Tuning spin and charge order in the cuprate superconductors

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Parent compound of the high temperature superconductors: La_2CuO_4

Mott insulator: square lattice antiferromagnet



Ground state has long-range magnetic Néel order, or a "spin density wave (SDW)"

Néel order parameter: $\boldsymbol{n}_i \sim \eta_i \vec{S}_i$ with $\eta_i = (-1)^{i_x + i_y}$

$$\langle \boldsymbol{n} \rangle \neq 0 \quad ; \quad \left\langle \vec{S}_i \right\rangle \neq 0$$

Introduce mobile carriers of density δ by substitutional doping of out-of-plane ions *e.g.* La_{2- δ}Sr_{δ}CuO₄



Exhibits superconductivity below a high critical temperature T_c

Superconductivity in a doped Mott insulator

BCS superconductor obtained by the Cooper instability of a metallic Fermi liquid



Pair wavefunction $\Psi = \left(k_x^2 - k_y^2\right) \left(\left|\uparrow\downarrow\right\rangle - \left|\downarrow\uparrow\right\rangle\right)$ $\left\langle \vec{S} \right\rangle = 0$

Some <u>*low*</u> temperature properties of the cuprate superconductors appear to be qualitatively similar to those predicted by BCS theory.

Many experiments above T_c are not described quantitatively by BCS theory: this is probably due to strong-coupling "crossover" effects, and I will not discuss this issue further. Superconductivity in a doped Mott insulator

When superconductivity is disrupted at low temperatures, BCS theory predicts that the Fermi surface will reappear.

Instead, we obtain states characterized by <u>competing order parameters</u>.

Theory and experiments indicate that the most likely competing orders are spin and "charge" density waves.

Superconductivity can be suppressed globally by a strong magnetic field or large current flow.

Competing orders are also revealed when superconductivity is suppressed locally, near impurities or around vortices.

S. Sachdev, *Phys. Rev.* B 45, 389 (1992); N. Nagaosa and P.A. Lee, *Phys. Rev.* B 45, 966 (1992);
D.P. Arovas, A. J. Berlinsky, C. Kallin, and S.-C. Zhang *Phys. Rev. Lett.* 79, 2871 (1997);
K. Park and S. Sachdev *Phys. Rev.* B 64, 184510 (2001).

Outline

- I. Phenomenological theory of competing order parameters: phase diagram in a magnetic field.
- II. Neutron scattering and STM observations.
- III. Magnetic quantum phase transitions in the Mott insulator: microstructure of charge order in the Mott insulator and the superconductor.
- IV. Neutron scattering and STM observations
- V. Conclusions



Theory for a system with strong interactions: describe SC and SC+SDW phases by expanding in the deviation from the quantum critical point between them.

- B. Keimer et al. Phys. Rev. B 46, 14034 (1992).
- S. Wakimoto, G. Shirane *et al.*, Phys. Rev. B **60**, R769 (1999).
- G. Aeppli, T.E. Mason, S.M. Hayden, H.A. Mook, J. Kulda, Science 278, 1432 (1997).
- Y. S. Lee, R. J. Birgeneau, M. A. Kastner et al., Phys. Rev. B 60, 3643 (1999).
- J. E. Sonier et al., cond-mat/0108479.
- C. Panagopoulos, B. D. Rainford, J. L. Tallon, T. Xiang, J. R. Cooper, and C. A. Scott, preprint.

I. Phenomenological theory of SDW order

Spin density wave order parameter for general ordering wavevector

$$S_{\alpha}(\mathbf{r}) = \Phi_{\alpha}(\mathbf{r})e^{i\mathbf{K}\cdot\mathbf{r}} + \text{c.c.}$$

 $\Phi_{\alpha}(\mathbf{r})$ is a *complex* field (except for $\mathbf{K} = (\pi, \pi)$ when $e^{i\mathbf{K}\cdot\mathbf{r}} = (-1)^{r_x + r_y}$

Symmetry implies a co-existing "CDW"
$$\delta \rho(\mathbf{r}) \propto S_{\alpha}^{2}(\mathbf{r}) = \sum_{\alpha} \Phi_{\alpha}^{2}(\mathbf{r}) e^{i2K\cdot\mathbf{r}} + \text{c.c.}$$

(modulation in spin-singlet, time-reversal invariant observables, such as the exchange and pairing energy per link, while that in the site charge density may be unobservably small.)



I. Phenomenological theory of SDW order



<u>Dominant effect: **uniform** softening of spin</u> <u>excitations by superflow kinetic energy</u>



E. Demler, S. Sachdev, and Y. Zhang, Phys. Rev. Lett. 87, 067202 (2001).

Main results





II. Neutron scattering measurements of static spin correlations of the superconductor+spin-density-wave (SC+SDW) in a magnetic field

Elastic neutron scattering off La_2CuO_{4+y} B. Khaykovich, Y. S. Lee, S. Wakimoto, K. J. Thomas, M. A. Kastner,

and R.J. Birgeneau, cond-mat/0112505.



a is the only fitting parameter Best fit value - a = 2.4 with $H_{c2} = 60$ T



Neutron scattering of $La_{2-x}Sr_{x}CuO_{4}$ at x=0.1



B. Lake, H. M. Rønnow, N. B. Christensen,
G. Aeppli, K. Lefmann, D. F. McMorrow,
P. Vorderwisch, P. Smeibidl, N. Mangkorntong,
T. Sasagawa, M. Nohara, H. Takagi, T. E. Mason, *Nature*, 415, 299 (2002).



II. <u>STM around vortices induced by a magnetic field in the superconducting state</u>

J. E. Hoffman, E. W. Hudson, K. M. Lang, V. Madhavan, S. H. Pan, H. Eisaki, S. Uchida, and J. C. Davis, *Science* **295**, 466 (2002).



S.H. Pan et al. Phys. Rev. Lett. 85, 1536 (2000).

Vortex-induced LDOS of $Bi_2Sr_2CaCu_2O_{8+\delta}$ integrated from 1meV to 12meV



J. Hoffman E. W. Hudson, K. M. Lang, V. Madhavan, S. H. Pan, H. Eisaki, S. Uchida, and J. C. Davis, *Science* 295, 466 (2002).

Fourier Transform of Vortex-Induced LDOS map

K-space locations of vortex induced LDOS





K-space locations of Bi and Cu atoms

Distances in k –space have units of $2\pi/a_0$ $a_0=3.83$ Å is Cu-Cu distance

J. Hoffman et al. Science, 295, 466 (2002).



Pinning of CDW order by vortex cores in SC phase

Y. Zhang, E. Demler, and S. Sachdev, cond-mat/0112343.

 $\left\langle \Phi_{\alpha}^{2}\left(\boldsymbol{r},\tau\right)\right\rangle \propto\zeta\int d\tau_{1}\left\langle \Phi_{\alpha}\left(\boldsymbol{r},\tau\right)\Phi_{\alpha}^{*}\left(\boldsymbol{r}_{\nu},\tau_{1}\right)
ight
angle ^{2}$



Vortex-induced LDOS of $Bi_2Sr_2CaCu_2O_{8+\delta}$ integrated from 1meV to 12meV



J. Hoffman E. W. Hudson, K. M. Lang, V. Madhavan, S. H. Pan, H. Eisaki, S. Uchida, and J. C. Davis, *Science* 295, 466 (2002).

III. Microstructure of the charge order: magnetic transitions in Mott insulators and superconductors



III. Magnetic ordering transitions in the insulator

$$H = \sum_{i \in J} J_{ij} \quad \vec{S}_i \cdot \vec{S}_j$$

Action for quantum spin fluctuations in spacetime Discretize spacetime into a cubic lattice with Néel order orientation n_a

$$Z = \prod_{a} \int d\boldsymbol{n}_{a} \delta\left(\boldsymbol{n}_{a}^{2} - 1\right) \exp\left(\frac{1}{g} \sum_{a,\mu} \boldsymbol{n}_{a} \cdot \boldsymbol{n}_{a+\mu}\right) \qquad a \to \text{cubic lattice sites;} \qquad \mu \to x, y, \tau;$$

S. Chakravarty, B.I. Halperin, and D.R. Nelson, Phys. Rev. B 39, 2344 (1989).

Quantum path integral for two-dimensional quantum antiferromagnet

 $\Leftrightarrow \quad \text{Partition function of a classical three-dimensional ferromagnet} \\ \text{at a "temperature" } g$

Missing: Spin Berry Phases

iSA



Berry phases profoundly modify paramagnetic states with $\langle n_a \rangle = \langle \vec{S} \rangle = 0$

Computations with Berry phases fully reproduce known states in one dimension: Bethe and Majumdar-Ghosh states for S=1/2, and Haldane states for S=1 K. Park and S. Sachdev, cond-mat/0108214

Field theory of paramagnetic ("quantum disordered") phase Discretize spacetime into a cubic lattice:

$$Z = \prod_{a} \int d\boldsymbol{n}_{a} \delta\left(\boldsymbol{n}_{a}^{2} - 1\right) \exp\left(\frac{1}{g} \sum_{a,\mu} \boldsymbol{n}_{a} \cdot \boldsymbol{n}_{a+\mu} - \frac{i}{2} \sum_{a} \eta_{a} A_{a\tau}\right)$$

 $\eta_a \to \pm 1$ on two square sublattices ; $n_a \sim \eta_a \vec{S}_a \to$ Neel order parameter; $A_{a\mu} \to$ oriented area of spherical triangle formed by n_a , $n_{a+\mu}$, and an arbitrary reference point n_0 $n_0 = n_0'$

Change in choice of n_0 is like a "gauge transformation"

$$A_{a\mu} \to A_{a\mu} - \gamma_{a+\mu} + \gamma_a$$

(γ_a is the oriented area of the spherical triangle formed by n_a and the two choices for n_0).



The area of the triangle is uncertain modulo 4π , and the action is invariant under $A_{a\mu} \rightarrow A_{a\mu} + 4\pi$

These principles strongly constrain the effective action for $A_{a\mu}$

Simplest large g effective action for the $A_{a\mu}$

$$Z = \prod_{a,\mu} \int dA_{a\mu} \exp\left(-\frac{1}{2e^2} \sum_{\Box} \cos\left(\frac{1}{2}\varepsilon_{\mu\nu\lambda}\Delta_{\nu}A_{a\lambda}\right) - \frac{i}{2} \sum_{a} \eta_a A_{a\tau}\right)$$

with $e^2 \sim g^2$

This is compact QED in 2+1 dimensions with Berry phases.

This theory can be reliably analyzed by a duality mapping. The gauge theory is <u>always</u> in a <u>confining</u> phase: There is an energy gap and the ground state has <u>spontaneous bond order</u>.

N. Read and S. Sachdev, *Phys. Rev. Lett.* 62, 1694 (1989).
S. Sachdev and R. Jalabert, *Mod. Phys. Lett.* B 4, 1043 (1990).
K. Park and S. Sachdev, cond-mat/0108214

Square lattice with first(J_1) and second (J_2) neighbor exchange interactions (say)



Studies on the 2D pyrochlore lattice agree with related predictions of theory: J.-B. Fouet, M. Mambrini, P. Sindzingre, C. Lhuillier, cond-mat/0108070. R. Moessner, Oleg Tchernyshyov, S.L. Sondhi, cond-mat/0106286.

N. Read and S. Sachdev, Phys. Rev. Lett. 62, 1694

O. P. Sushkov, J. Oitmaa, and Z. Weihong, Phys. *Rev.* B 63, 104420 (2001).

M.S.L. du Croo de Jongh, J.M.J. van Leeuwen, W. van Saarloos, *Phys. Rev.* B **62**, 14844 (2000).

See however L. Capriotti, F. Becca, A. Parola, cond-mat/0107204.

Bond-centered stripe order in a frustrated S=1/2 XY magnet



A. W. Sandvik, S. Daul, R. R. P. Singh, and D. J. Scalapino, cond-mat/0205270

Framework for spin/charge order in cuprate superconductors





C. Castellani, C. Di Castro, and M. Grilli, Phys. Rev. Lett. 75, 4650 (1995).

IV. STM image of pinned charge order in $Bi_2Sr_2CaCu_2O_{8+\delta}$ in zero magnetic field



C. Howald, H. Eisaki, N. Kaneko, and A. Kapitulnik, cond-mat/0201546

Spectral properties of the STM signal are sensitive to the microstructure of the charge order



Measured energy dependence of the Fourier component of the density of states which modulates with a period of 4 lattice spacings

C. Howald, H. Eisaki, N. Kaneko, and A. Kapitulnik, cond-mat/0201546



Theoretical modeling shows that this spectrum is best obtained by a modulation of bond variables, such as the exchange, kinetic or pairing energies.

> M. Vojta, cond-mat/0204284. D. Podolsky, E. Demler, K. Damle, and B.I. Halperin, condmat/0204011

IV. Neutron scattering observation of static charge order in $YBa_2Cu_3O_{6.35}$ (spin correlations are dynamic)



Charge order period = 8 lattice spacings

FIG. 1. Measurements of the charge order for YBCO6.35. (a) Measurements obtained at a small momentum transfer so the results are not affected by impurity powder lines. Powder lines were also avoided around the (1.125, 0, 1.3) r.l.u. position shown in (b). The lines are Gaussian fits to the data. In (a) 200 and (b) 100 additional counts were added onto successive scans so the data could be presented on the same plot. The scattering broadens at higher temperatures.

H. A. Mook, Pengcheng Dai, and F. Dogan Phys. Rev. Lett. **88**, 097004 (2002).



See also J. Zaanen, *Physica* C 217, 317 (1999),
S. Kivelson, E. Fradkin and V. Emery, *Nature* 393, 550 (1998),
S. White and D. Scalapino, *Phys. Rev. Lett.* 80, 1272 (1998).
C. Castellani, C. Di Castro, and M. Grilli, *Phys.Rev. Lett.* 75, 4650 (1995).

Conclusions

- I. Cuprate superconductivity is associated with doping Mott insulators with charge carriers
- II. The correct paramagnetic Mott insulator has chargeorder and confinement of spinons
- III. Mott insulator reveals itself vortices and near impurities. Predicted effects seen recently in STM and NMR experiments.
- IV. Semi-quantitative predictions for neutron scattering measurements of spin-density-wave order in superconductors; theory also establishes connection to STM experiments.
- V. Future experiments should search for SC+SDW to SC quantum transition driven by a magnetic field.
- VI. Major open question: how does understanding of low temperature order parameters help explain anomalous behavior at high temperatures ?