

Quantum phase transitions and Fermi surface reconstruction

Talk online: sachdev.physics.harvard.edu





Max Metlitski



Matthias Punk



Erez Berg

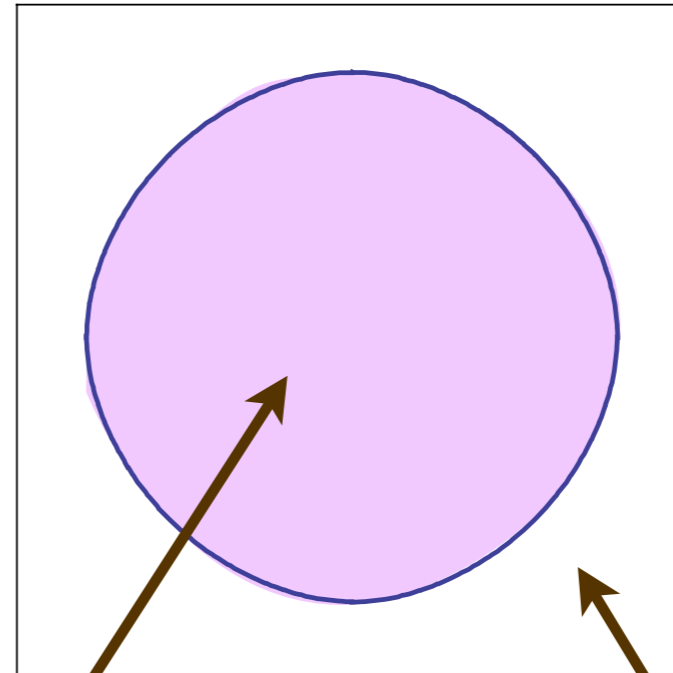


1. Fate of the Fermi surface:
reconstruction or not ? Experimental
motivations from cuprates and pnictides
2. Conventional theory and its breakdown
in two spatial dimensions
3. Fermi surface reconstruction: onset
of unconventional superconductivity
4. Fermi surface reconstruction *without*
symmetry breaking: metals with
“topological” order
5. The nematic transition: field theory of
antipodal Fermi surface points

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Fermi surface

Metal with “large”
Fermi surface

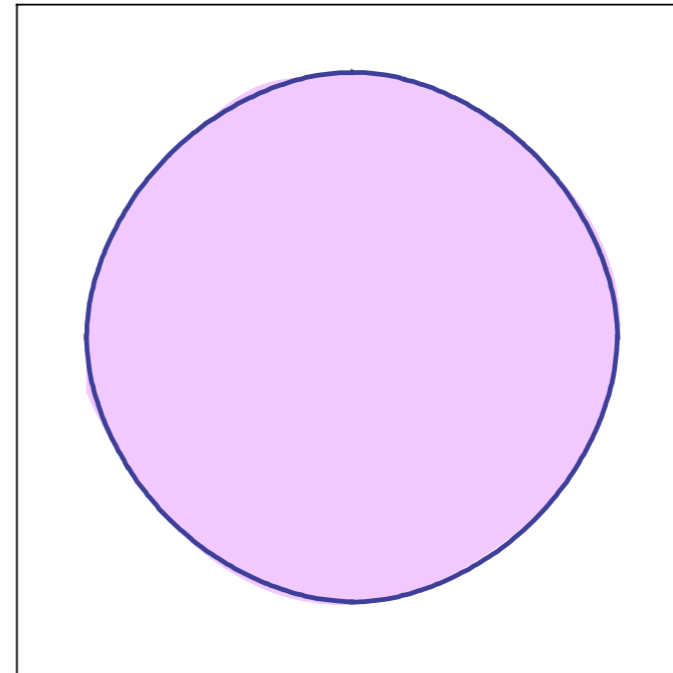


Momenta with
electronic
states empty

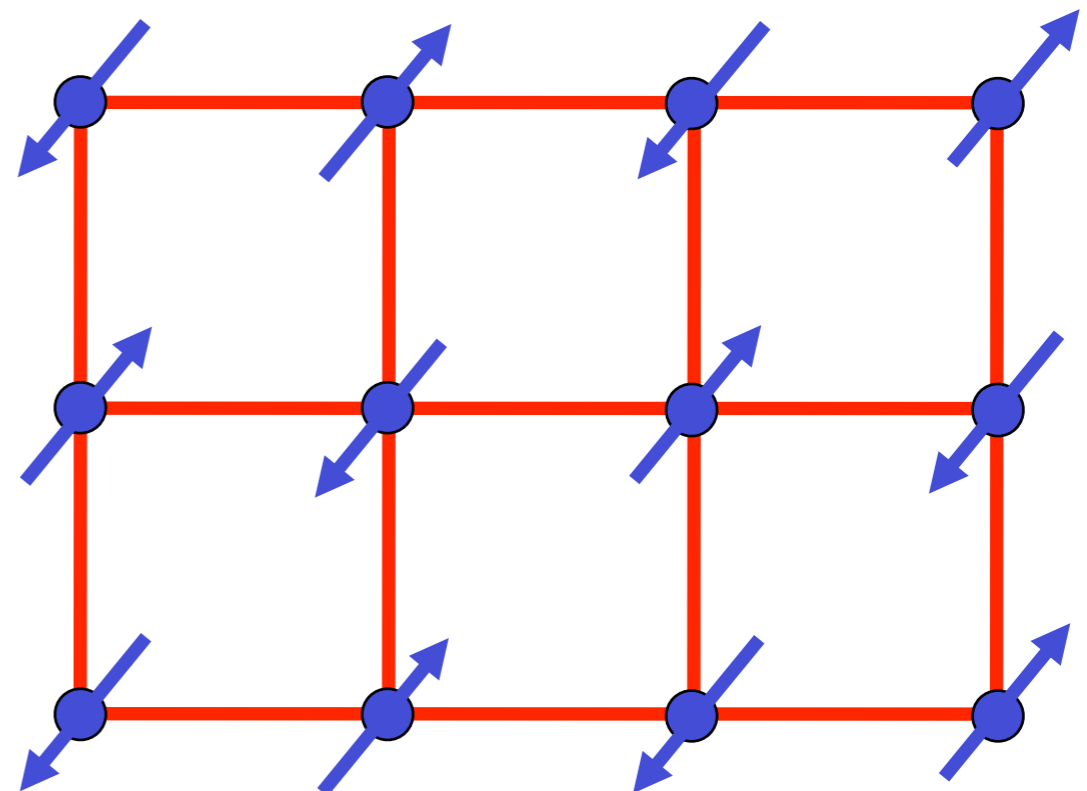
Momenta with
electronic
states
occupied

Fermi surface+antiferromagnetism

Metal with “large”
Fermi surface



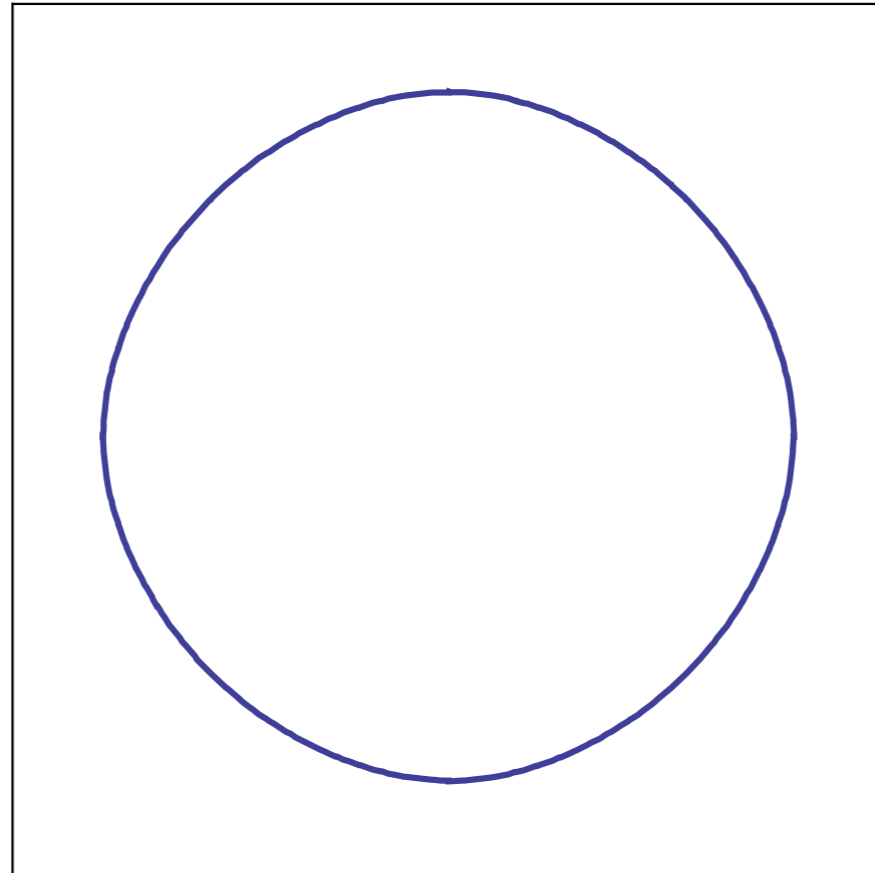
+



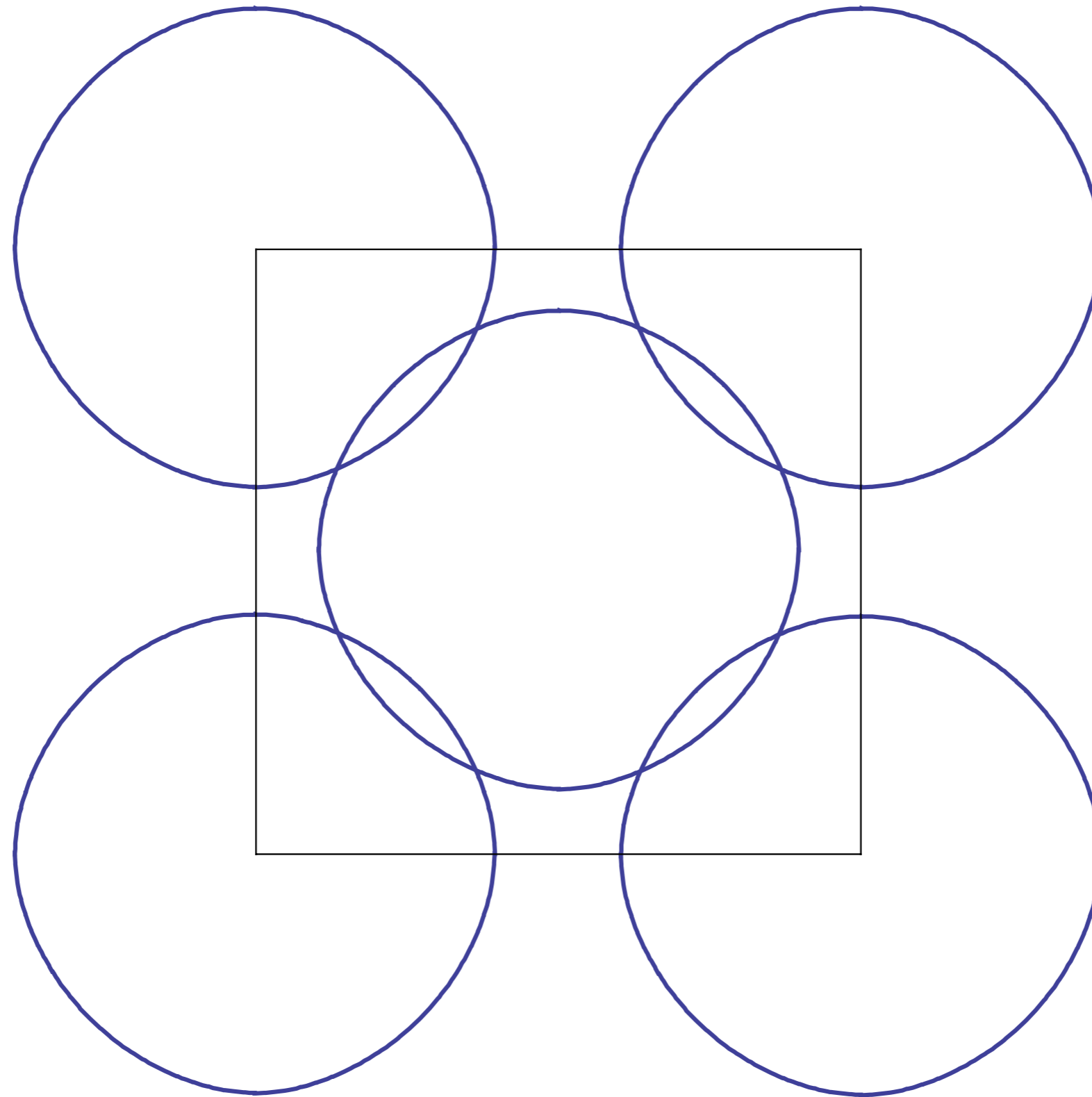
The electron spin polarization obeys

$$\langle \vec{S}(\mathbf{r}, \tau) \rangle = \vec{\varphi}(\mathbf{r}, \tau) e^{i\mathbf{K} \cdot \mathbf{r}}$$

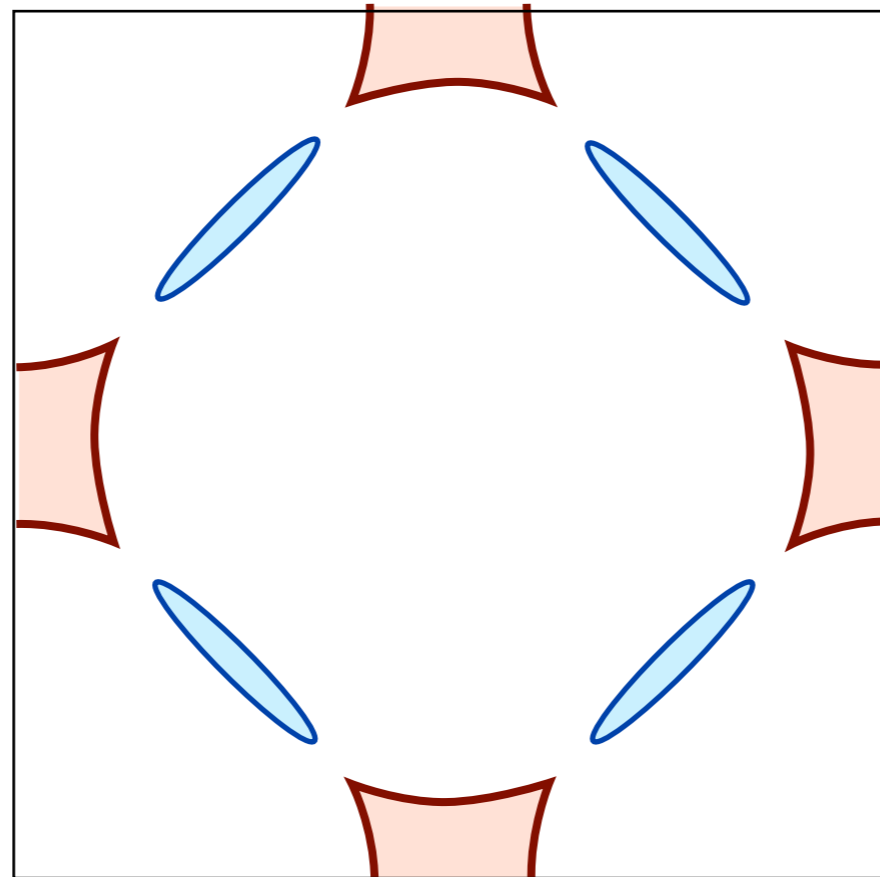
where \mathbf{K} is the ordering wavevector.



Metal with “large” Fermi surface

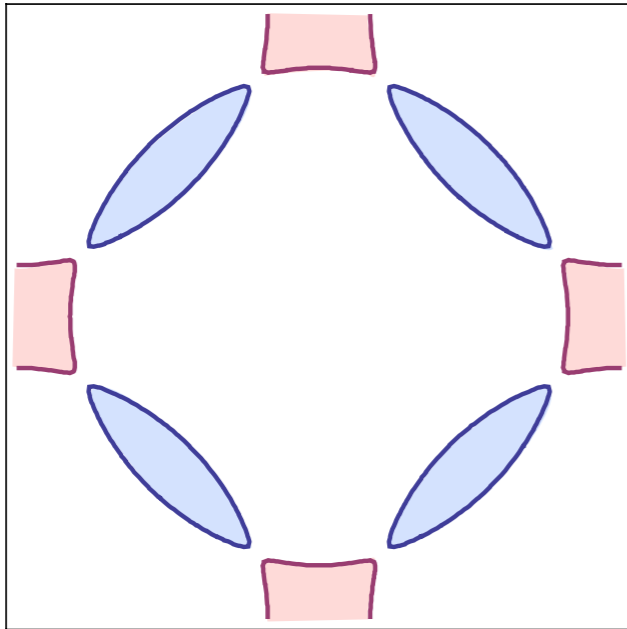


Fermi surfaces translated by $\mathbf{K} = (\pi, \pi)$.



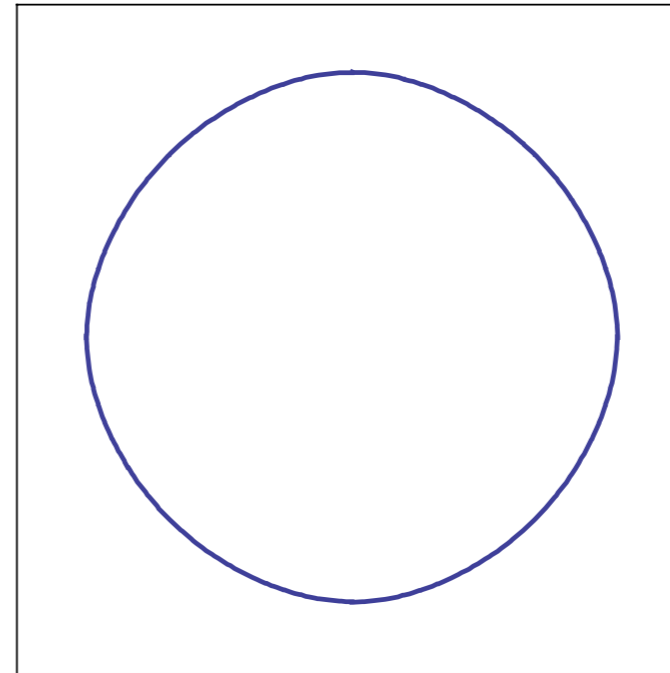
Fermi surface reconstruction
into electron and hole pockets in
antiferromagnetic phase with $\langle \vec{\varphi} \rangle \neq 0$

Quantum phase transition with Fermi surface reconstruction



$$\langle \vec{\varphi} \rangle \neq 0$$

Metal with electron
and hole pockets



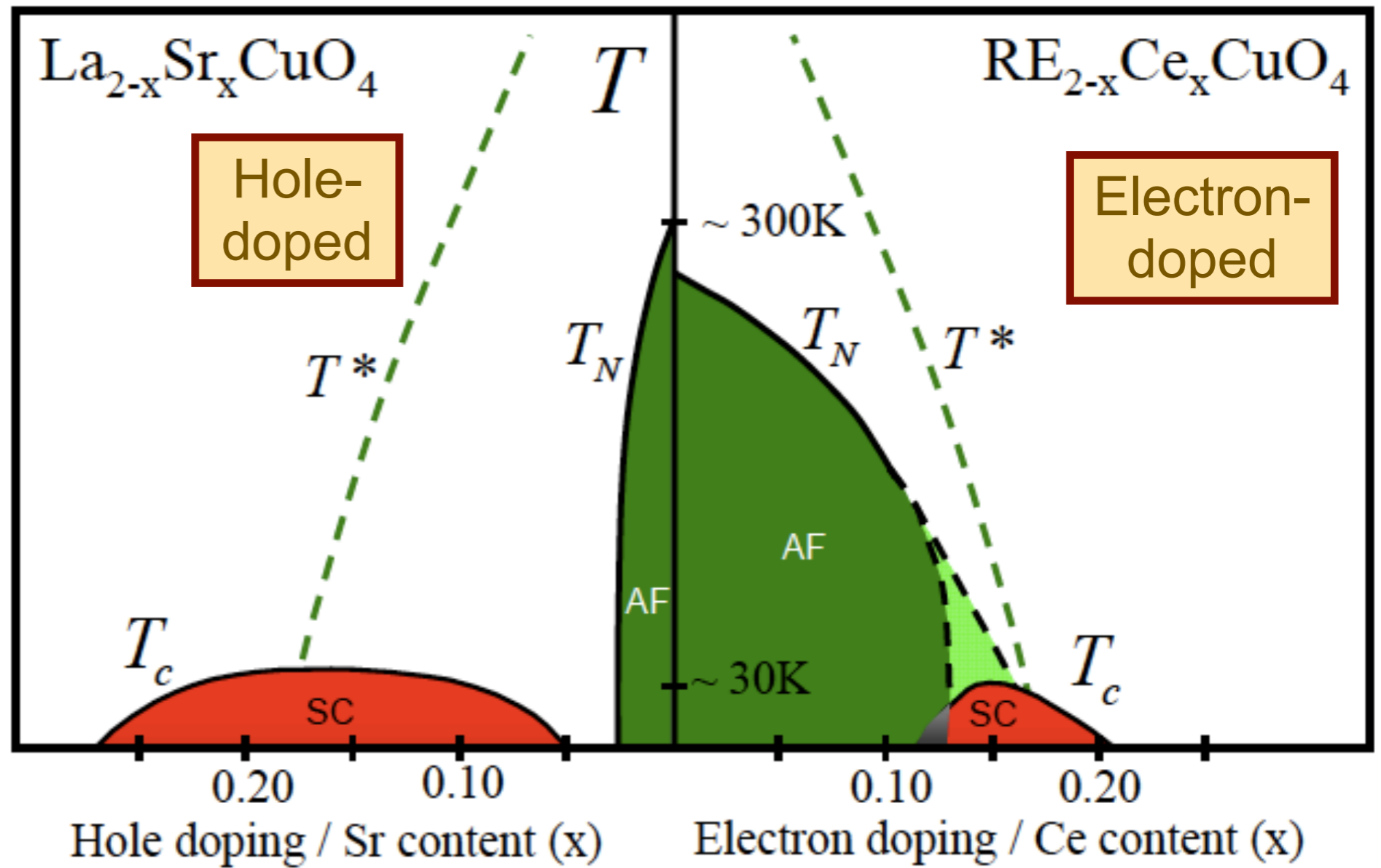
$$\langle \vec{\varphi} \rangle = 0$$

Metal with “large”
Fermi surface

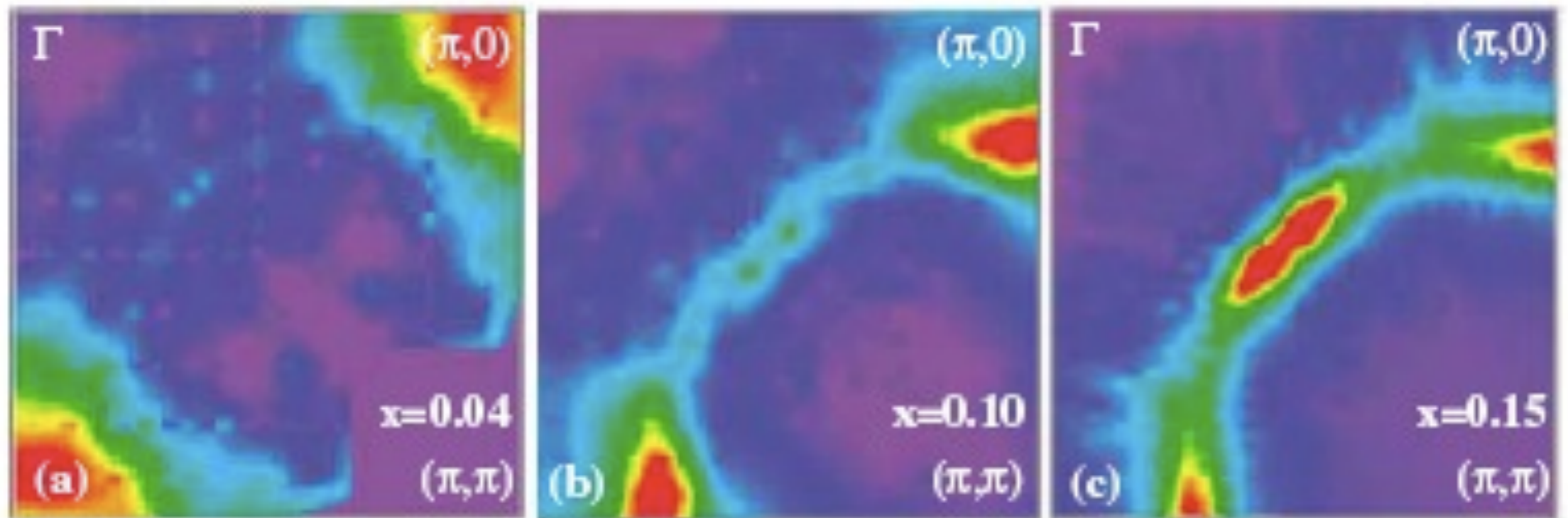
← Increasing interaction

S. Sachdev, A. V. Chubukov, and A. Sokol, *Phys. Rev. B* **51**, 14874 (1995).
A. V. Chubukov and D. K. Morr, *Physics Reports* **288**, 355 (1997).

Electron-doped cuprate superconductors



Photoemission in $\text{Nd}_{2-x}\text{Ce}_x\text{CuO}_4$

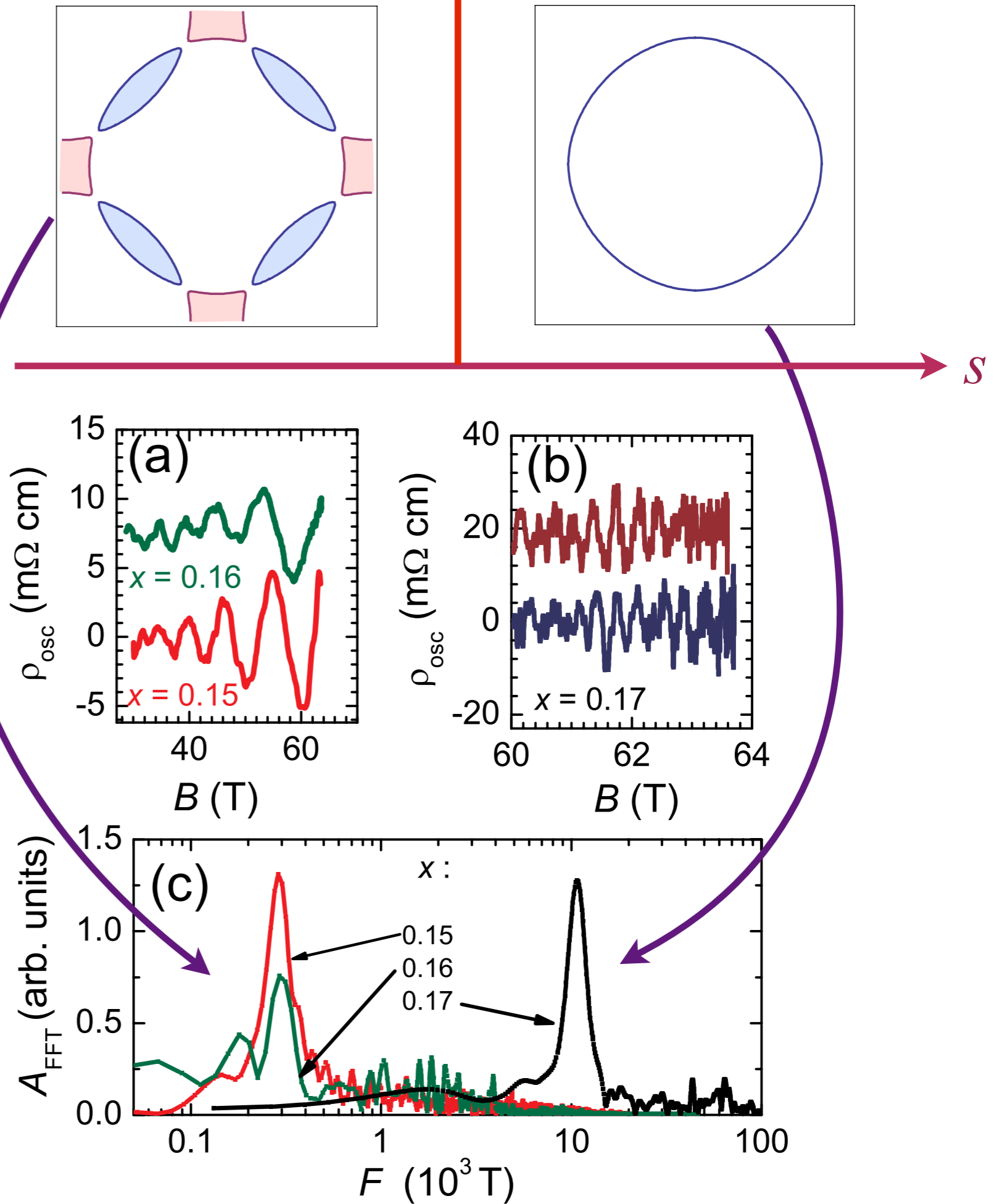


N. P. Armitage *et al.*, Phys. Rev. Lett. **88**, 257001 (2002).

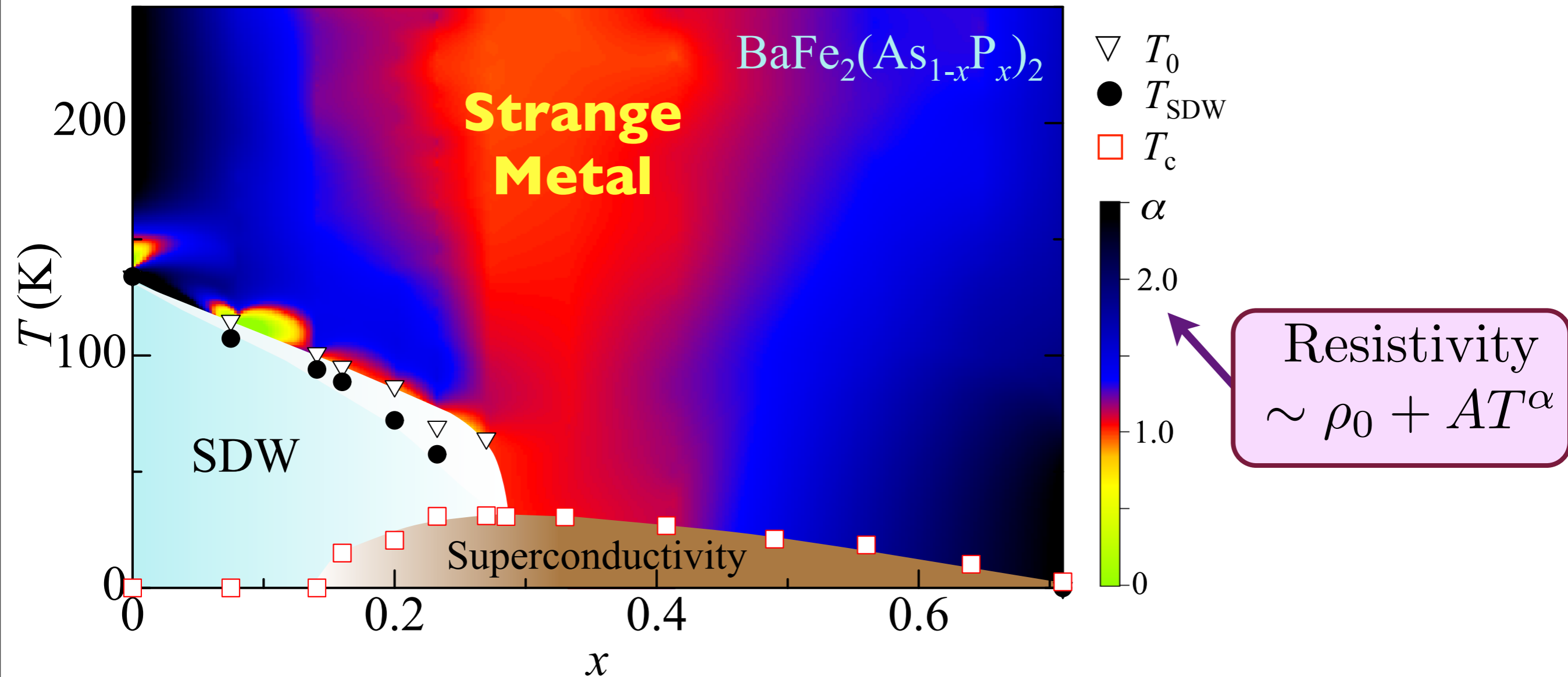
Quantum oscillations



T. Helm, M.V. Kartsovnik,
M. Bartkowiak, N. Bittner,
M. Lambacher, A. Erb, J. Wosnitza,
and R. Gross,
Phys. Rev. Lett. **103**, 157002 (2009).



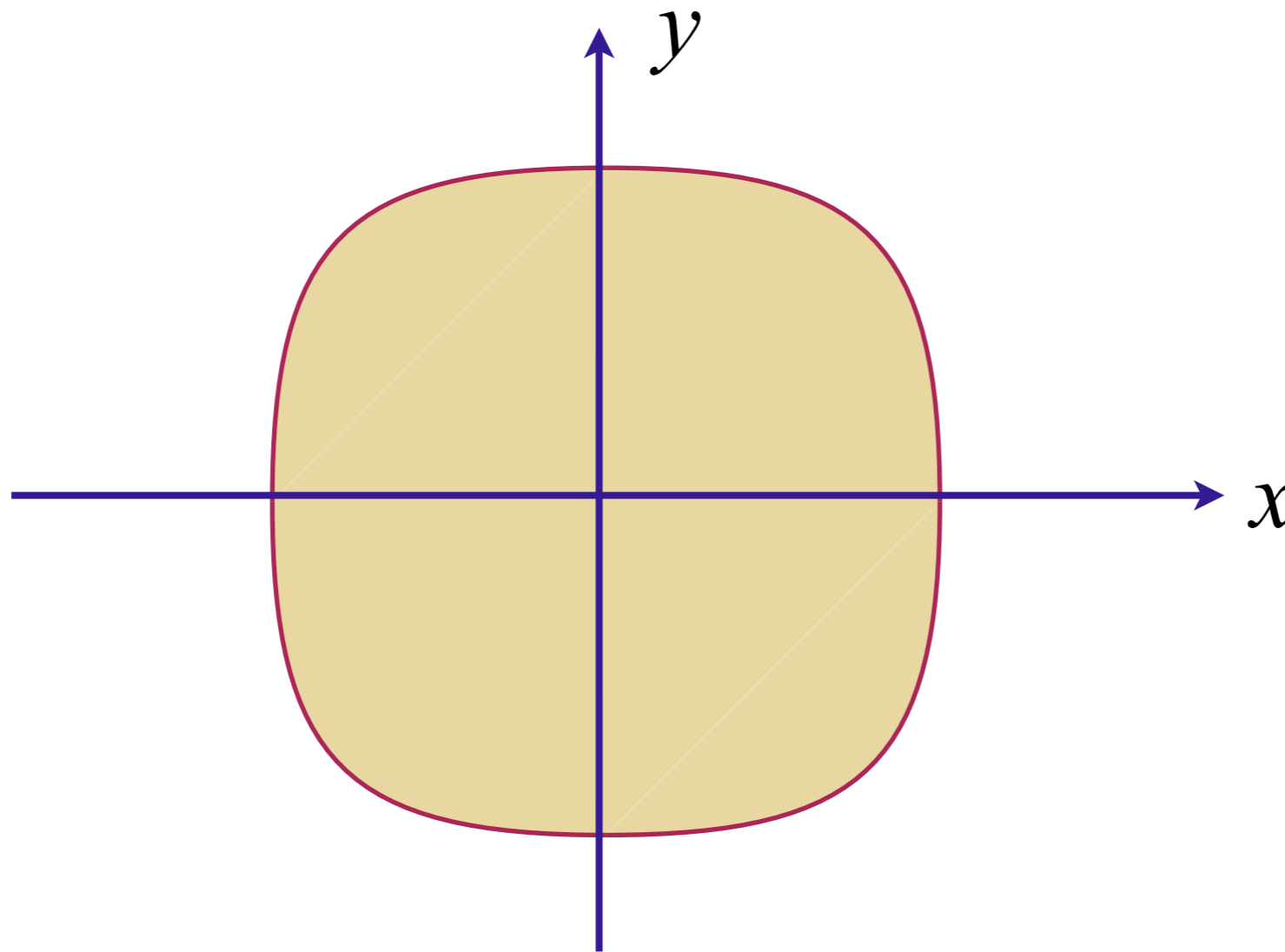
Temperature-doping phase diagram of the iron pnictides:



S. Kasahara, T. Shibauchi, K. Hashimoto, K. Ikada, S. Tonegawa, R. Okazaki, H. Shishido, H. Ikeda, H. Takeya, K. Hirata, T. Terashima, and Y. Matsuda, *Physical Review B* **81**, 184519 (2010)

Quantum phase transition with Ising-nematic order

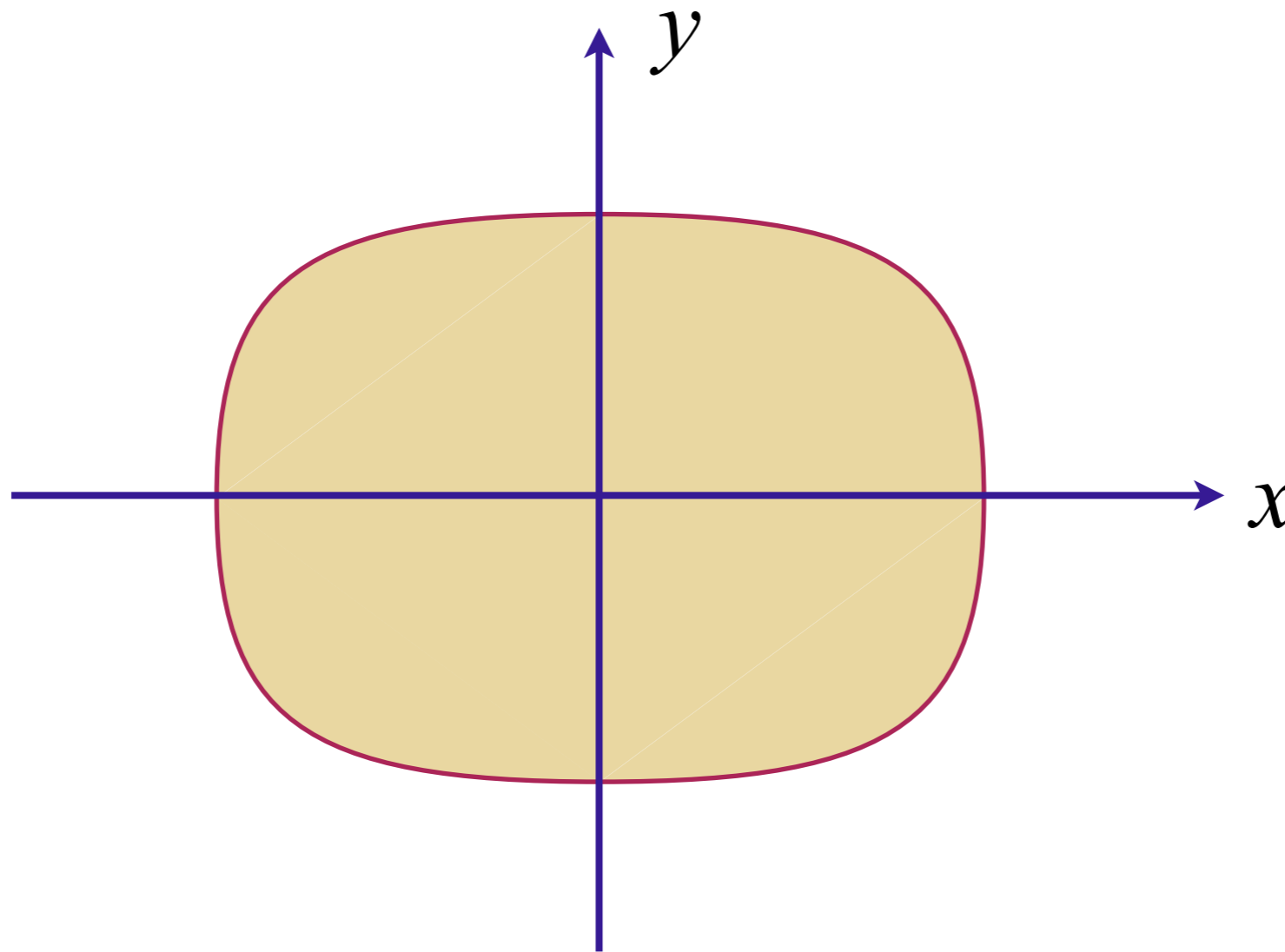
No Fermi surface reconstruction



Fermi surface with full square lattice symmetry

Quantum phase transition with Ising-nematic order

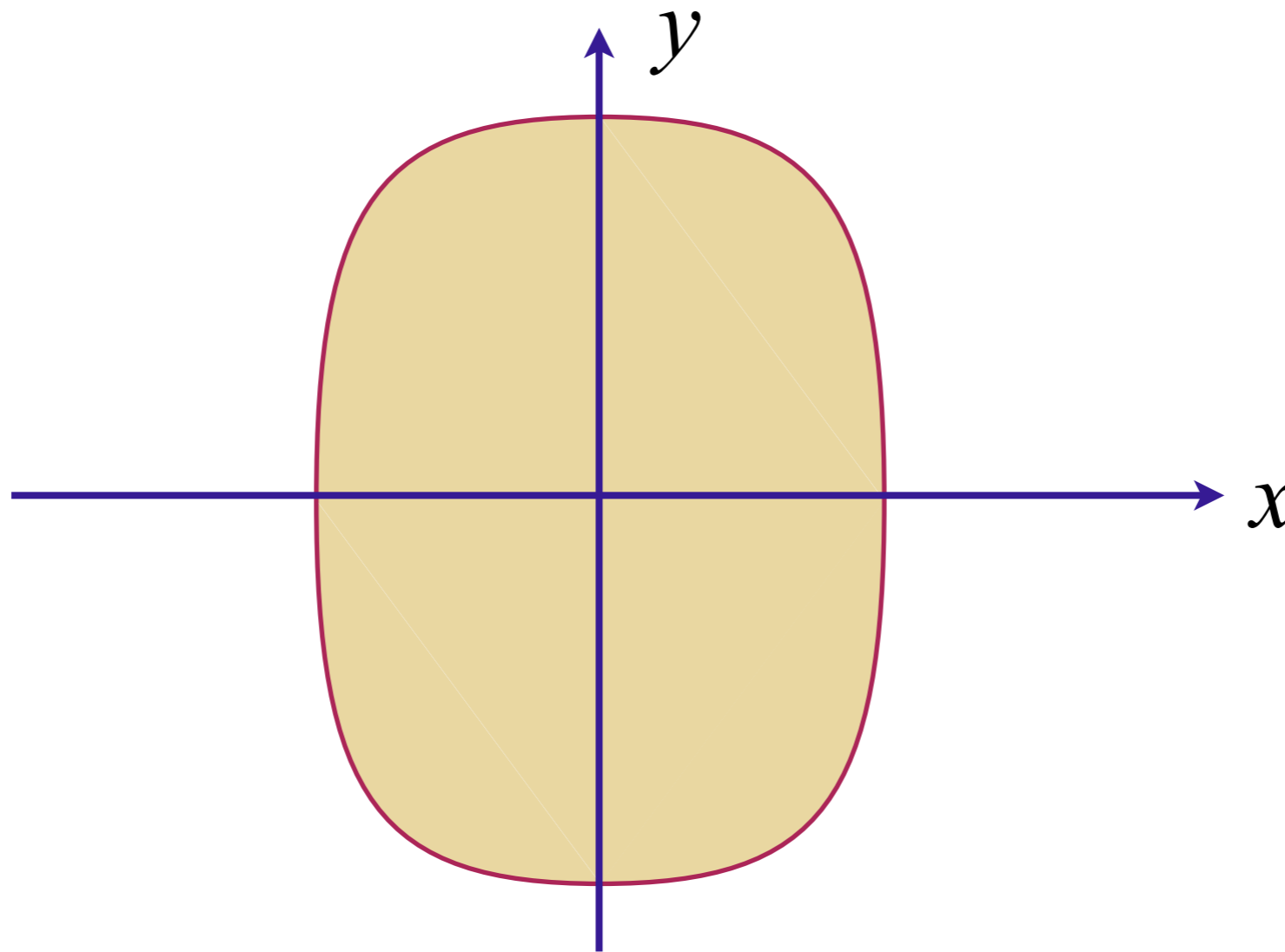
No Fermi surface reconstruction



Spontaneous elongation along x direction:

Quantum phase transition with Ising-nematic order

No Fermi surface reconstruction



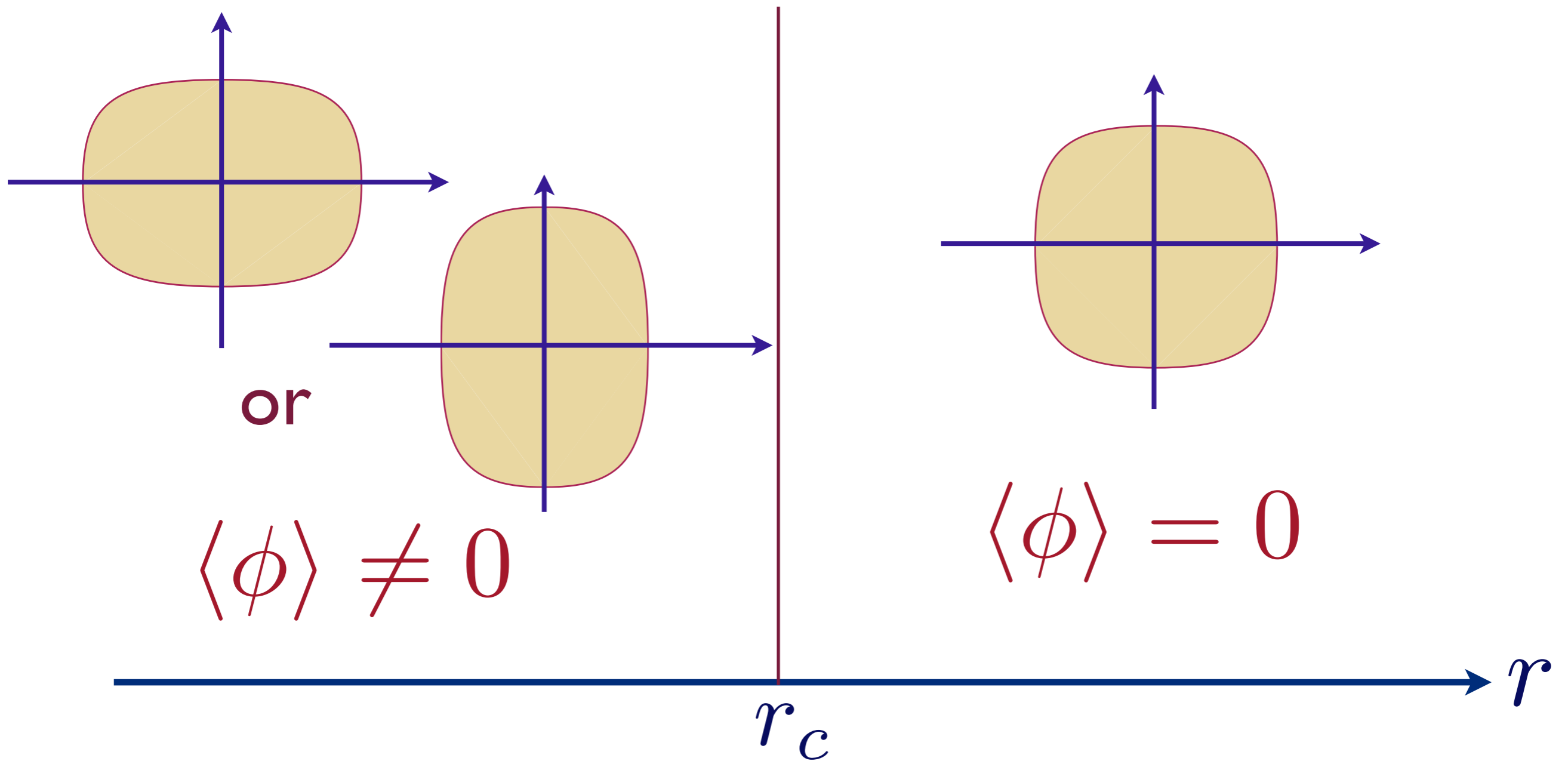
Spontaneous elongation along y direction:

Ising-nematic order parameter

$$\phi \sim \int d^2 k (\cos k_x - \cos k_y) c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma}$$

Measures spontaneous breaking of square lattice point-group symmetry of underlying Hamiltonian

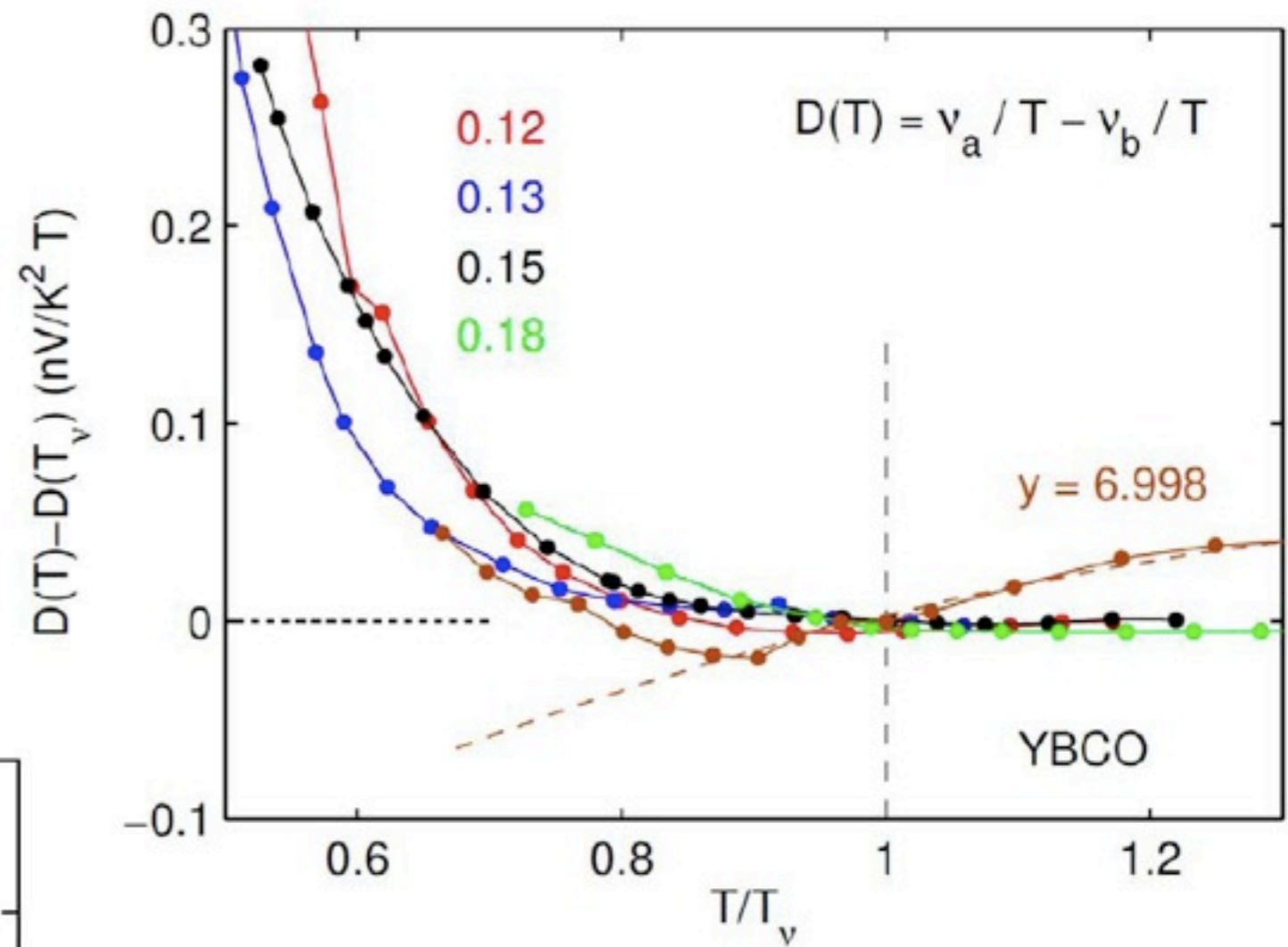
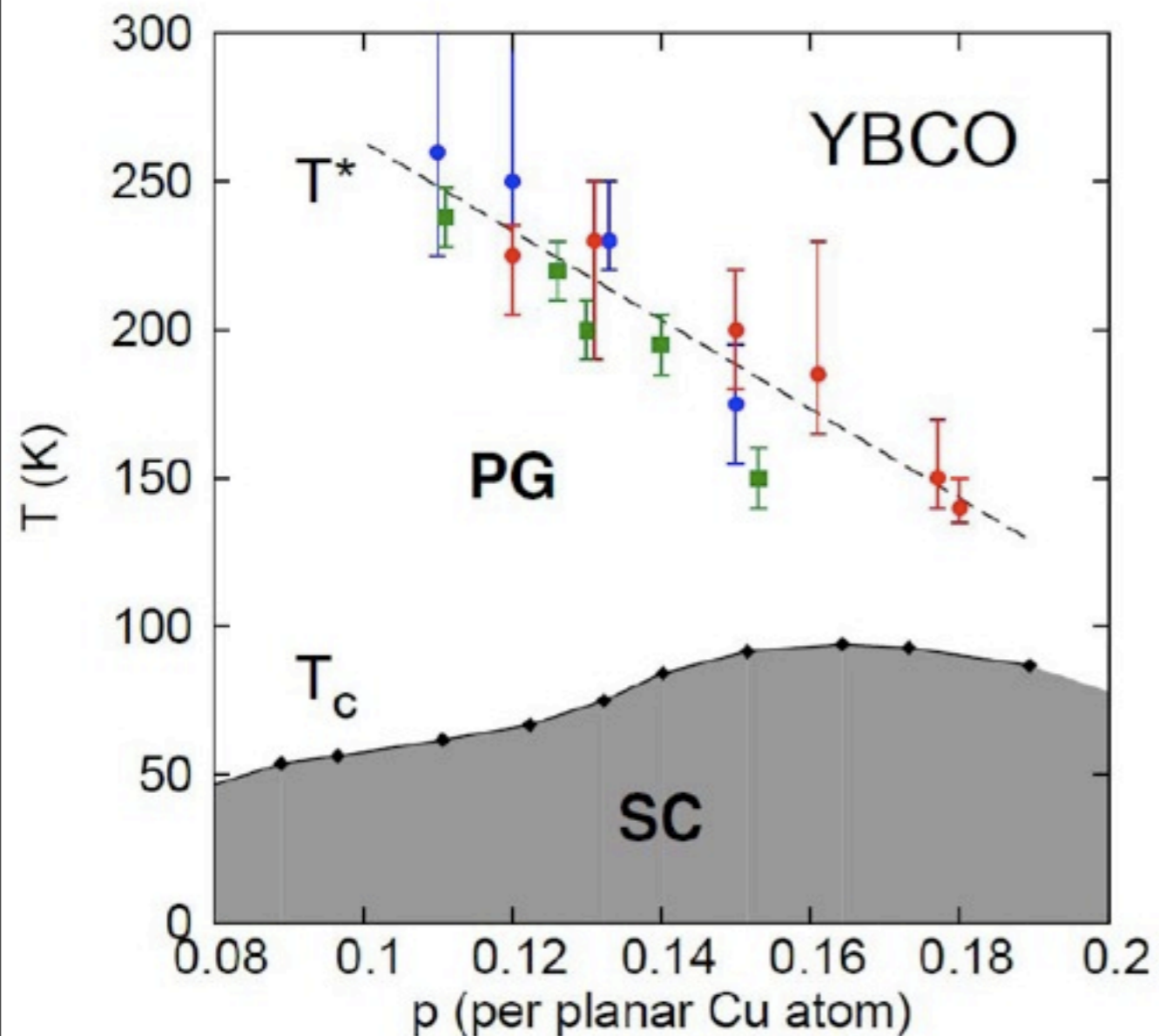
Quantum criticality of Ising-nematic ordering



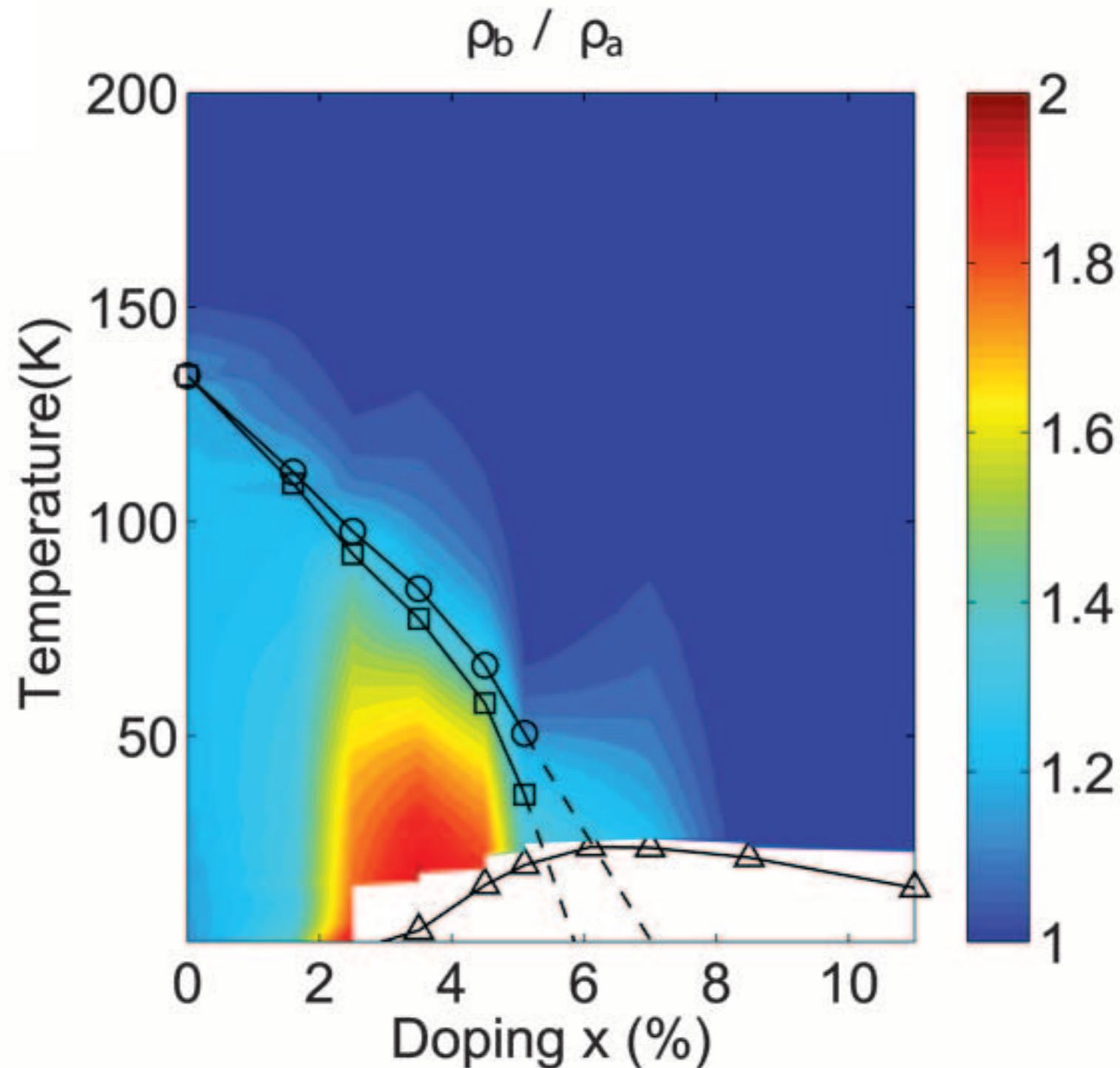
Pomeranchuk instability as a function of coupling r

Broken rotational symmetry in the pseudogap phase of a high- T_c superconductor

R. Daou, J. Chang, David LeBoeuf, Olivier Cyr-Choiniere, Francis Laliberte, Nicolas Doiron-Leyraud, B. J. Ramshaw, Ruixing Liang, D.A. Bonn, W. N. Hardy, and Louis Taillefer
Nature, **463**, 519 (2010).



In-plane resistivity anisotropy in $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$



Jiun-Haw Chu, J. G. Analytis, K. De Greve, P. L. McMahon, Z. Islam, Y. Yamamoto, and I. R. Fisher, *Science* **329**, 824 (2010)

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Hertz-Moriya-Millis theory

- Integrate out Fermi surface quasiparticles and obtain an effective theory for the order parameter $\vec{\varphi}$ alone.

Hertz-Moriya-Millis theory

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- This is dangerous, and will lead to non-local in the $\vec{\varphi}$ theory. Hertz focused on only the simplest such non-local term.

Hertz-Moriya-Millis theory

- Integrate out Fermi surface quasiparticles and obtain an effective theory for the order parameter $\vec{\varphi}$ alone.
- This is dangerous, and will lead to non-local in the $\vec{\varphi}$ theory. Hertz focused on only the simplest such non-local term.
- However, there are an infinite number of non-local terms at higher order, and these lead to a breakdown of the Hertz theory in two spatial dimensions.

Ar. Abanov and A.V. Chubukov, *Phys. Rev. Lett.* **93**, 255702 (2004).

- In $d = 2$, we *must* work in local theories which keeps both the order parameter and the Fermi surface quasiparticles “alive”.

Sung-Sik Lee, *Phys. Rev. B* **80**, 165102 (2009)

M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

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- The theories can be organized in a $1/N$ expansion, where N is the number of fermion “flavors”.

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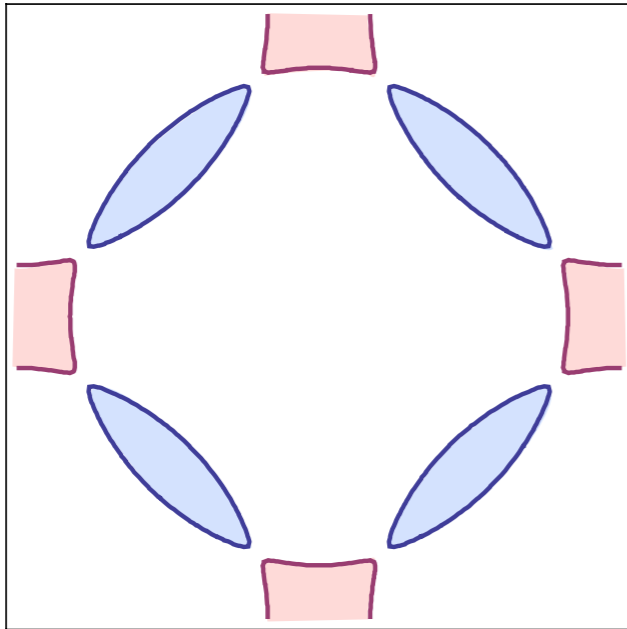
- In $d = 2$, we *must* work in local theories which keeps both the order parameter and the Fermi surface quasiparticles “alive”.
- The theories can be organized in a $1/N$ expansion, where N is the number of fermion “flavors”.
- At subleading order, resummation of all “planar” graphics is required (at least): this theory is even more complicated than QCD.

Sung-Sik Lee, *Phys. Rev. B* **80**, 165102 (2009)

M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

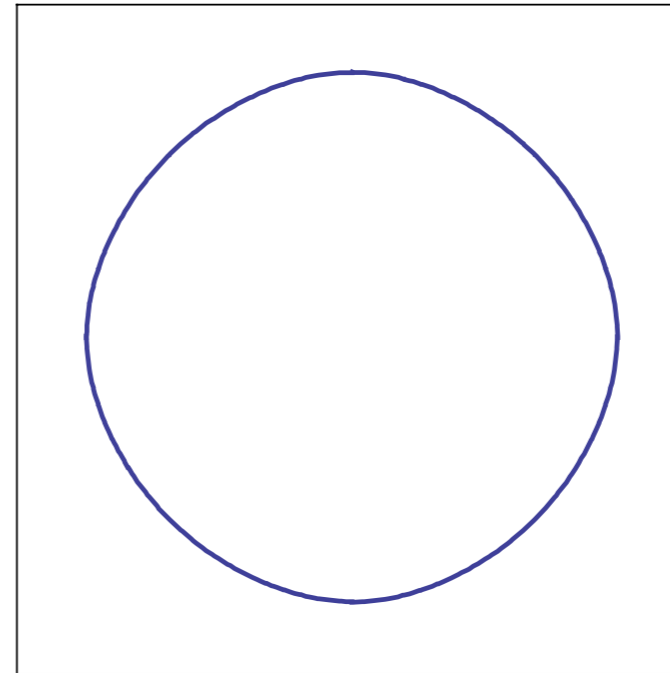
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Quantum phase transition with Fermi surface reconstruction



$$\langle \vec{\varphi} \rangle \neq 0$$

Metal with electron
and hole pockets



$$\langle \vec{\varphi} \rangle = 0$$

Metal with “large”
Fermi surface

← Increasing interaction

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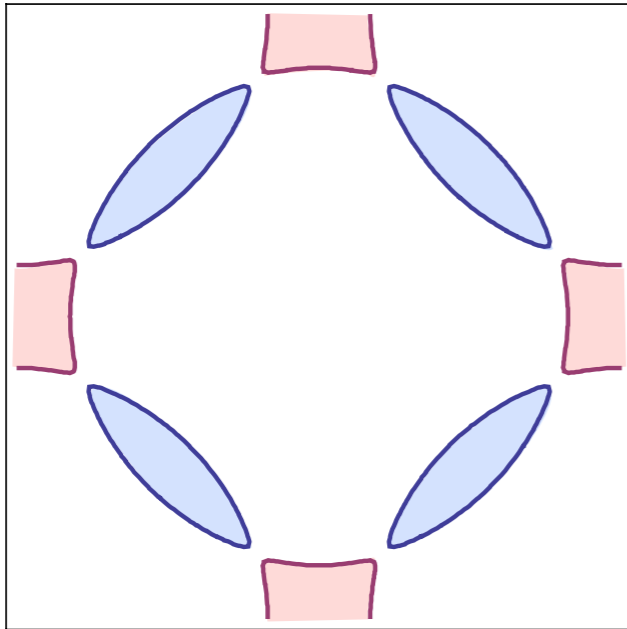
- Steglich: Evidence for two types of quantum critical points between the SDW metal and the heavy fermion metal (both Fermi liquid phases) in $d = 3$: one described by SDW theory, and the other by Kondo breakdown in Kondo lattice model (Q Si, P. Coleman)

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- Our theory: Because the phases on either side are qualitatively identical, there is only one theory, whether one uses the SDW or Kondo lattice models. In $d = 2$, this theory is strongly coupled. In $d = 3$, we can show that the weak coupling (as in Hertz-Millis-Moriya) theory is stable; however there may also be another fixed point at strong coupling.

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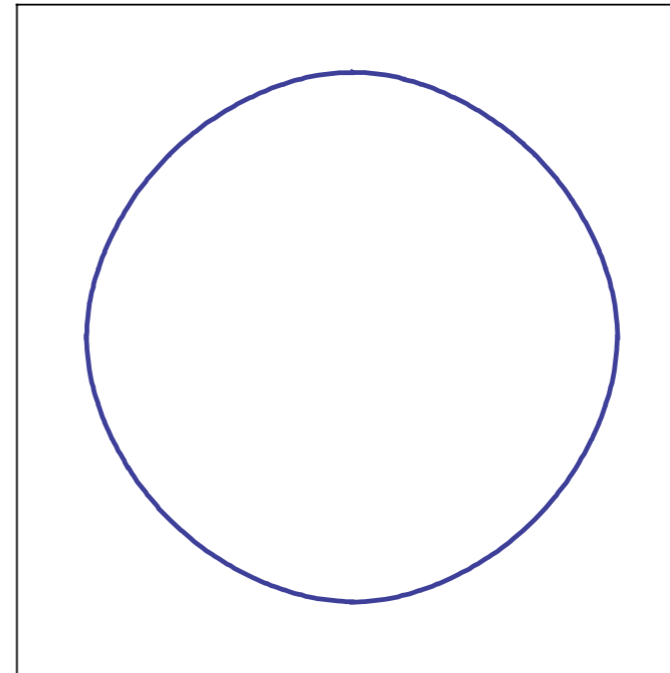
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Metal with electron
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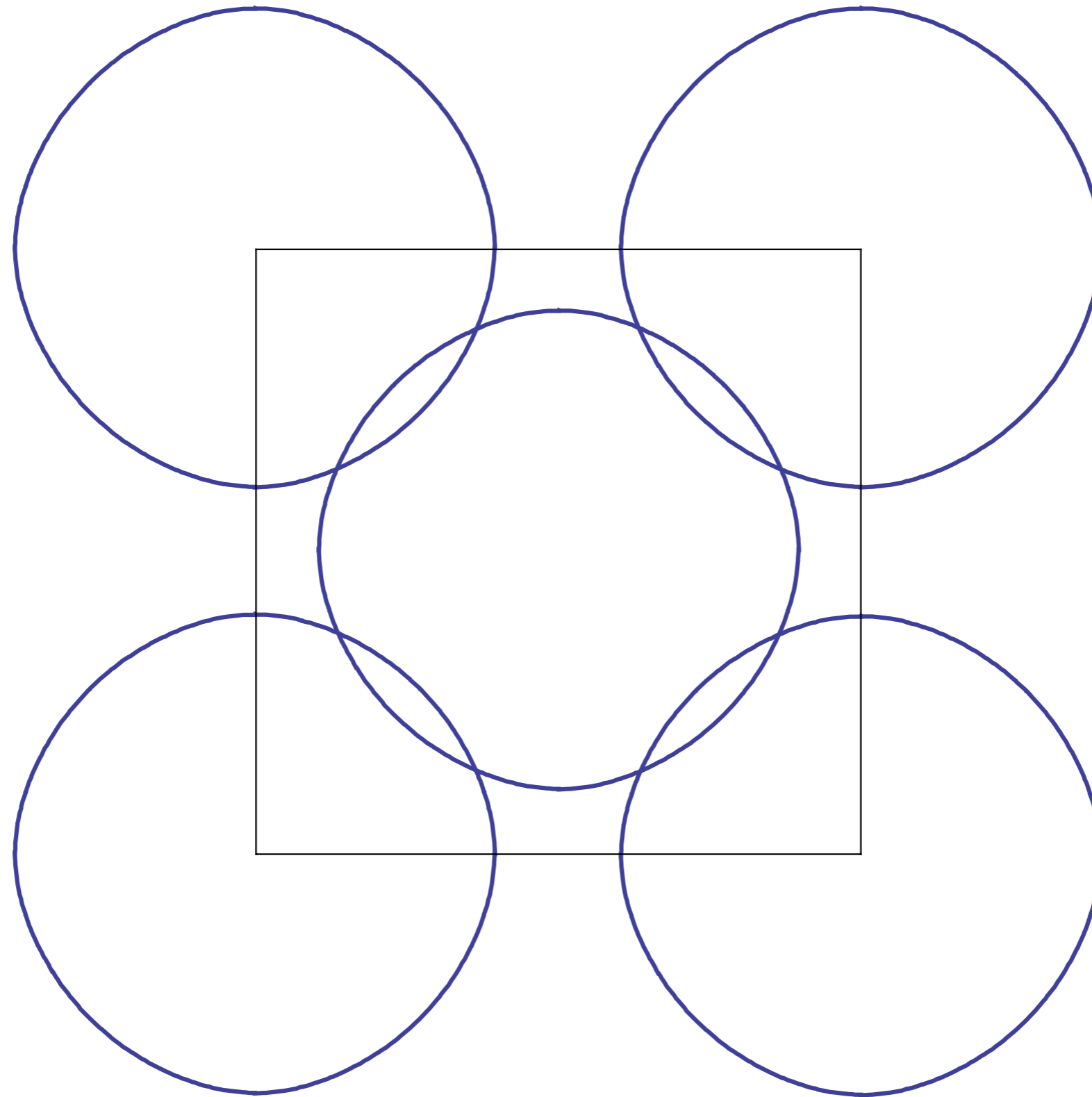


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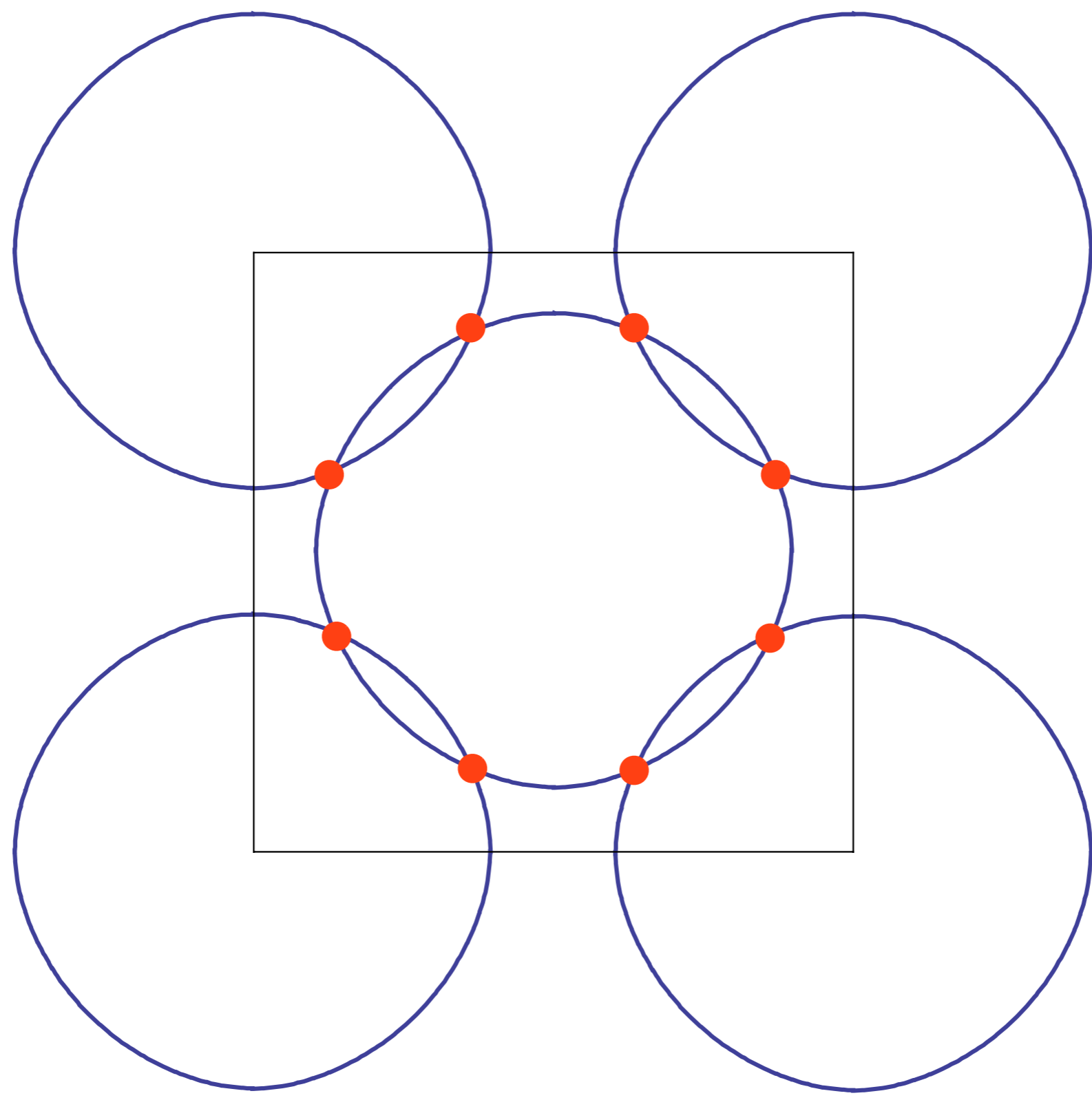
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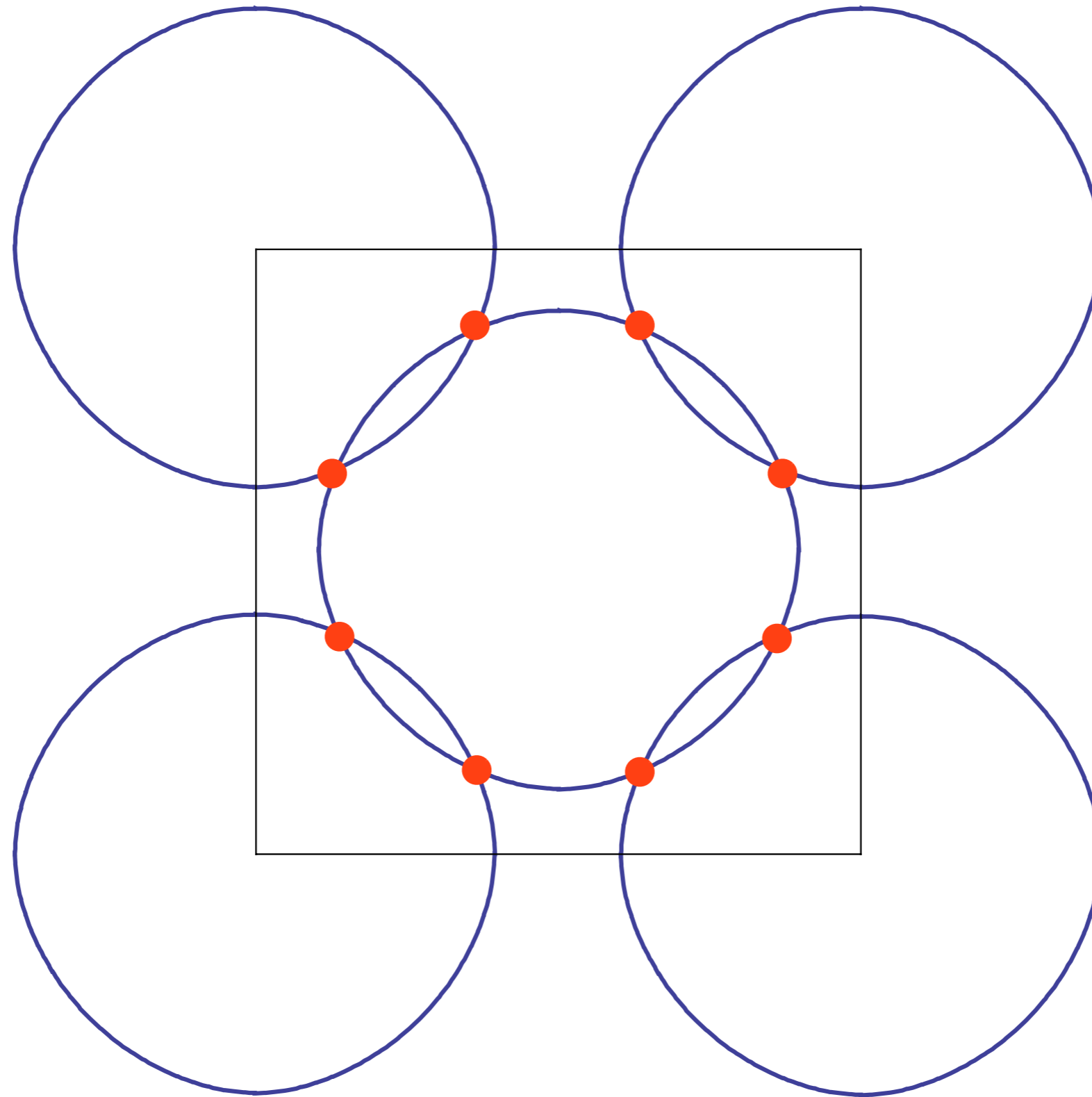
S. Sachdev, A. V. Chubukov, and A. Sokol, *Phys. Rev. B* **51**, 14874 (1995).
A. V. Chubukov and D. K. Morr, *Physics Reports* **288**, 355 (1997).



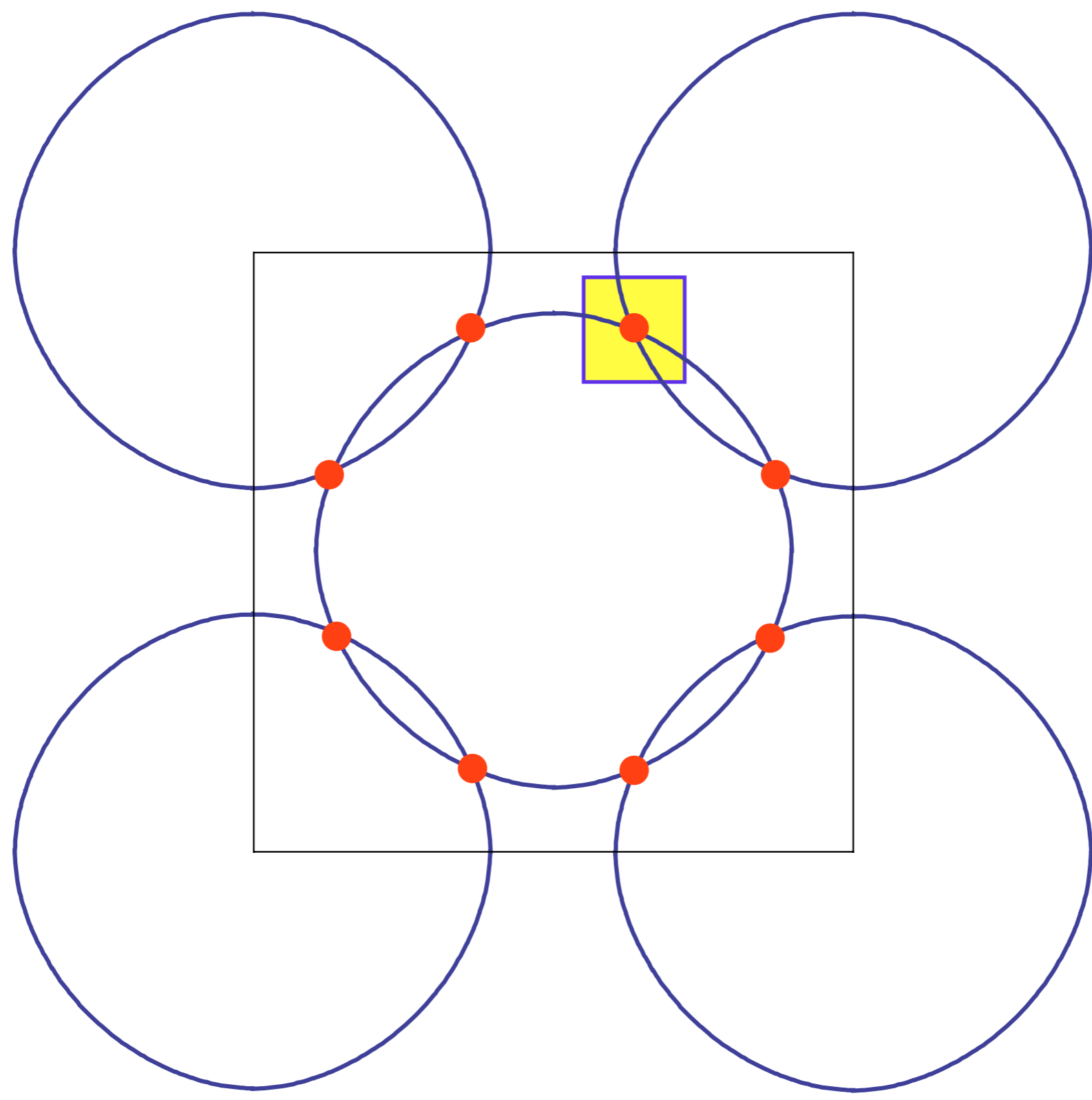
Fermi surfaces translated by $\mathbf{K} = (\pi, \pi)$.



“Hot” spots

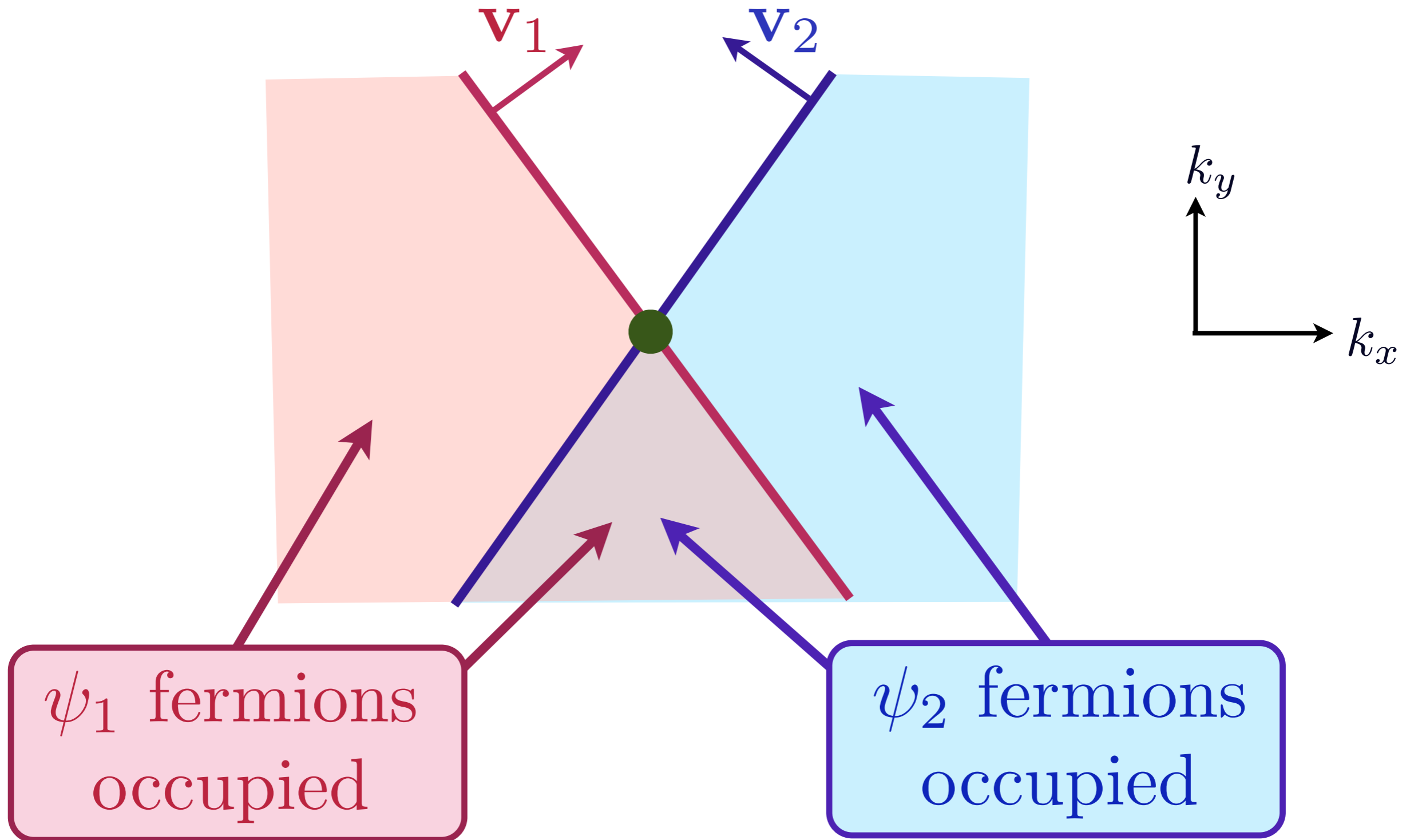


Low energy theory for critical point near hot spots

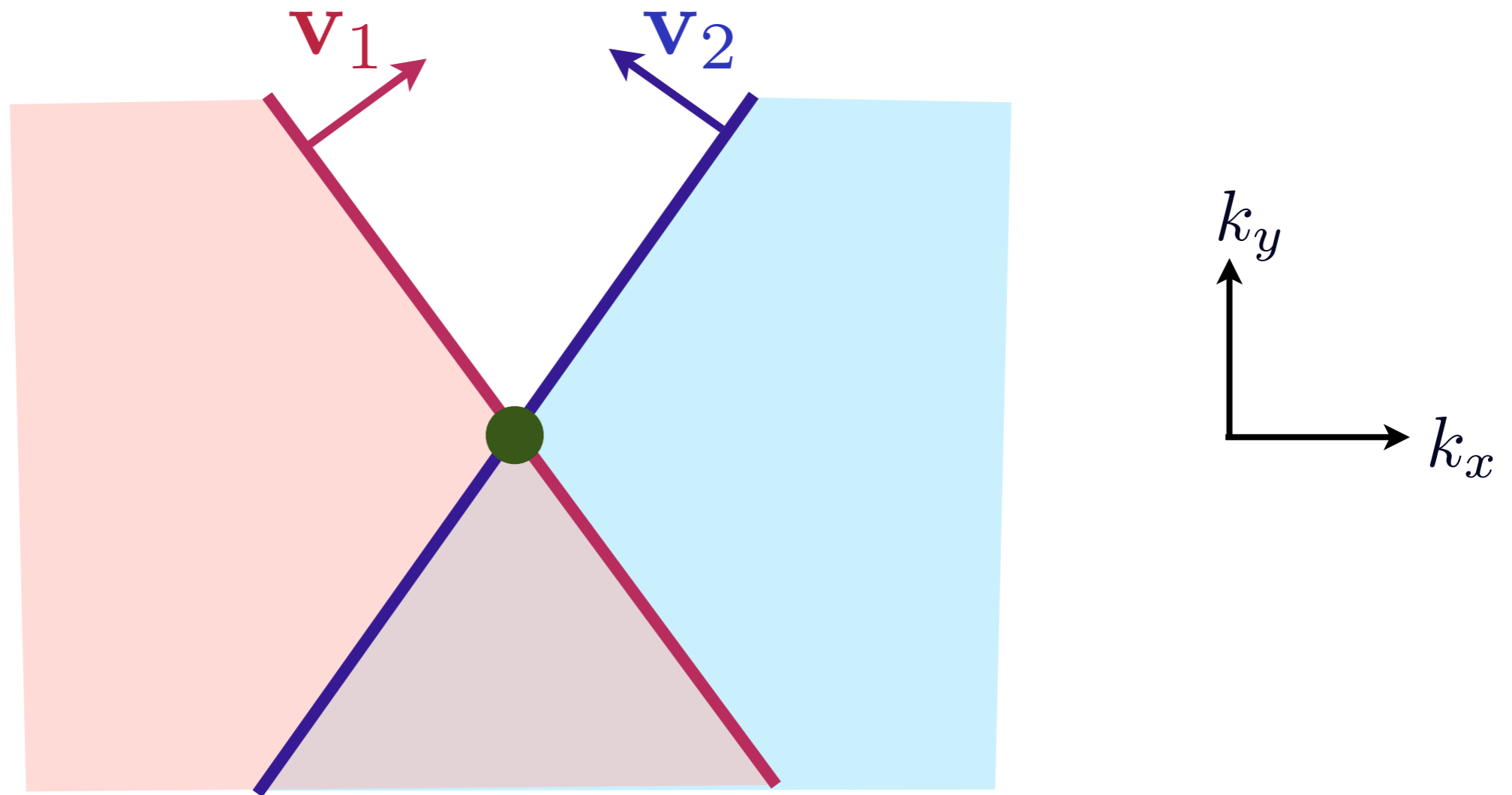


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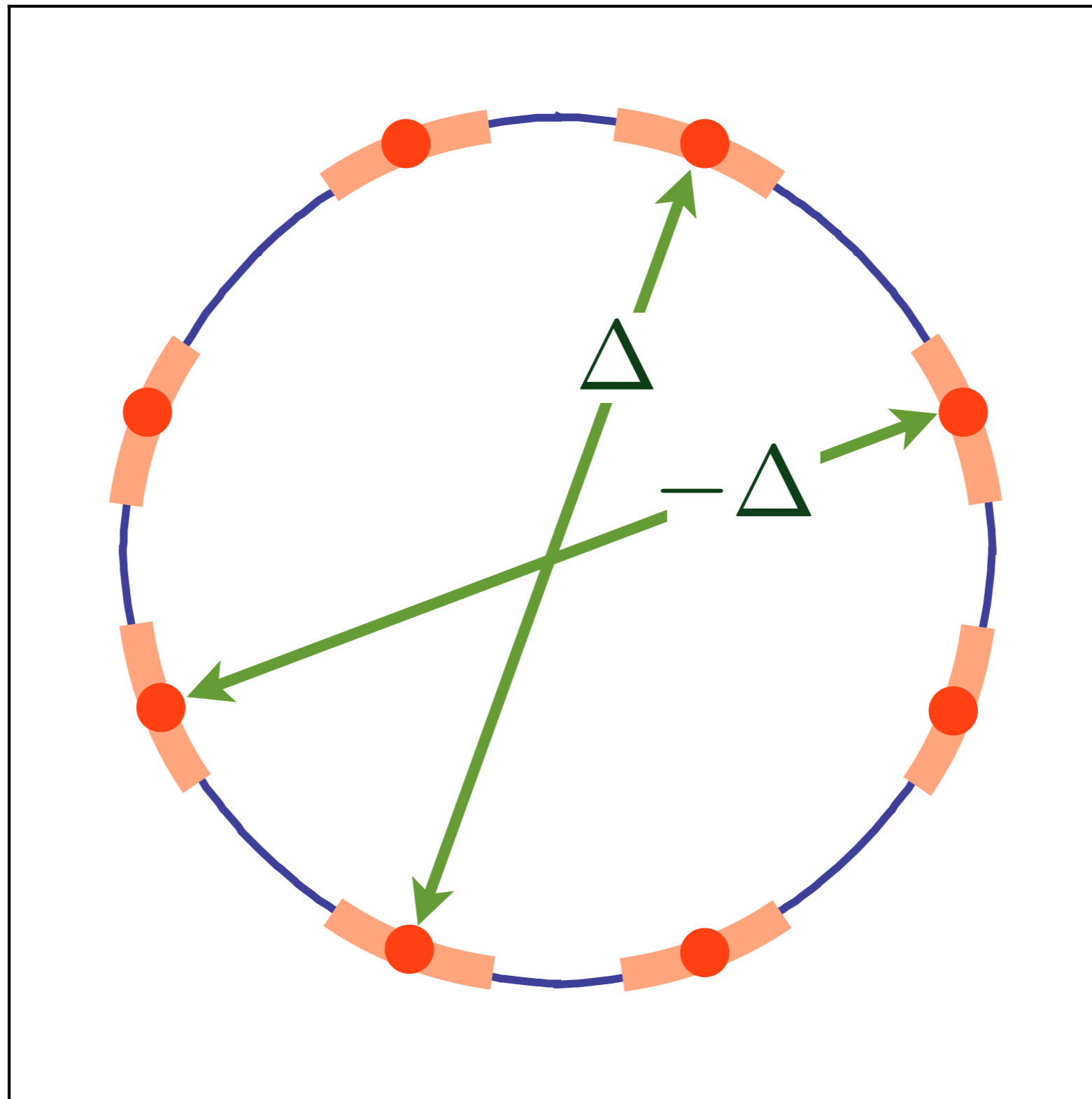
Theory has fermions $\psi_{1,2}$ (with Fermi velocities $\mathbf{v}_{1,2}$) and boson order parameter $\vec{\varphi}$, interacting with coupling λ



Critical point theory is strongly coupled in $d = 2$
Results are *independent* of coupling λ

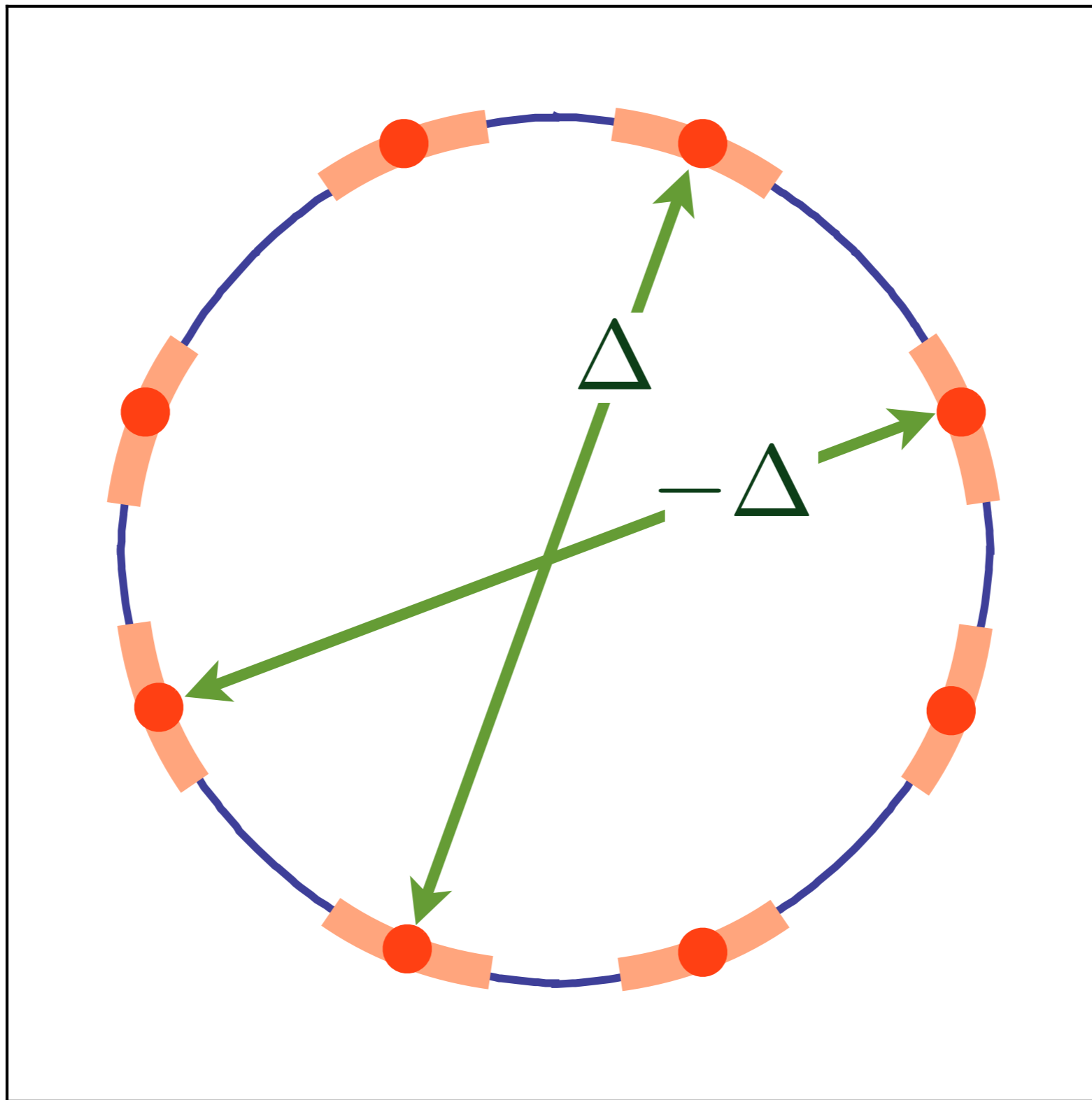


M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)



Unconventional pairing at and near hot spots

$$\langle c_{\mathbf{k}\alpha}^\dagger c_{-\mathbf{k}\beta}^\dagger \rangle = \varepsilon_{\alpha\beta} \Delta (\cos k_x - \cos k_y)$$



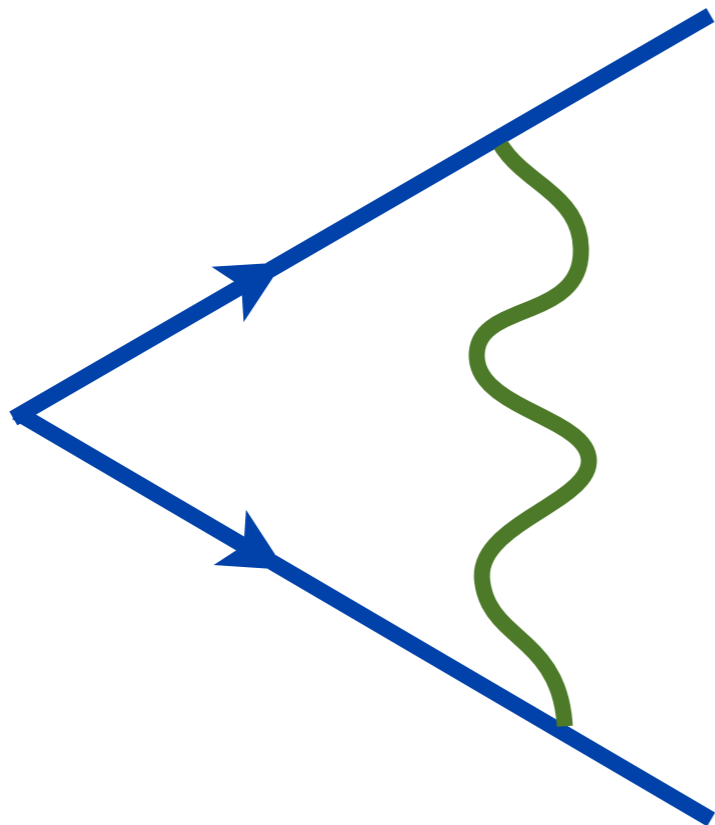
Unconventional pairing at and near hot spots

BCS theory

$$1 + \lambda_{\text{e-ph}} \log \left(\frac{\omega_D}{\omega} \right)$$



Cooper
logarithm



BCS theory

$$1 + \lambda_{\text{e-ph}} \log \left(\frac{\omega_D}{\omega} \right)$$

Electron-phonon
coupling

Debye
frequency

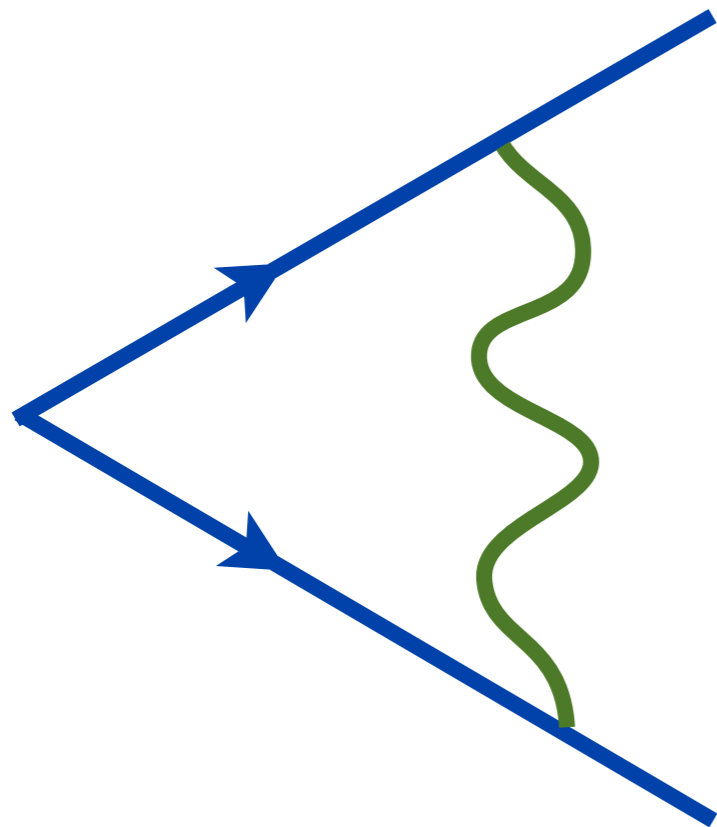
Implies

$$T_c \sim \omega_D \exp(-1/\lambda)$$

Enhancement of pairing susceptibility by interactions

Antiferromagnetic fluctuations: weak-coupling

$$1 + \left(\frac{U}{t}\right)^2 \log\left(\frac{E_F}{\omega}\right)$$



Cooper
logarithm

V. J. Emery, *J. Phys. (Paris) Colloq.* **44**, C3-977 (1983)

D. J. Scalapino, E. Loh, and J. E. Hirsch, *Phys. Rev. B* **34**, 8190 (1986)

K. Miyake, S. Schmitt-Rink, and C. M. Varma, *Phys. Rev. B* **34**, 6554 (1986)

S. Raghu, S. A. Kivelson, and D. J. Scalapino, *Phys. Rev. B* **81**, 224505 (2010)

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Antiferromagnetic fluctuations: weak-coupling

$$1 + \left(\frac{U}{t}\right)^2 \log\left(\frac{E_F}{\omega}\right)$$

Applies in a Fermi liquid
as repulsive interaction $U \rightarrow 0$.

Fermi
energy

Implies

$$T_c \sim E_F \exp\left(-\left(t/U\right)^2\right)$$

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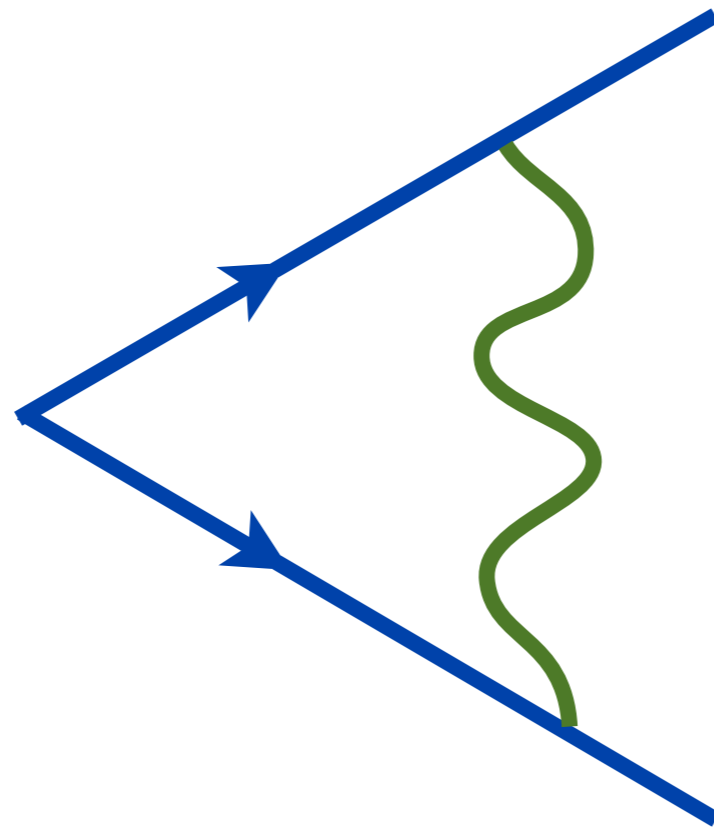
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Enhancement of pairing susceptibility by interactions

Spin density wave quantum critical point

$$1 + \frac{\alpha}{\pi(1 + \alpha^2)} \log^2 \left(\frac{E_F}{\omega} \right)$$



M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

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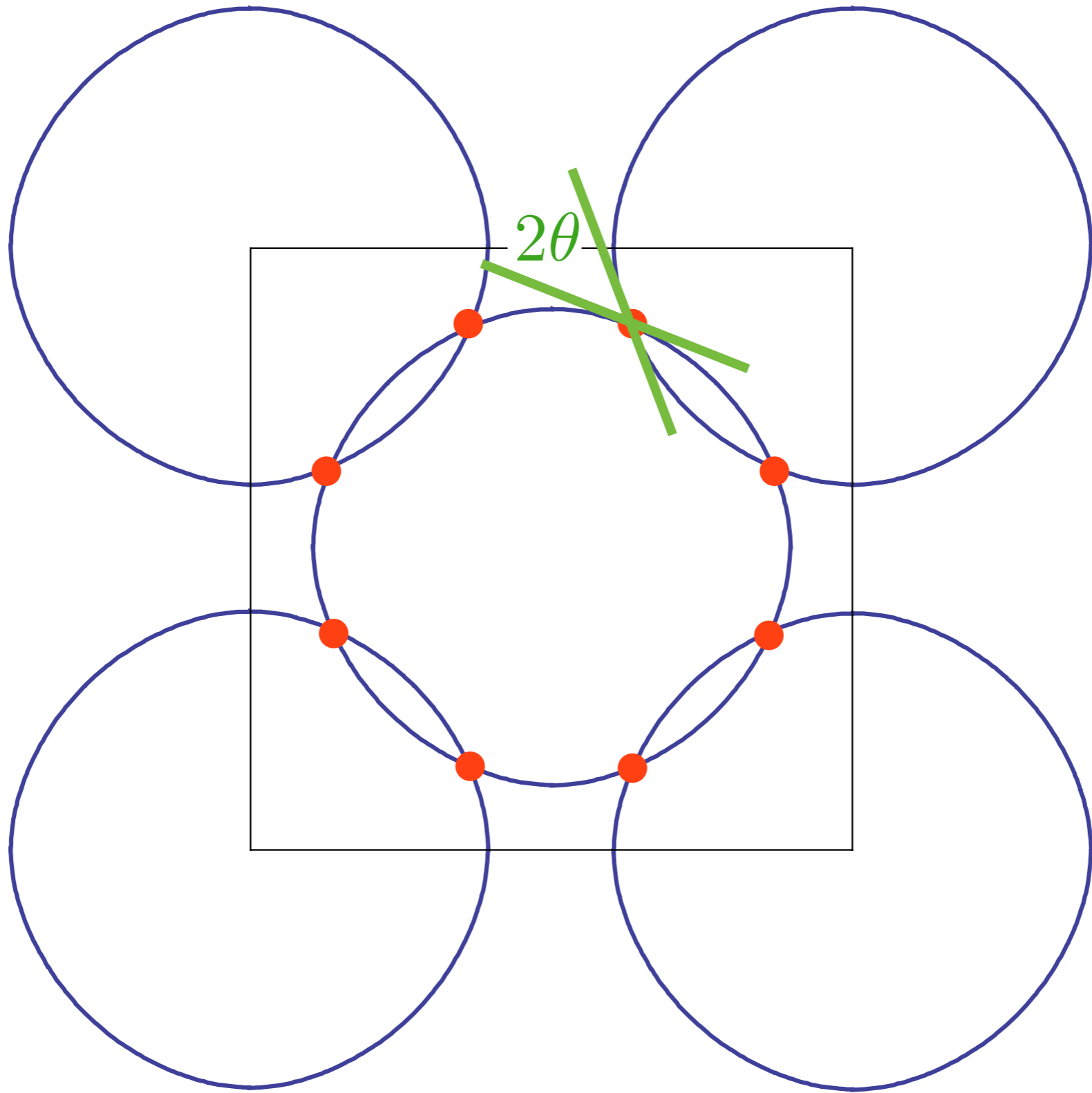
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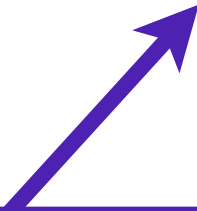
$\alpha = \tan \theta$, where 2θ is
the angle between Fermi lines.
Independent of interaction strength
 U in 2 dimensions.

(see also Ar. Abanov, A. V. Chubukov, and A. M. Finkel'stein, *Europhys. Lett.* **54**, 488 (2001))
M. A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)



Enhancement of pairing susceptibility by interactions

Spin density wave quantum critical point

$$1 + \frac{\alpha}{\pi(1 + \alpha^2)} \log^2 \left(\frac{E_F}{\omega} \right)$$


- \log^2 singularity arises from Fermi lines; singularity *at* hot spots is weaker.
- Interference between BCS and quantum-critical logs.
- Momentum dependence of self-energy is crucial.
- Not suppressed by $1/N$ factor in $1/N$ expansion.

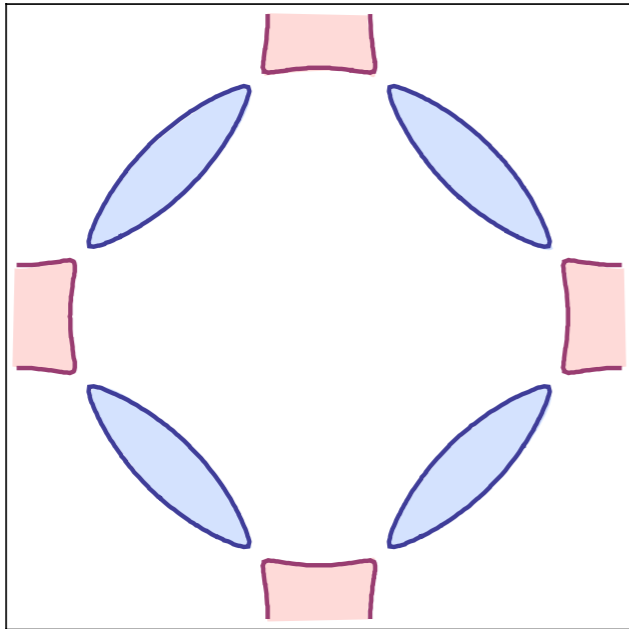
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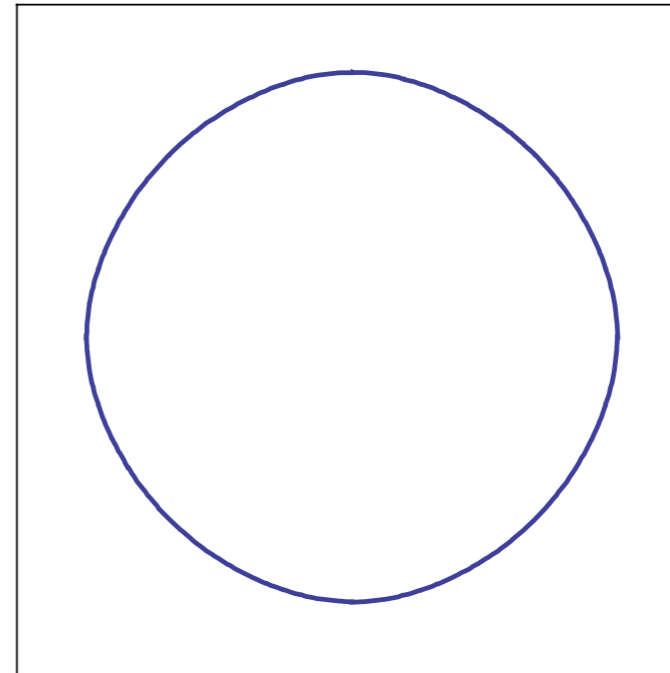
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Quantum phase transition with Fermi surface reconstruction



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Metal with electron
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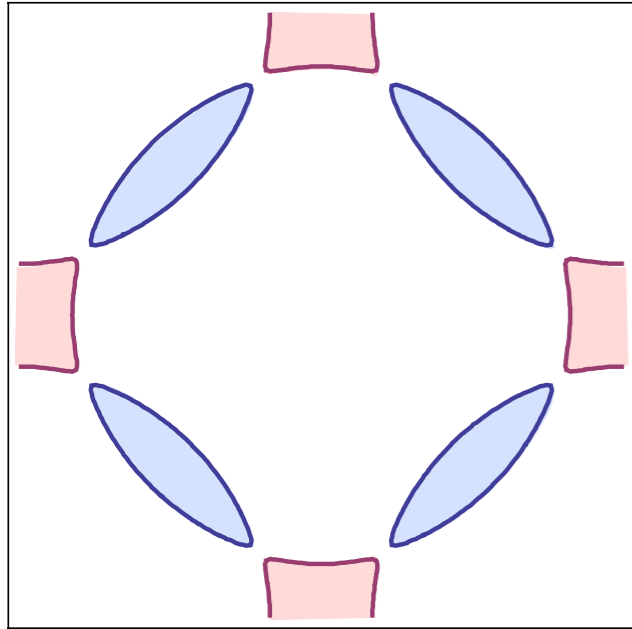


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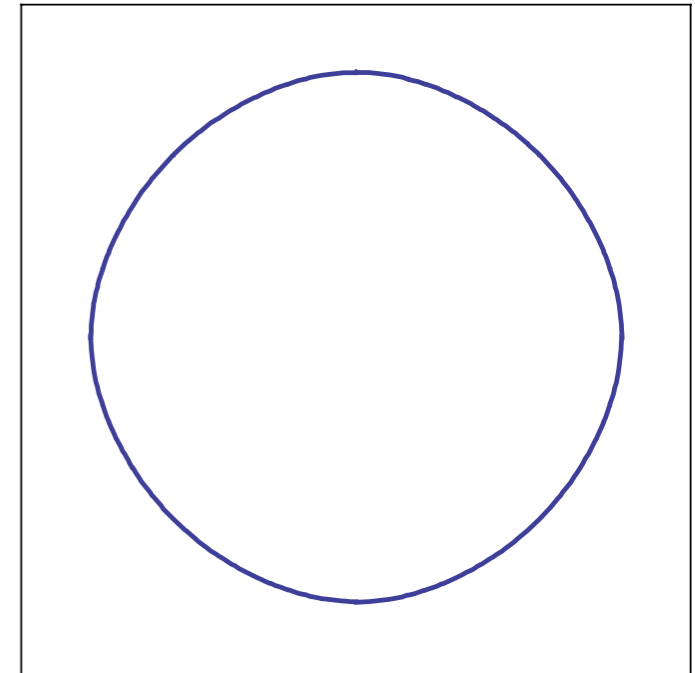


Separating onset of SDW order and Fermi surface reconstruction



$$\langle \vec{\varphi} \rangle \neq 0$$

Metal with electron
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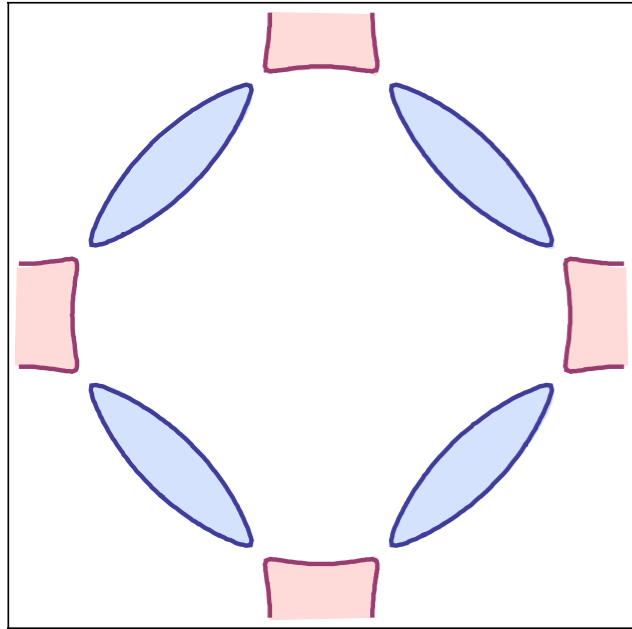


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Fermi surface



Separating onset of SDW order and Fermi surface reconstruction

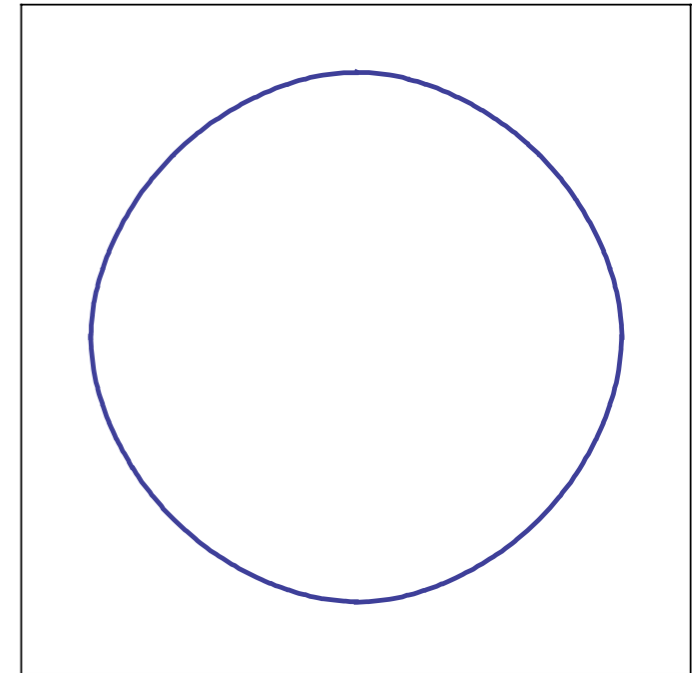


$$\langle \vec{\varphi} \rangle \neq 0$$

Metal with electron
and hole pockets

Electron and/or hole
Fermi pockets form in
“local” SDW order, but
quantum fluctuations
destroy long-range
SDW order

$$\langle \vec{\varphi} \rangle = 0$$

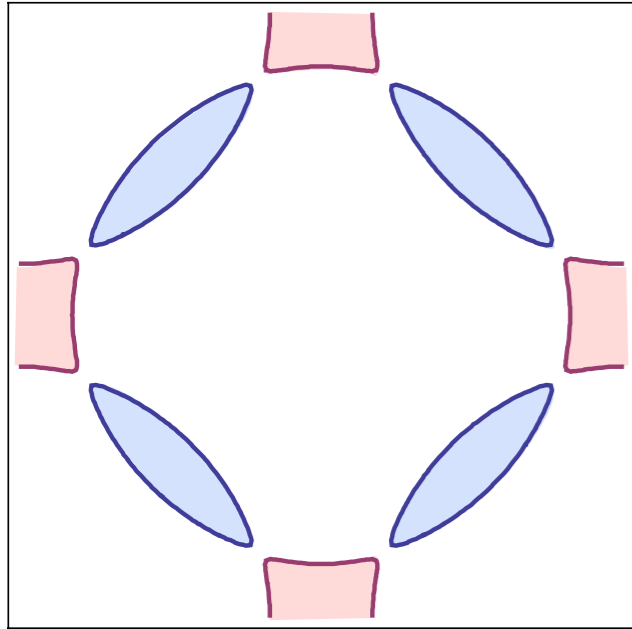


$$\langle \vec{\varphi} \rangle = 0$$

Metal with “large”
Fermi surface

T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

Separating onset of SDW order and Fermi surface reconstruction



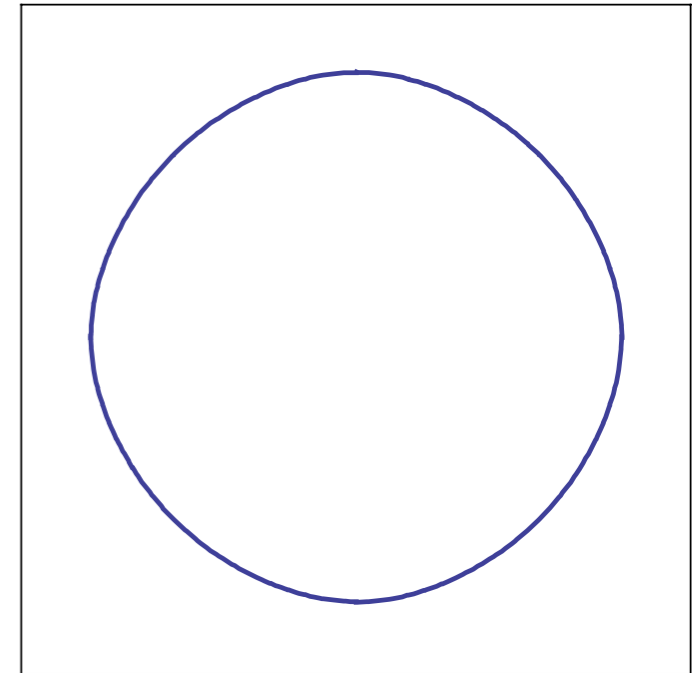
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Fractionalized Fermi
liquid (FL*) phase
with no symmetry
breaking and “small”
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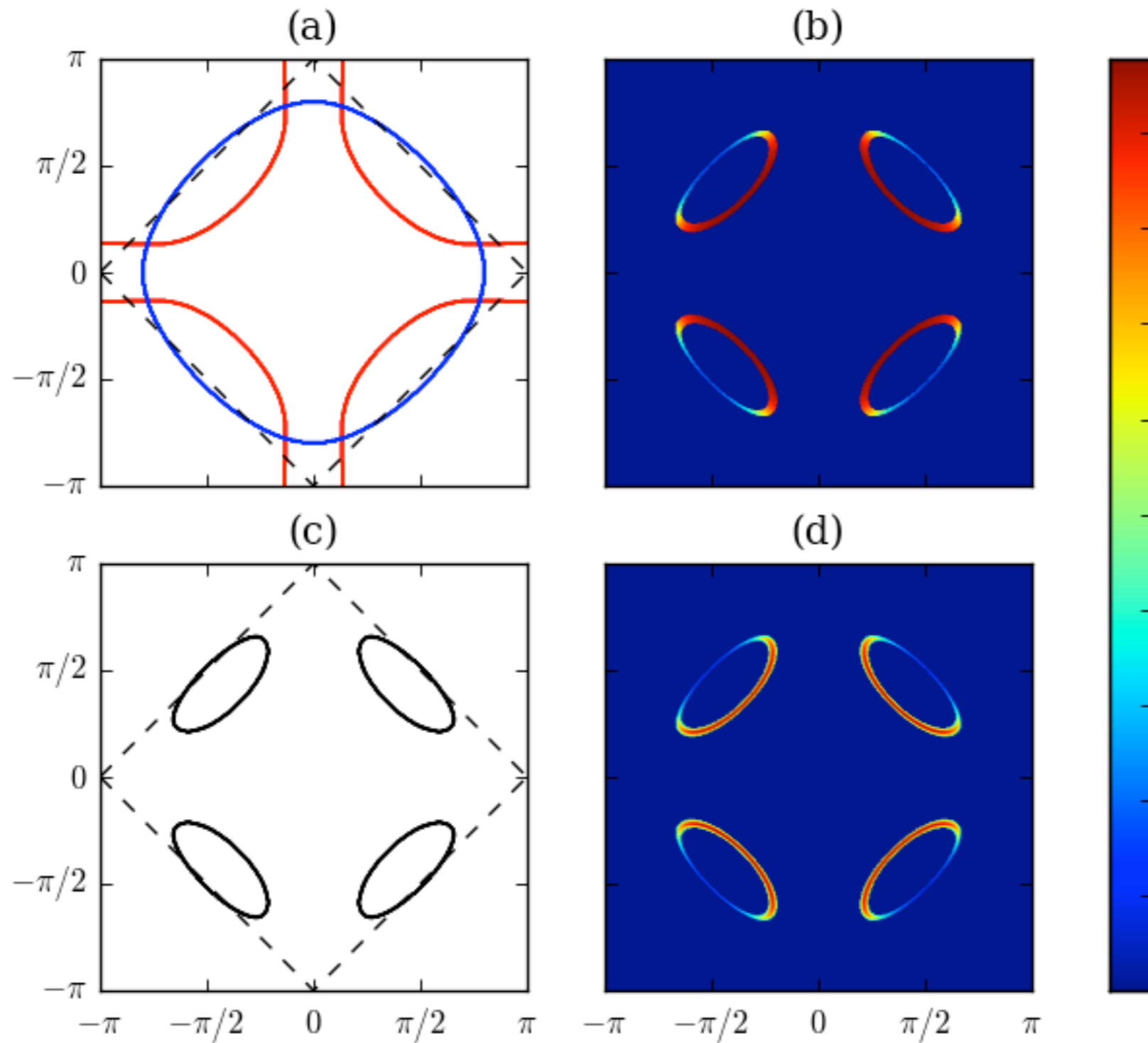


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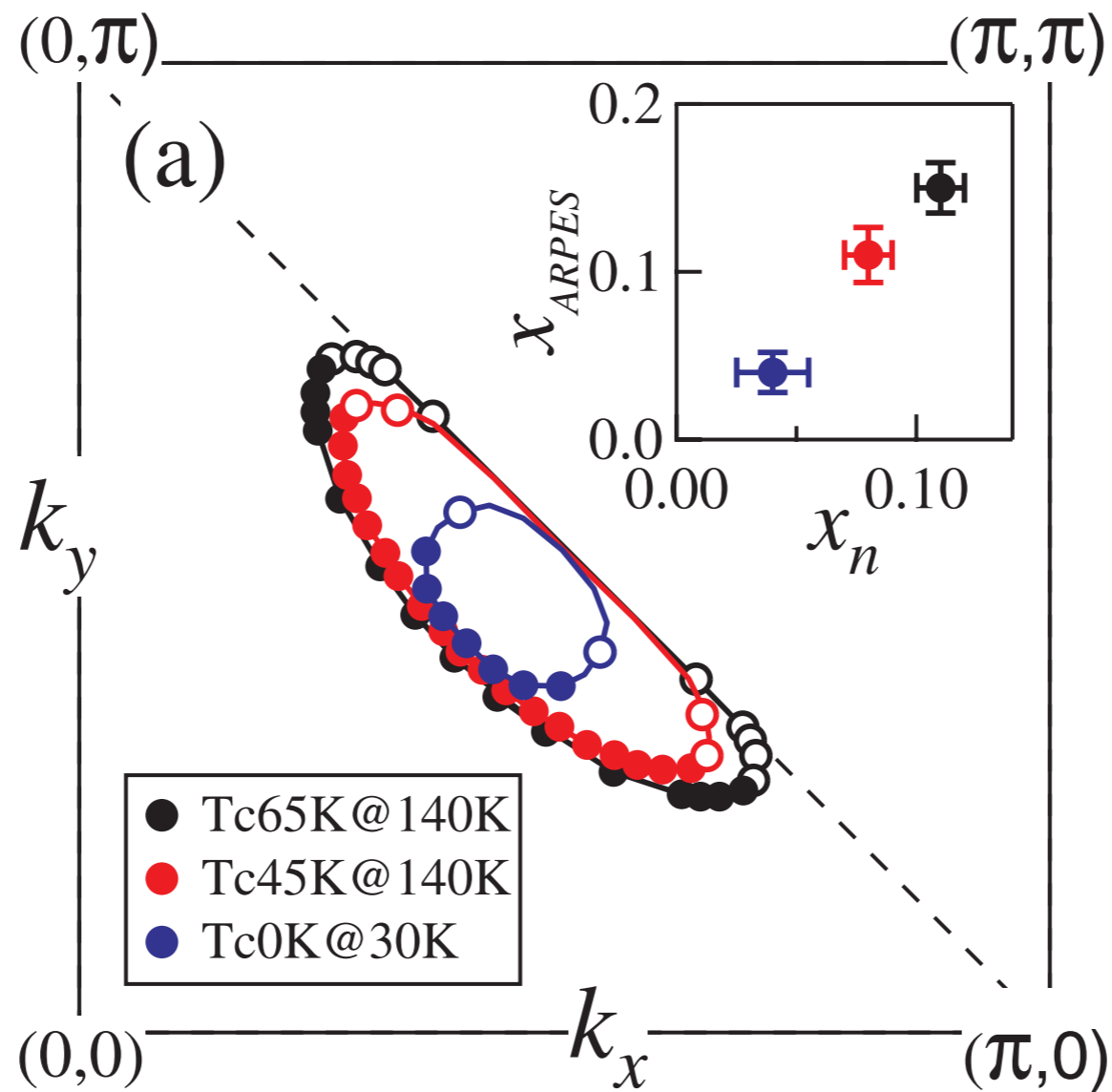
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T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

FL* phase has Fermi pockets without long-range antiferromagnetism, along with emergent gauge excitations



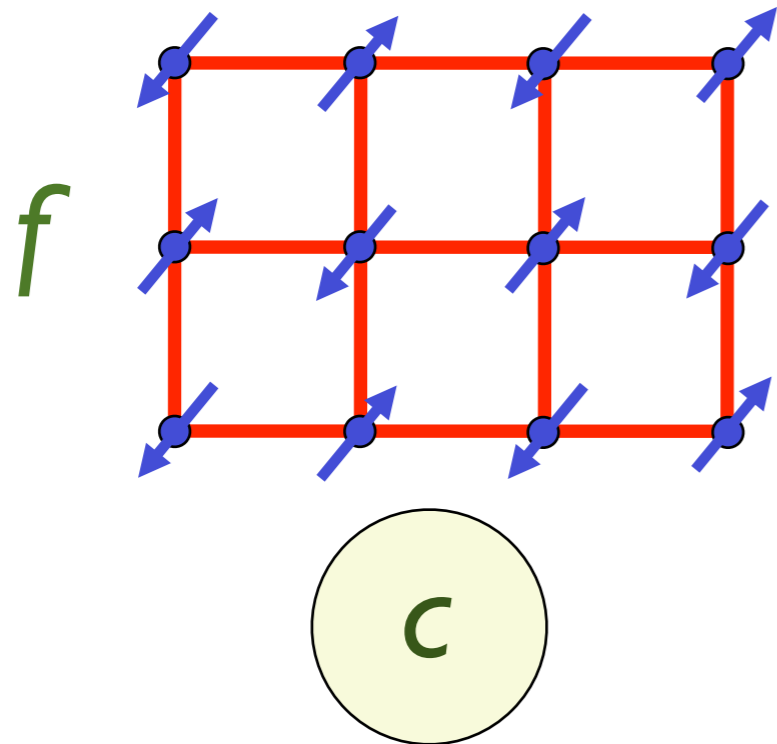
Y. Qi and S. Sachdev, *Physical Review B* **81**, 115129 (2010)



Reconstructed Fermi Surface of Underdoped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ Cuprate Superconductors

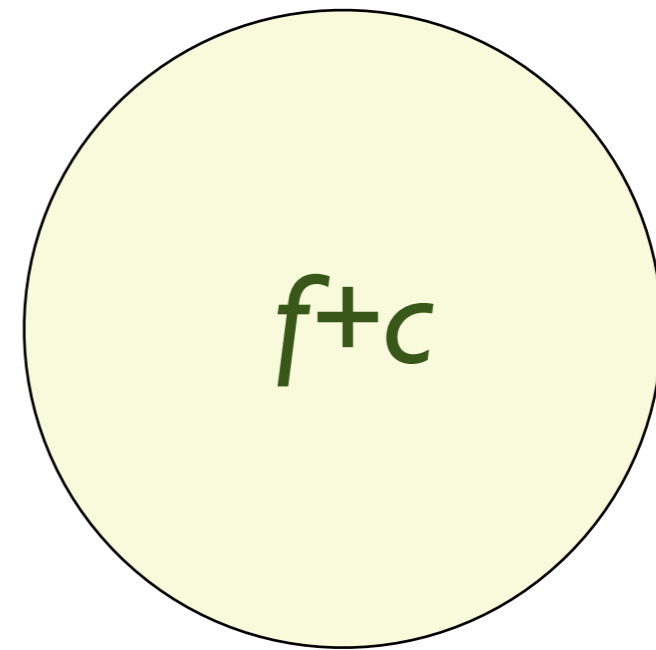
H.-B. Yang,¹ J. D. Rameau,¹ Z.-H. Pan,¹ G. D. Gu,¹ P. D. Johnson,¹ H. Claus,² D. G. Hinks,² and T. E. Kidd³

Magnetic order and the heavy Fermi liquid in the Kondo lattice



$$\langle \vec{\varphi} \rangle \neq 0$$

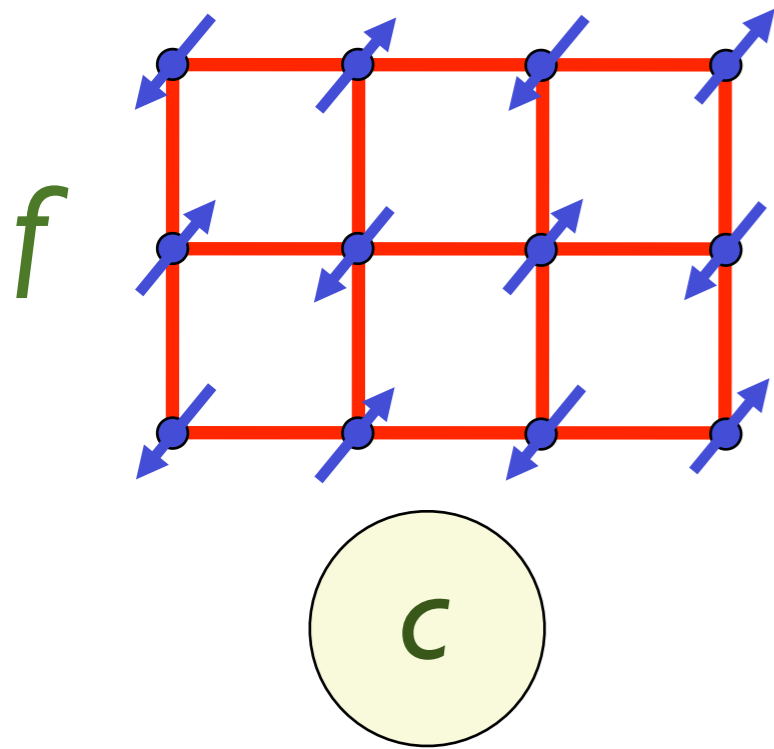
Magnetic Metal:
f-electron moments
and
c-conduction electron
Fermi surface



$$\langle \vec{\varphi} \rangle = 0$$

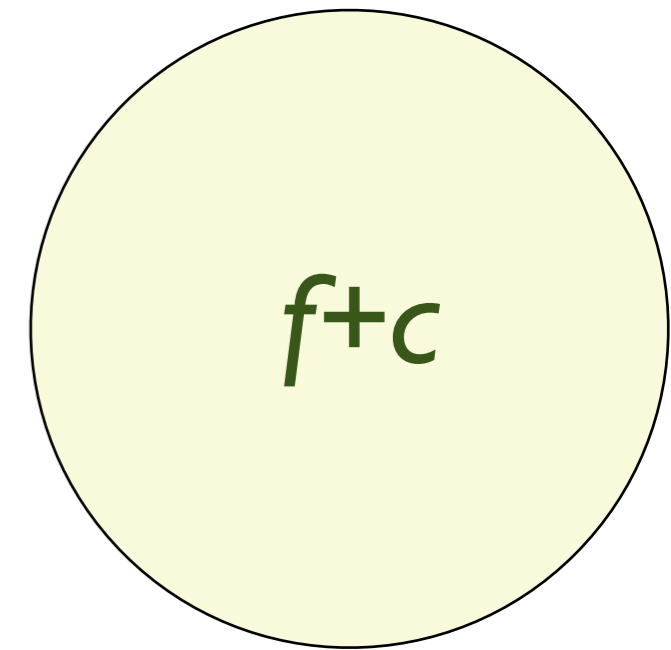
Heavy Fermi liquid
with “large” Fermi
surface of
hybridized f and
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Separating onset of SDW order and the heavy Fermi liquid in the Kondo lattice



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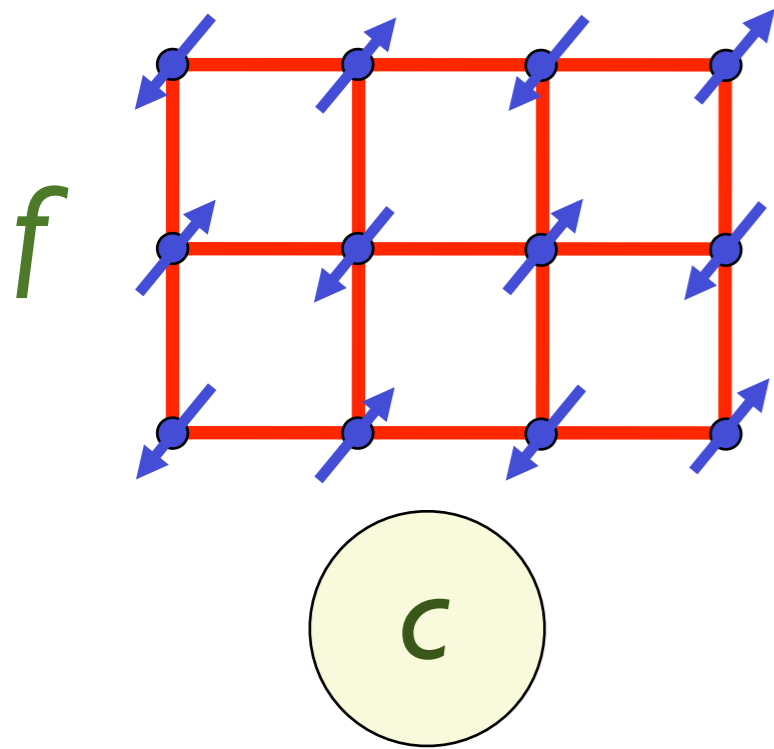


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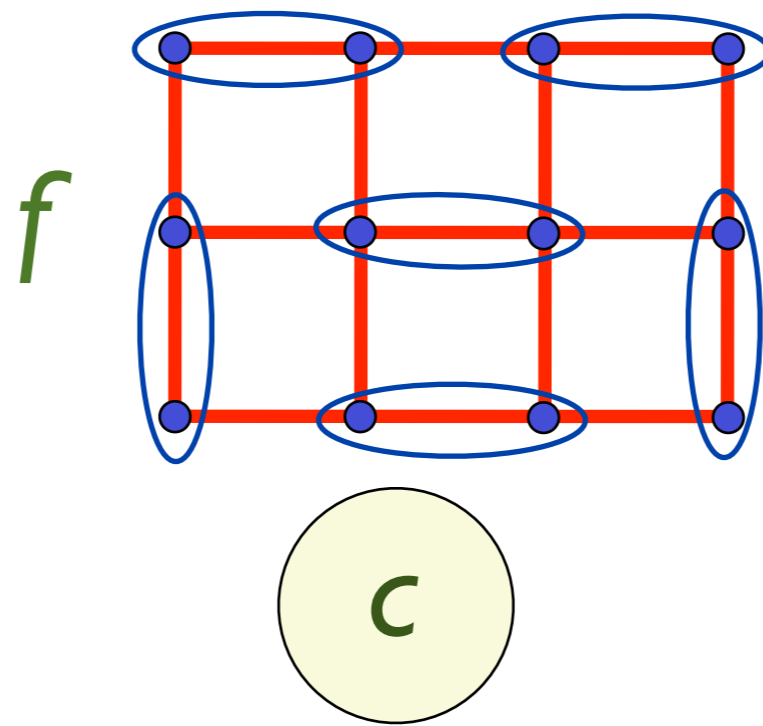
T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

Separating onset of SDW order and the heavy Fermi liquid in the Kondo lattice



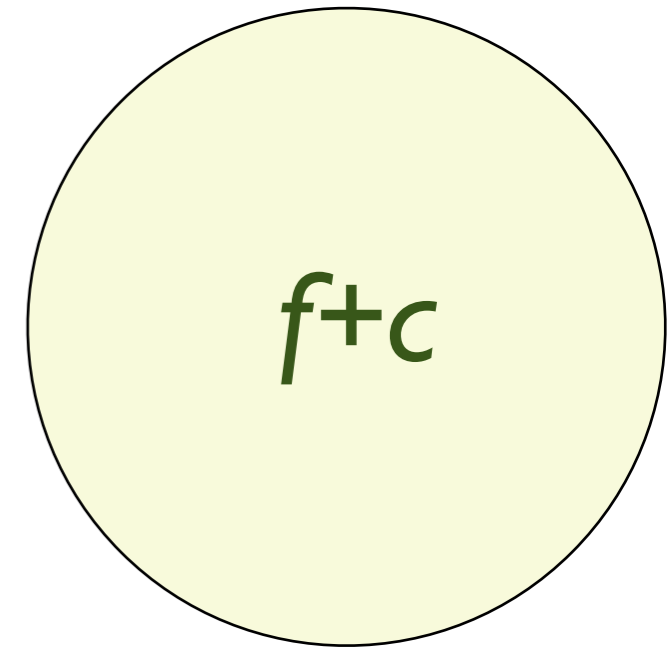
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$$\langle \vec{\varphi} \rangle = 0$$

Conduction electron
Fermi surface
and
spin-liquid of
f-electrons

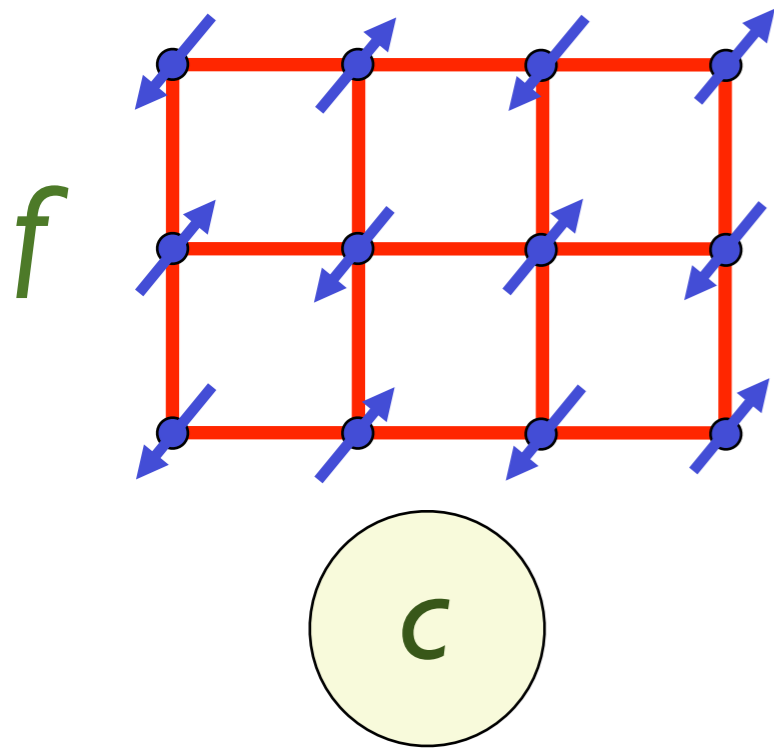


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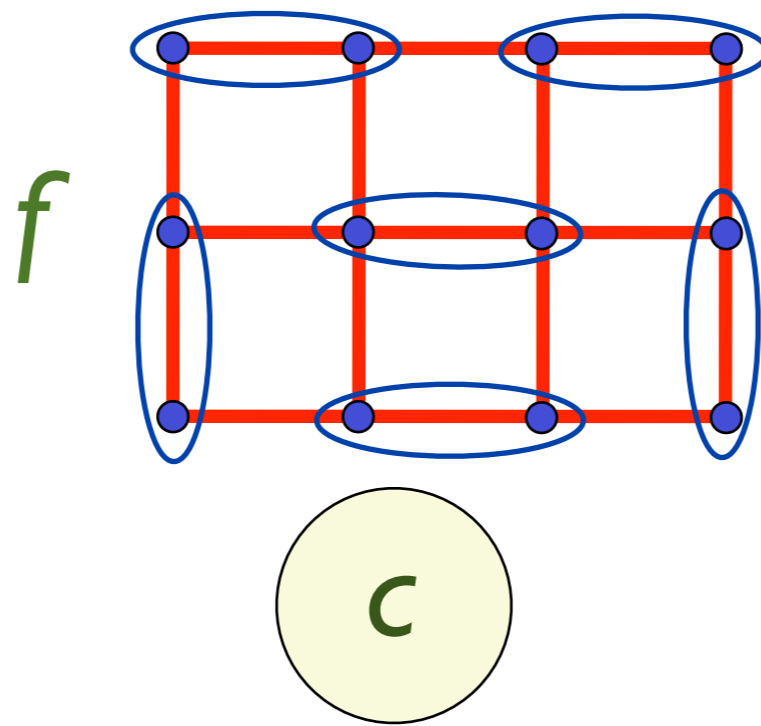
T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

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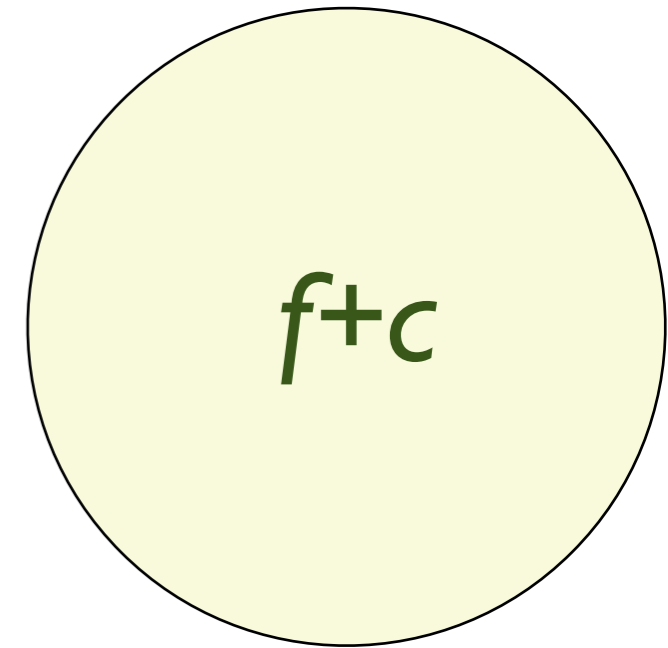
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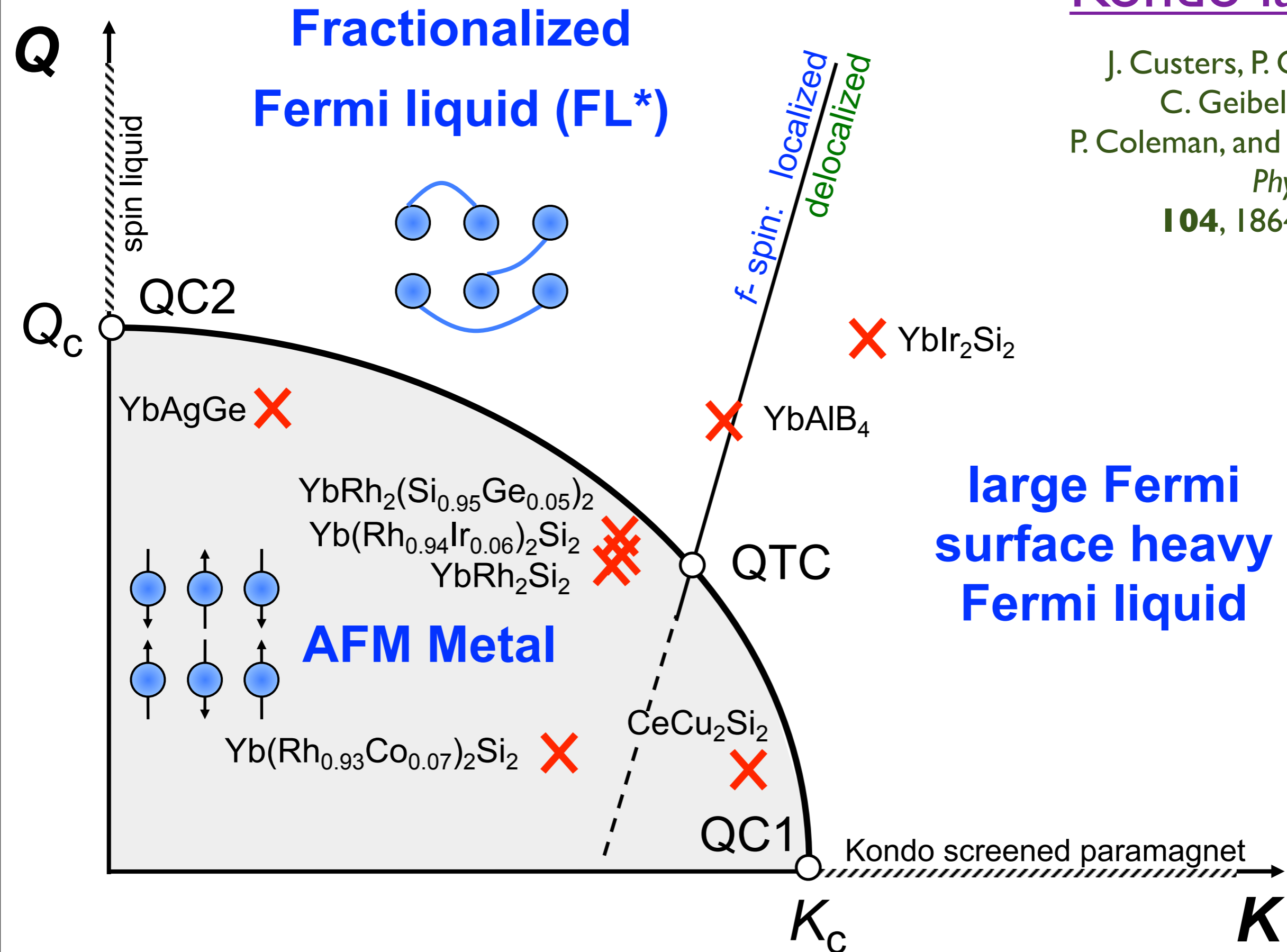
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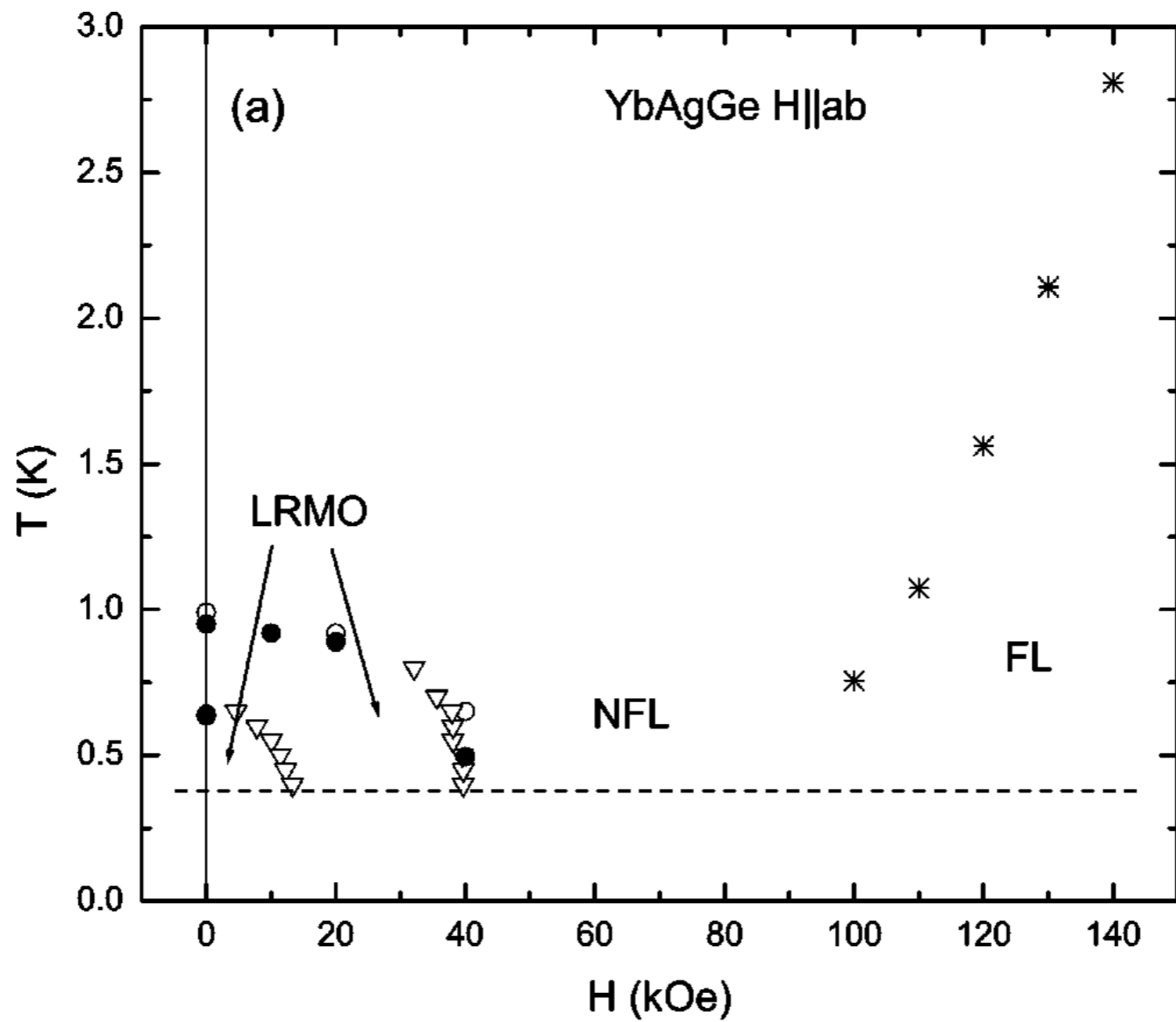
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T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

Experimental perspective on same phase diagrams of Kondo lattice

J. Custers, P. Gegenwart,
C. Geibel, F. Steglich,
P. Coleman, and S. Paschen,
Phys. Rev. Lett.
104, 186402 (2010)

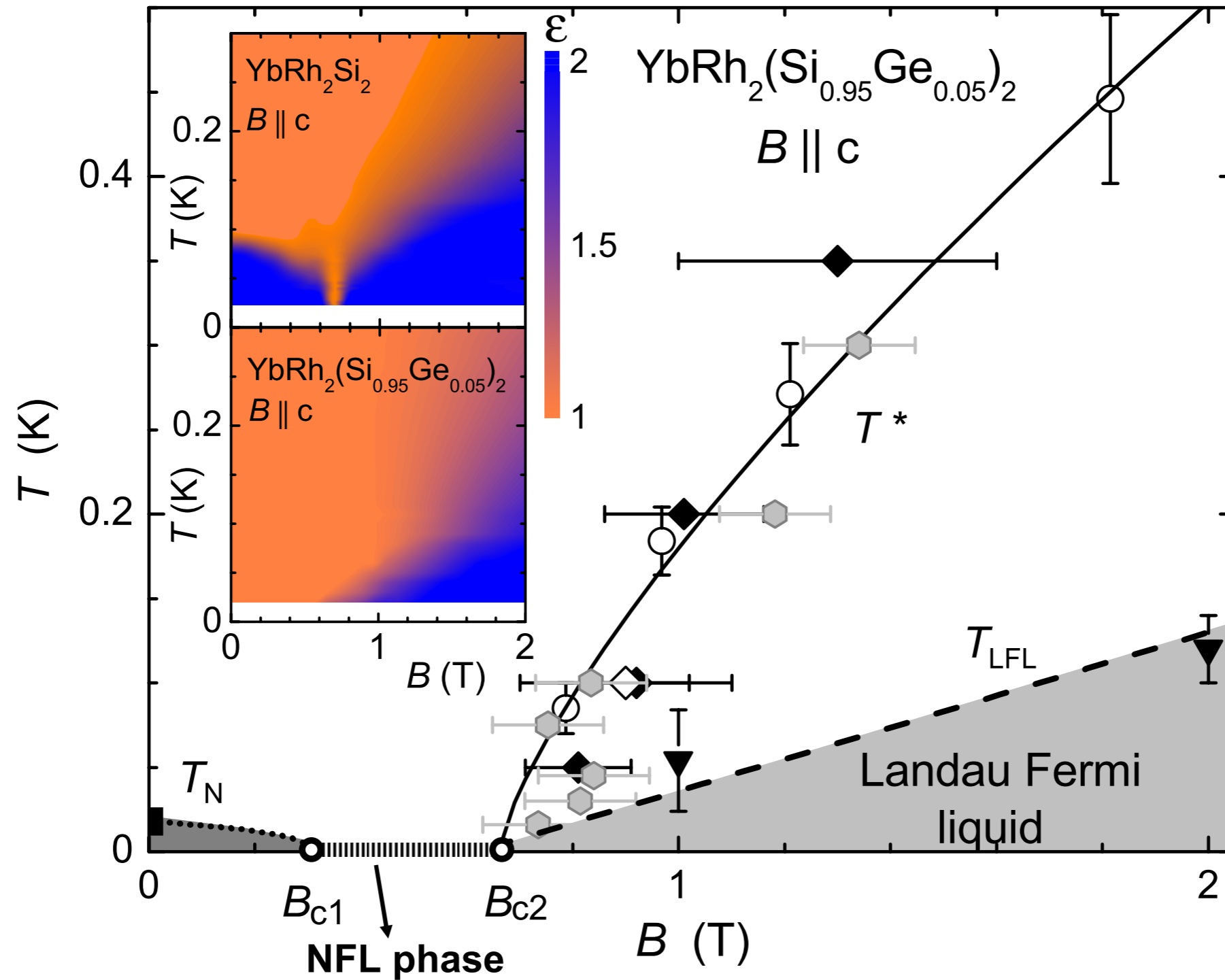




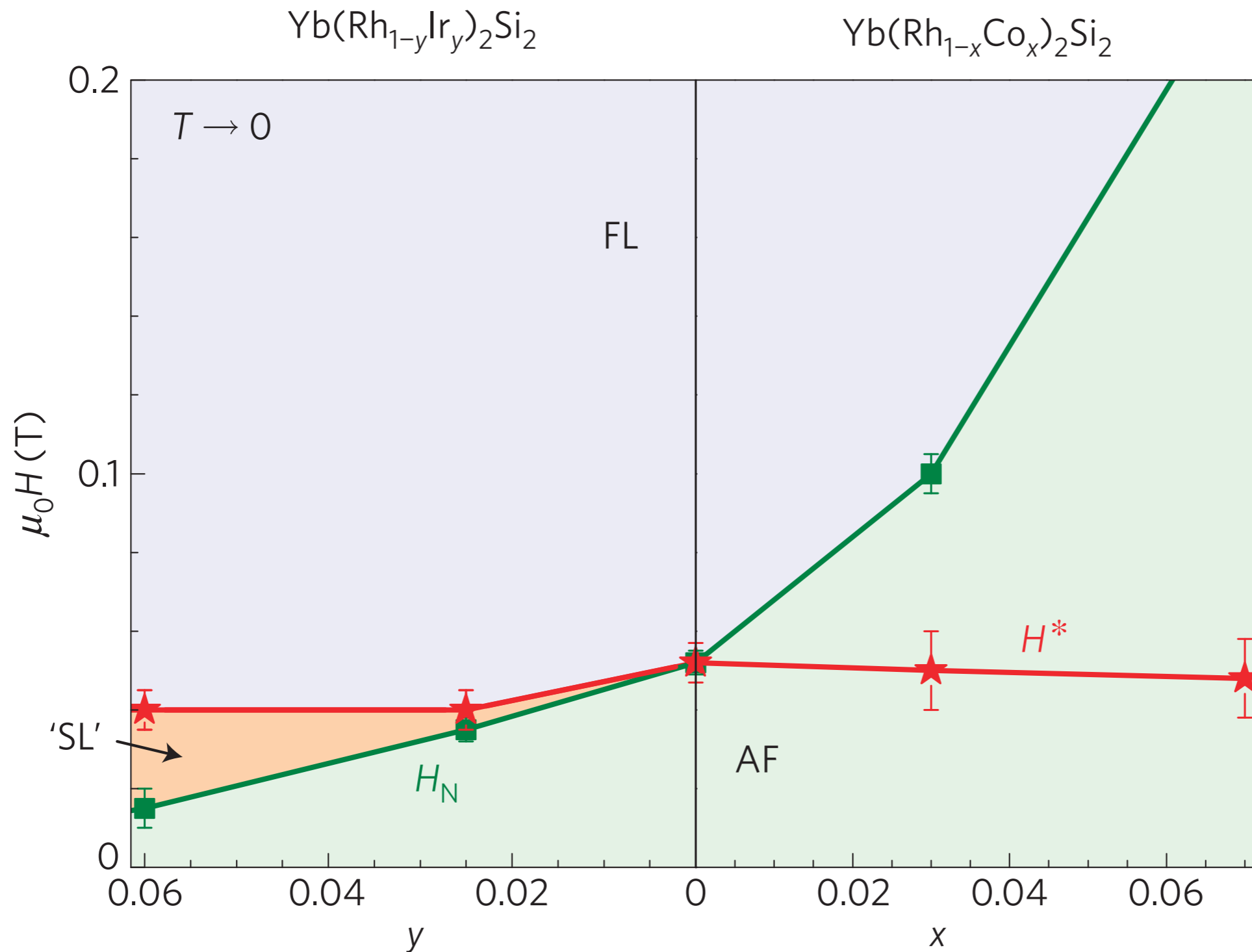
PHYSICAL REVIEW B **69**, 014415 (2004)

Magnetic field induced non-Fermi-liquid behavior in YbAgGe single crystals

S. L. Bud'ko,¹ E. Morosan,^{1,2} and P. C. Canfield^{1,2}



J. Custers, P. Gegenwart, C. Geibel, F. Steglich, P. Coleman, and S. Paschen,
Phys. Rev. Lett. **104**, 186402 (2010)



Detaching the antiferromagnetic quantum critical point from the Fermi-surface reconstruction in YbRh₂Si₂

Nature Physics 5, 465 (2009)

S. Friedemann^{1*}, T. Westerkamp¹, M. Brando¹, N. Oeschler¹, S. Wirth¹, P. Gegenwart^{1,2}, C. Krellner¹, C. Geibel¹ and F. Steglich^{1*}

Characteristics of FL* phase

- Fermi surface volume does not count all electrons.

T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

Characteristics of FL* phase

- Fermi surface volume does not count all electrons.
- Such a phase *must* have neutral $S = 1/2$ excitations (“spinons”), and collective spinless gauge excitations (“topological” order).

T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

Characteristics of FL* phase

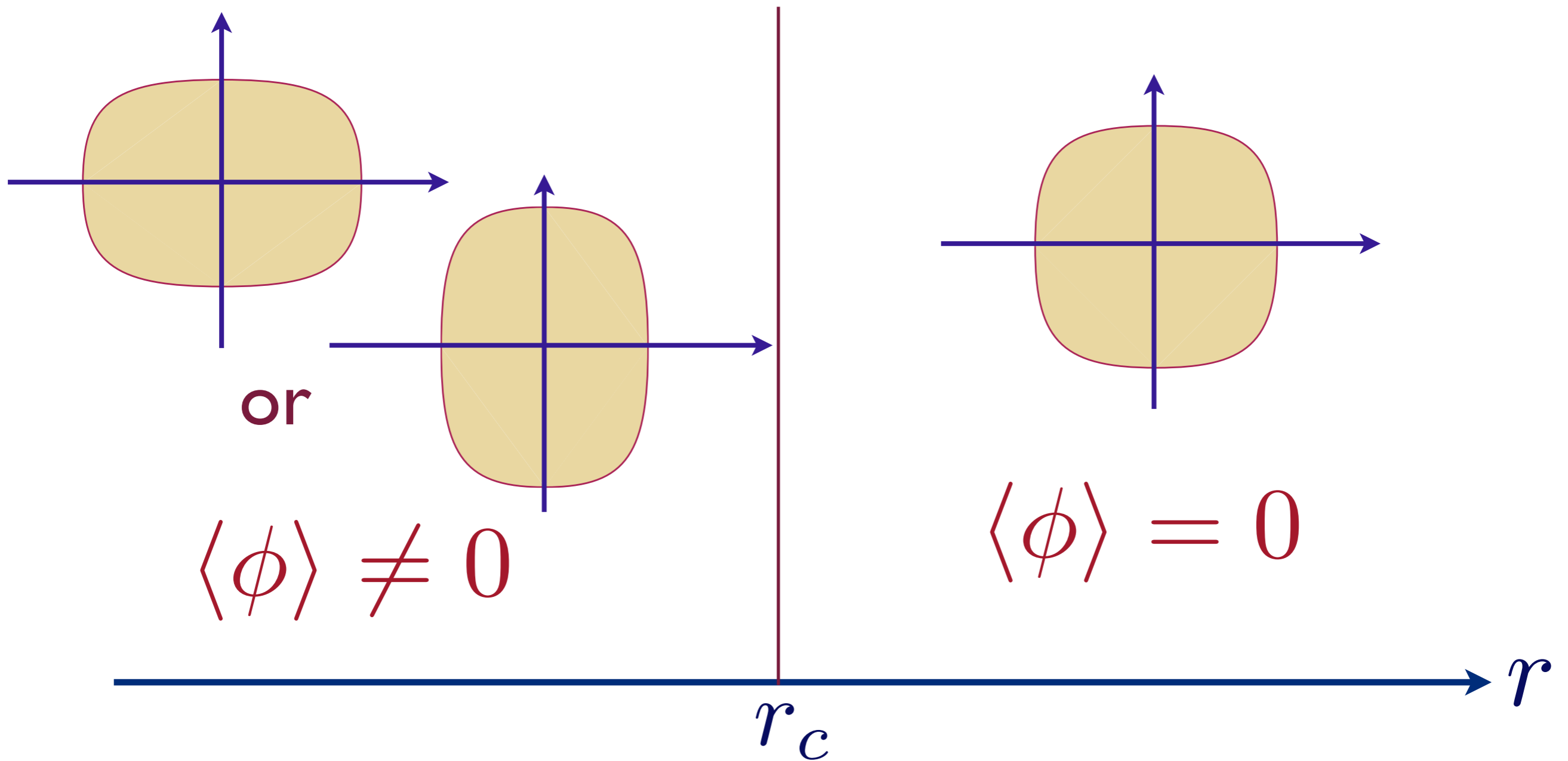
- Fermi surface volume does not count all electrons.
- Such a phase *must* have neutral $S = 1/2$ excitations (“spinons”), and collective spinless gauge excitations (“topological” order).
- These topological excitations are needed to account for the deficit in the Fermi surface volume, in M. Oshikawa’s proof of the Luttinger theorem.

T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003)

1. Fate of the Fermi surface:
reconstruction or not ? Experimental motivations from cuprates and pnictides
2. Conventional theory and its breakdown in two spatial dimensions
3. Fermi surface reconstruction: onset of unconventional superconductivity
4. Fermi surface reconstruction *without* symmetry breaking: metals with “topological” order
5. The nematic transition: field theory of antipodal Fermi surface points

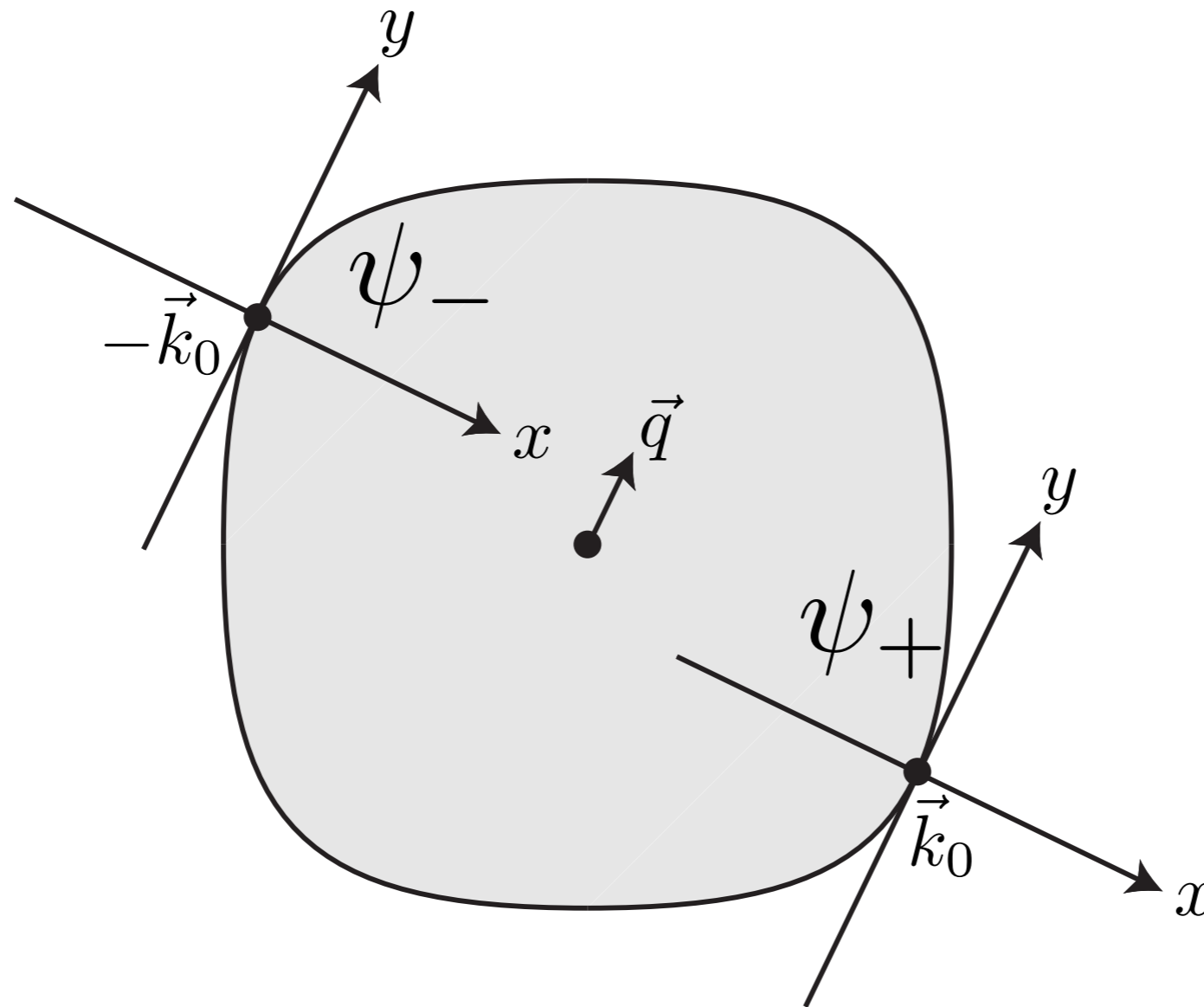
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Quantum criticality of Ising-nematic ordering



Pomeranchuk instability as a function of coupling r

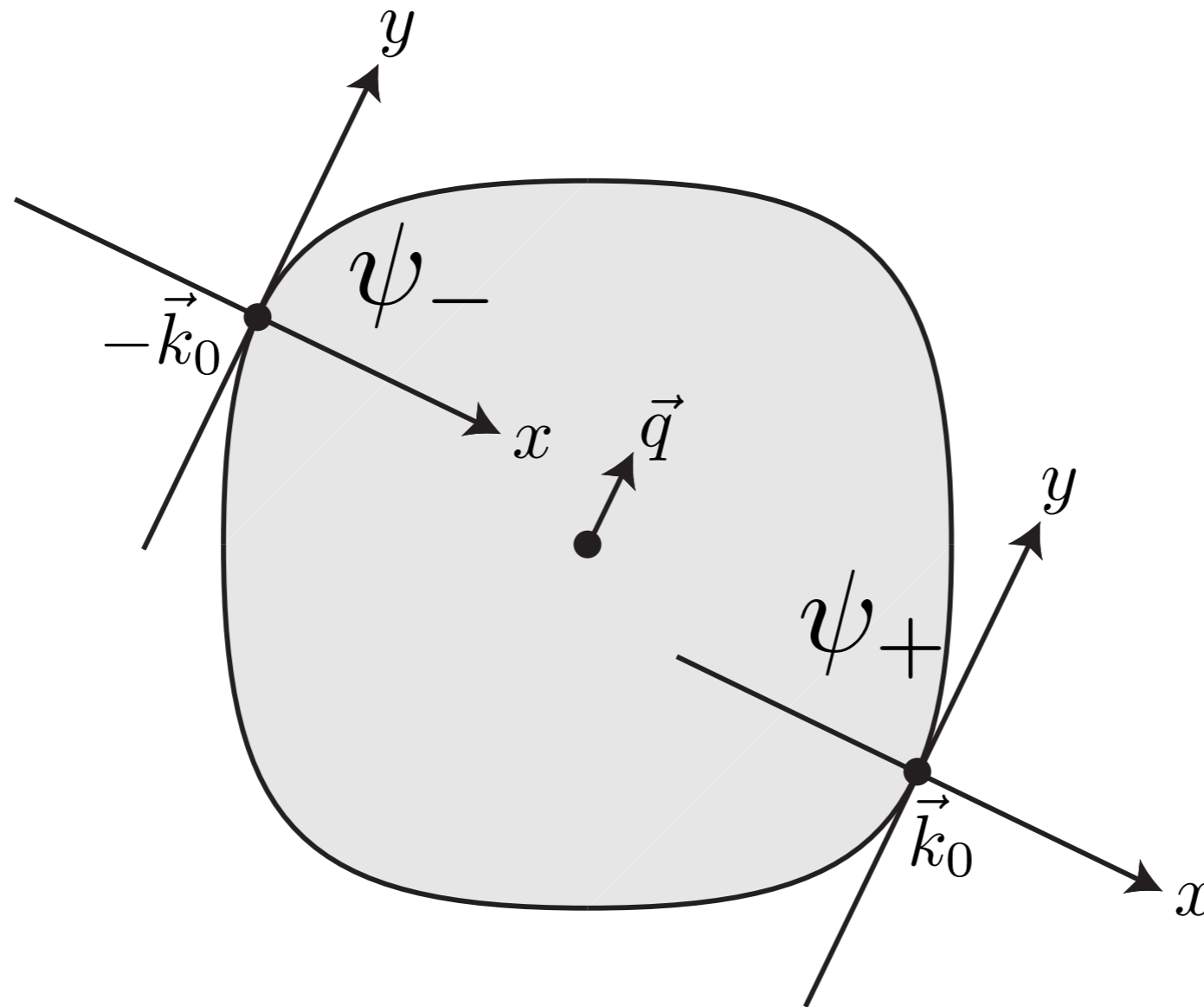
Quantum criticality of Ising-nematic ordering



- Critical point is described by an *infinite* set of 2+1 dimensional field theories, one for each direction \hat{q} . Each theory has a finite Fermi surface curvature, with quasiparticle dispersion $= v_F q_x + q_y^2 / (2m^*)$.

M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

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M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

Quantum criticality of Ising-nematic ordering

Strong coupling problem:
Infinite number of 2+1
dimensional field theories
at Ising-nematic
quantum critical point

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M.A. Metlitski and S. Sachdev, *Phys. Rev. B* **85**, 075127 (2010)

Conclusions

All quantum phase transitions of metals
in two spatial dimensions
involving symmetry breaking
are strongly-coupled
and
and very different from the
“Stoner” mean field theory

Conclusions

There is an instability of
universal strength to
unconventional superconductivity
near the onset of antiferromagnetism
in a two-dimensional metal

Conclusions

The strong-coupling physics may also apply in three spatial dimensions, but the “Stoner” mean field theory is locally stable.

Conclusions

There can be an intermediate
non-Fermi liquid phase
between the two Fermi liquids:
the antiferromagnetic metal
with “small” Fermi surfaces
and
the metal with “large” Fermi surfaces

Conclusions

This *non-Fermi liquid phase* has neutral $S=1/2$ excitations, and “topological” gauge excitations, which account for deficits in the Luttinger count of the volume enclosed by the Fermi surfaces