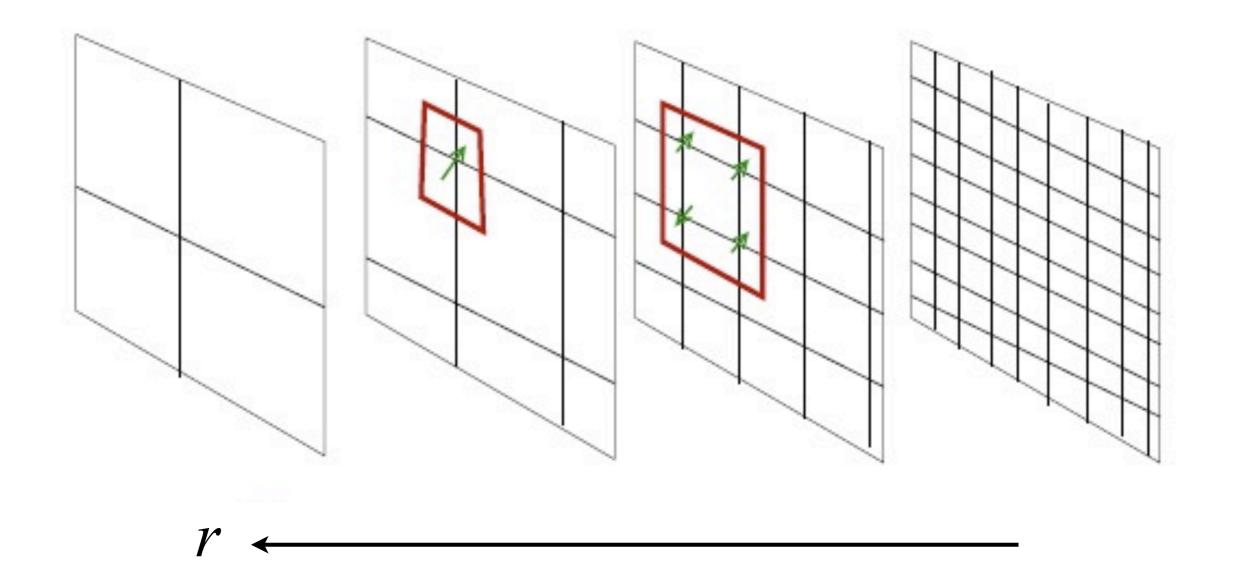
## Fermions coupled to a gauge field



- Area enclosed by the Fermi surface  $\mathcal{A} = \mathcal{Q}$ , the fermion density
- Critical continuum of excitations near the Fermi surface with energy  $\omega \sim |q|^z$ , where  $q = |\mathbf{k}| k_F$  is the distance from the Fermi surface and z is the dynamic critical exponent.
- The phase space density of fermions is effectively one-dimensional, so the entropy density  $S \sim T^{d_{\rm eff}/z}$  with  $d_{\rm eff} = 1$ .

```
S.-S. Lee, Phys. Rev. B 80, 165102 (2009)
M. A. Metlitski and S. Sachdev, Phys. Rev. B 82, 075127 (2010)
```

D. F. Mross, J. McGreevy, H. Liu, and T. Senthil, Phys. Rev. B 82, 045121 (2010)



J. McGreevy, arXiv0909.0518

Consider the following (most) general metric for the holographic theory

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)} dr^{2} + dx_{i}^{2} \right)$$

Consider the following (most) general metric for the holographic theory

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)} dr^{2} + dx_{i}^{2} \right)$$

This metric transforms under rescaling as

$$x_i \rightarrow \zeta x_i$$
 $t \rightarrow \zeta^z t$ 
 $ds \rightarrow \zeta^{\theta/d} ds.$ 

This identifies z as the dynamic critical exponent (z=1 for "relativistic" quantum critical points).

Consider the following (most) general metric for the holographic theory

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)} dr^{2} + dx_{i}^{2} \right)$$

This metric transforms under rescaling as

$$x_i \rightarrow \zeta x_i$$
 $t \rightarrow \zeta^z t$ 
 $ds \rightarrow \zeta^{\theta/d} ds.$ 

This identifies z as the dynamic critical exponent (z=1 for "relativistic" quantum critical points).

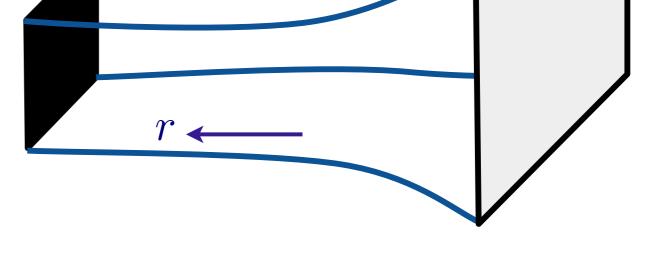
What is  $\theta$ ? ( $\theta = 0$  for "relativistic" quantum critical points).

At T > 0, there is a "black-brane" at  $r = r_h$ .

The Beckenstein-Hawking entropy of the black-brane is the thermal entropy of the quantum system r = 0.

The entropy density, S, is proportional to the

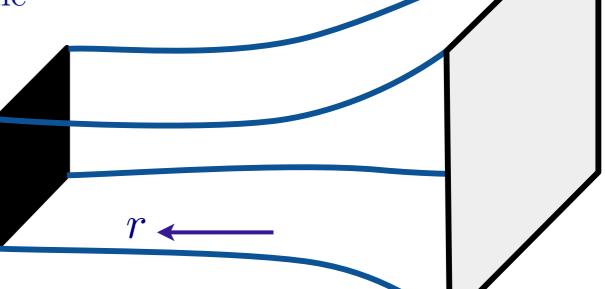
"area" of the horizon, and so  $S \sim r_h^{-d}$ 



At T > 0, there is a "black-brane" at  $r = r_h$ .

The Beckenstein-Hawking entropy of the black-brane is the thermal entropy of the quantum system r=0.

The entropy density, S, is proportional to the "area" of the horizon, and so  $S \sim r_h^{-d}$ 



Under rescaling  $r \to \zeta^{(d-\theta)/d} r$ , and the temperature  $T \sim t^{-1}$ , and so

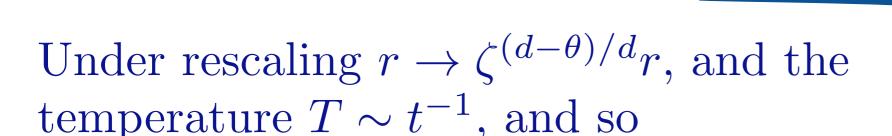
$$S \sim T^{(d-\theta)/z} = T^{d_{\rm eff}/z}$$

where  $\theta = d - d_{\text{eff}}$  measures "dimension deficit" in the phase space of low energy degrees of a freedom.

At T > 0, there is a "black-brane" at  $r = r_h$ .

The Beckenstein-Hawking entropy of the black-brane is the thermal entropy of the quantum system r = 0.

The entropy density, S, is proportional to the "area" of the horizon, and so  $S \sim r_h^{-d}$ 



$$S \sim T^{(d-\theta)/z} = T^{d_{\rm eff}/z}$$

where  $\theta = d - d_{\text{eff}}$  measures "dimension deficit" in the phase space of low energy degrees of a freedom. For a strange metal should choose  $\theta = d - 1$ .

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)} dr^{2} + dx_{i}^{2} \right)$$

$$\theta = d - 1$$

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)}dr^{2} + dx_{i}^{2} \right)$$

$$\theta = d - 1$$

• The entanglement entropy exhibits logarithmic violation of the area law, expected for systems with Fermi surfaces, only for this value of  $\theta$ !

N. Ogawa, T. Takayanagi, and T. Ugajin, arXiv:1111.1023 L. Huijse, S. Sachdev, B. Swingle, Physical Review B **85**, 035121 (2012)

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)}dr^{2} + dx_{i}^{2} \right)$$

$$\theta = d - 1$$

- The entanglement entropy exhibits logarithmic violation of the area law, expected for systems with Fermi surfaces, only for this value of  $\theta$ !
- The co-efficient of the logarithmic term is consistent with the Fermi surface size expected from  $\mathcal{A} = \mathcal{Q}$ .

L. Huijse, S. Sachdev, B. Swingle, Physical Review B 85, 035121 (2012)

$$ds^{2} = \frac{1}{r^{2}} \left( -\frac{dt^{2}}{r^{2d(z-1)/(d-\theta)}} + r^{2\theta/(d-\theta)} dr^{2} + dx_{i}^{2} \right)$$

$$\theta = d - 1$$

- The entanglement entropy exhibits logarithmic violation of the area law, expected for systems with Fermi surfaces, only for this value of  $\theta$ !
- The co-efficient of the logarithmic term is consistent with the Fermi surface size expected from  $\mathcal{A} = \mathcal{Q}$ .
- Many other features of the holographic theory are consistent with a boundary theory which has "hidden" Fermi surfaces of gauge-charged fermions.

L. Huijse, S. Sachdev, B. Swingle, Physical Review B 85, 035121 (2012)

Phases of matter with long-range quantum entanglement are prominent in numerous modern materials.

Simplest examples of long-range entanglement are at quantum-critical points of insulating antiferromagnets

More complex examples in metallic states are experimentally ubiquitous, but pose difficult strong-coupling problems to conventional methods of field theory

String theory and gravity in emergent dimensions offer a remarkable new approach to describing states with long-range quantum entanglement.

String theory and gravity in emergent dimensions offer a remarkable new approach to describing states with long-range quantum entanglement.

Much recent progress offers hope of a holographic description of "strange metals"