

# Universal conductance of nanowires near the superconductor-metal quantum transition

Subir Sachdev (Yale)  
Philipp Werner (ETH)  
Matthias Troyer (ETH)

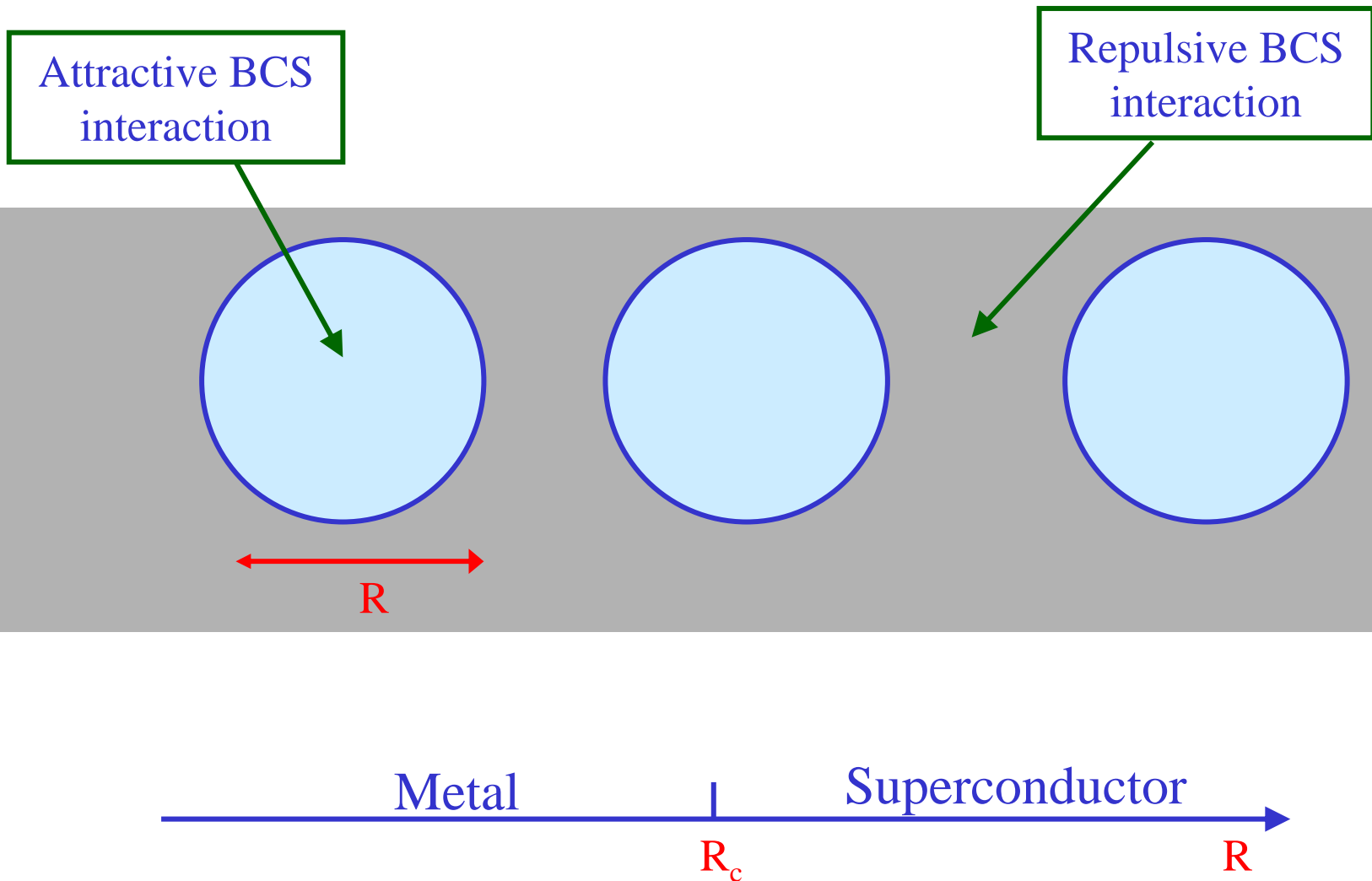
*cond-mat/0402431*



Talk online:  
Google Sachdev

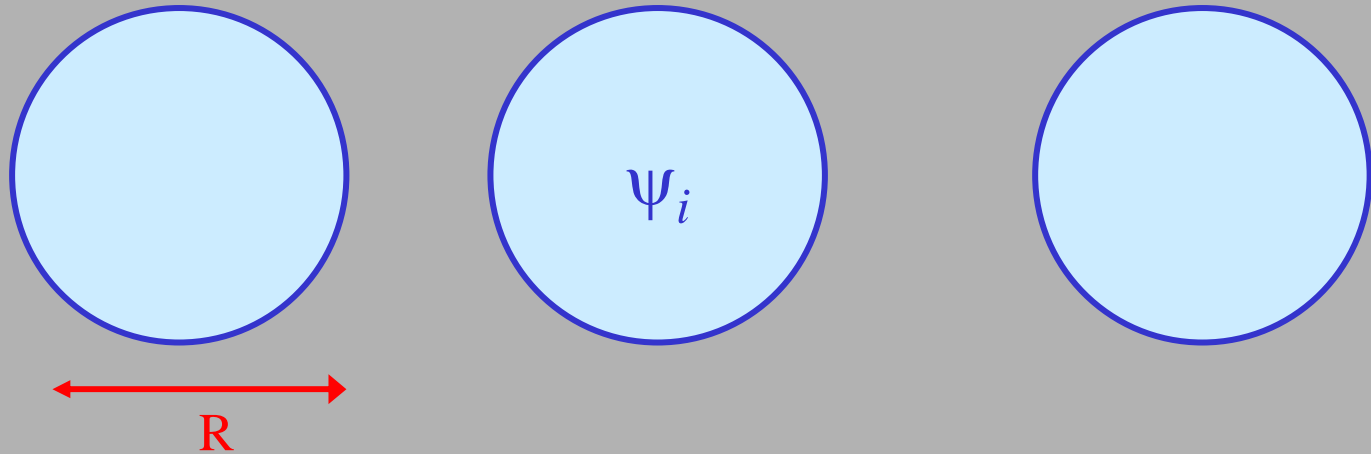


# $T=0$ Superconductor-metal transition



M.V. Feigel'man and A.I. Larkin, *Chem. Phys.* **235**, 107 (1998)  
B. Spivak, A. Zyuzin, and M. Hruska, *Phys. Rev. B* **64**, 132502 (2001).

# $T=0$ Superconductor-metal transition



$$\mathcal{S} = - \int d\tau \sum_{i,j} J_{ij} \psi_i^*(\tau) \psi_j(\tau) - \int d\tau d\tau' \sum_i \frac{\psi_i^*(\tau) \psi_i(\tau')}{(\tau - \tau')^2}$$

# Continuum theory for quantum critical point

$$\mathcal{S}_{\text{bulk}} = \frac{A}{\hbar} \int_0^L dx \left[ \int_0^\beta d\tau \left( \delta |\partial_x \psi|^2 + a |\psi|^2 + \frac{b}{2} |\psi|^4 \right) + \frac{\hbar \gamma}{\beta} \sum_{\omega_n} |\omega_n| |\psi(x, \omega_n)|^2 \right],$$

Obeys strong hyperscaling properties in spatial dimensions  $d < 2$ .

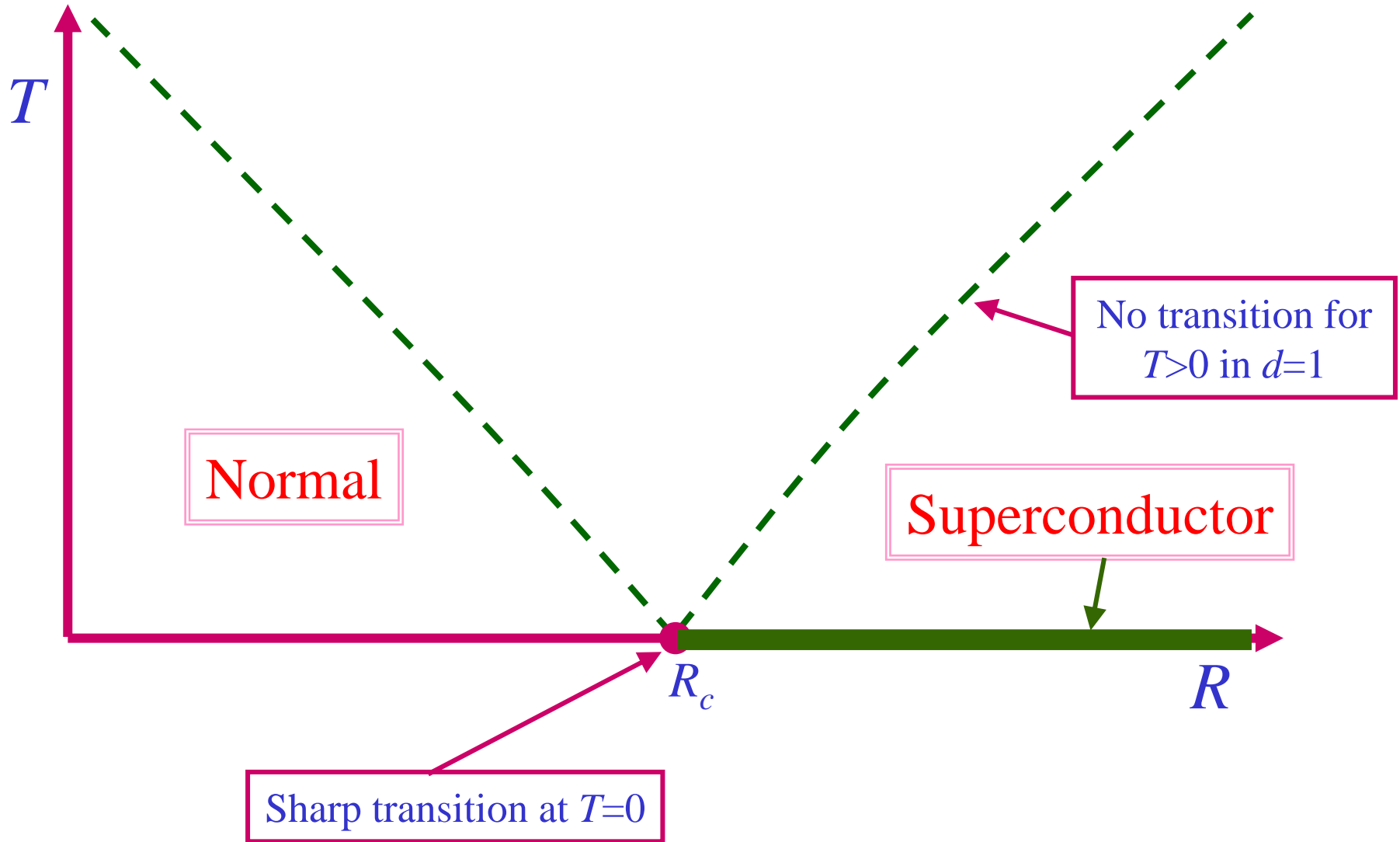
Critical properties can be determined by an expansion in  $\epsilon = 2 - d$  in a theory with  $n$ -component fields ( $n = 2$  here).

$$z = 2 - \eta$$

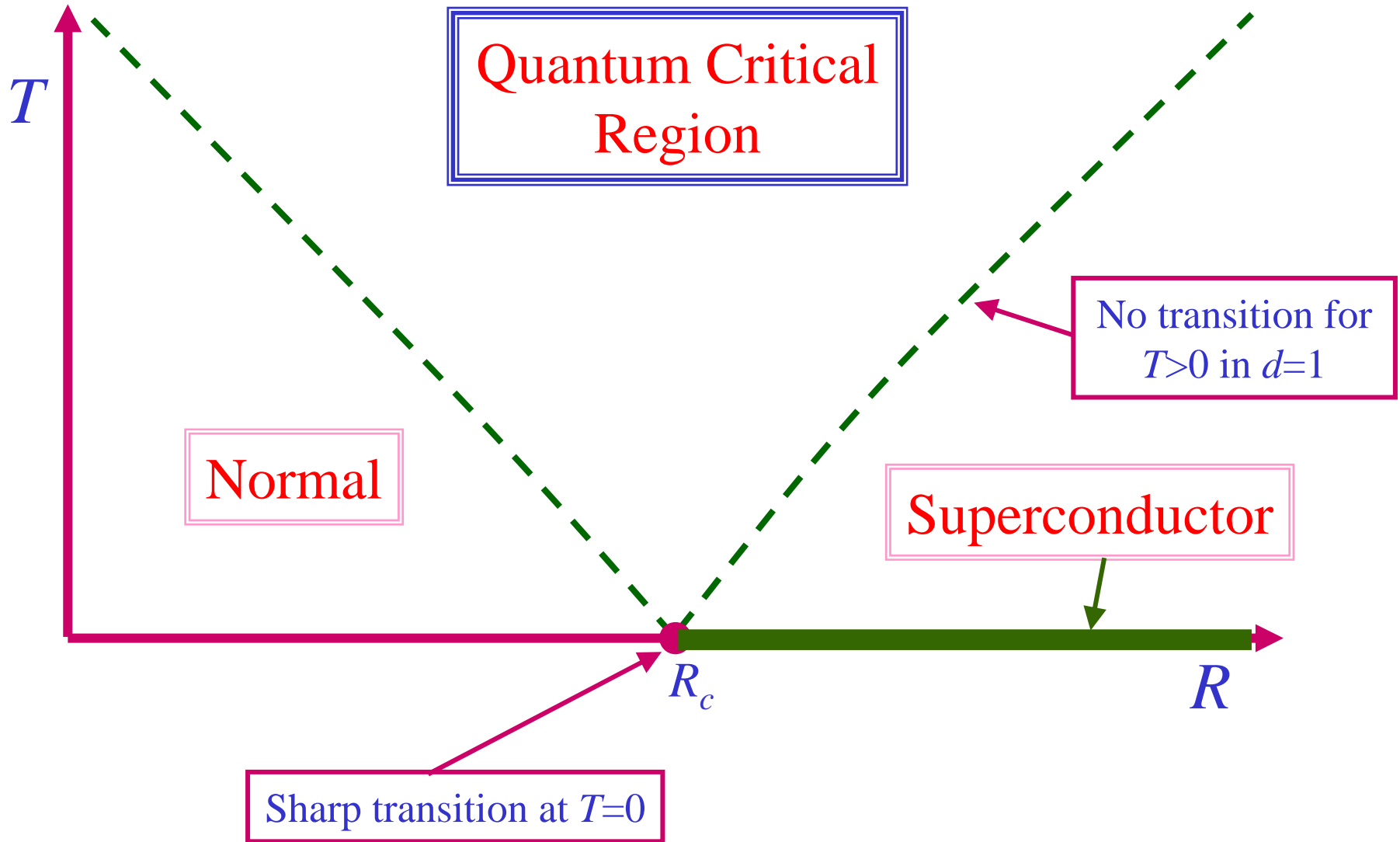
$$\eta = \frac{(n+2)(12 - \pi^2)}{4(n+8)^2} \epsilon^2$$

$$\nu = \frac{1}{2} + \frac{(n+2)}{4(n+8)} \epsilon + \frac{(n+2)(n^2 + (38 - 7\pi^2/6)n + 132 - 19\pi^2/3)}{8(n+8)^3} \epsilon^2$$

# Consequences of hyperscaling



# Consequences of hyperscaling



# Consequences of hyperscaling

## Quantum Critical Region

The conductance  $g$  obeys

$$g = \frac{4e^2}{h} \Phi \left( c_1 T L^z, \frac{\hbar\omega}{k_B T} \right)$$

where  $\Phi$  is a universal function and only constant  $c_1$  is non-universal.

For  $L > (c_1 T)^{-1/z}$ , we have hydrodynamic, “incoherent” transport and  $g = \sigma/L$ , where  $\sigma$  is the conductivity which is *independent of the leads* and obeys

$$\sigma = \frac{4e^2}{h} \frac{1}{(c_1 T)^{1/z}} \Phi_1 \left( \frac{\hbar\omega}{k_B T} \right)$$

# Consequences of hyperscaling

## Quantum Critical Region

The conductance  $g$  obeys

$$g = \frac{4e^2}{h} \Phi \left( c_1 T L^z, \frac{\hbar\omega}{k_B T} \right)$$

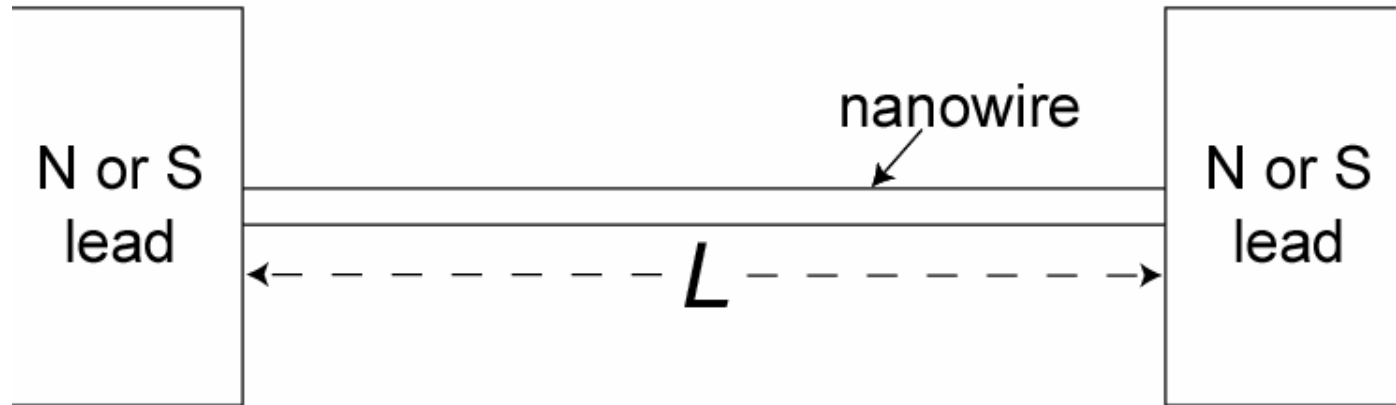
where  $\Phi$  is a universal function and only constant  $c_1$  is non-universal.

For  $L < (c_1 T)^{-1/z}$ , we have “coherent” transport, and the d.c. conductance is independent of  $L$ , but sensitive to the nature of the leads.

$$g = \frac{4e^2}{h} F(c_1 \omega L^z)$$



## Effect of the leads



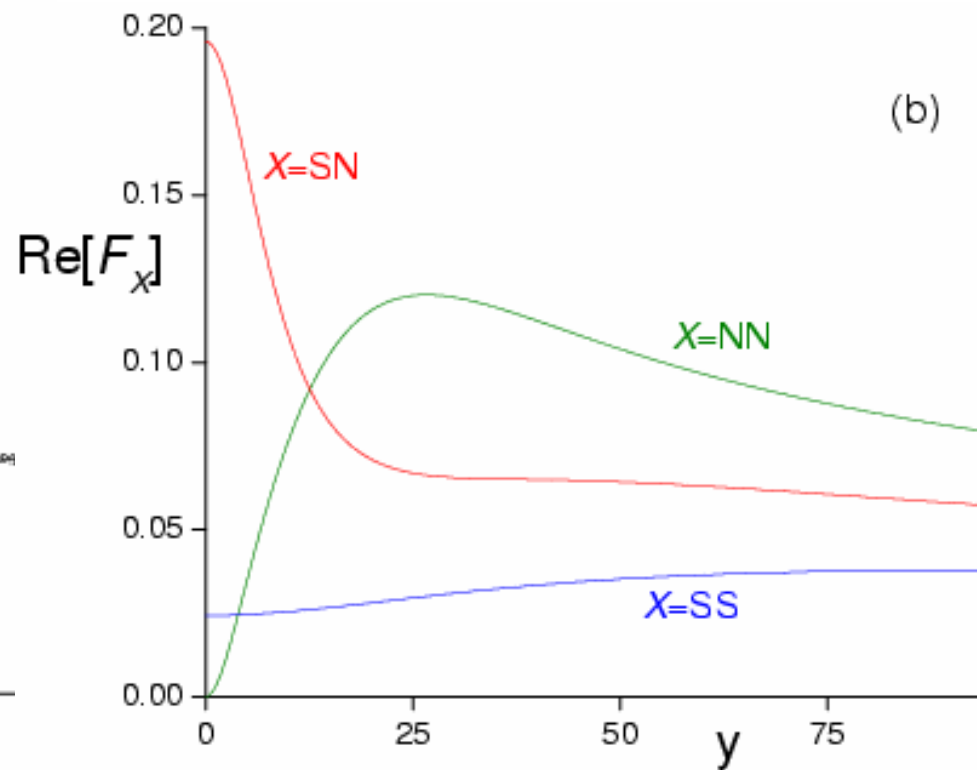
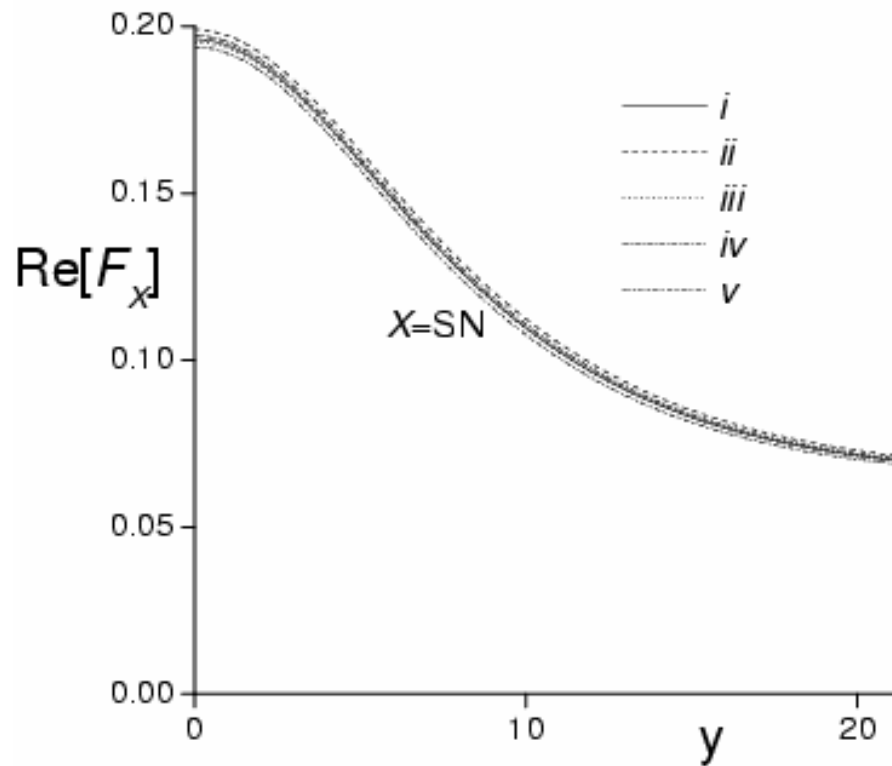
$$\mathcal{S}_{\text{lead}} = \int d\tau \left[ -H^* \psi(0, \tau) - H \psi^*(0, \tau) + C |\Psi(0, \tau)|^2 \right]$$

where  $H \neq 0$  for a superconducting lead.

Both  $H$  and  $C$  scale to strong-coupling, and therefore we have Dirichlet boundary conditions ( $\Psi = 0$ ) for a N lead, and Fixed boundary conditions for a S lead

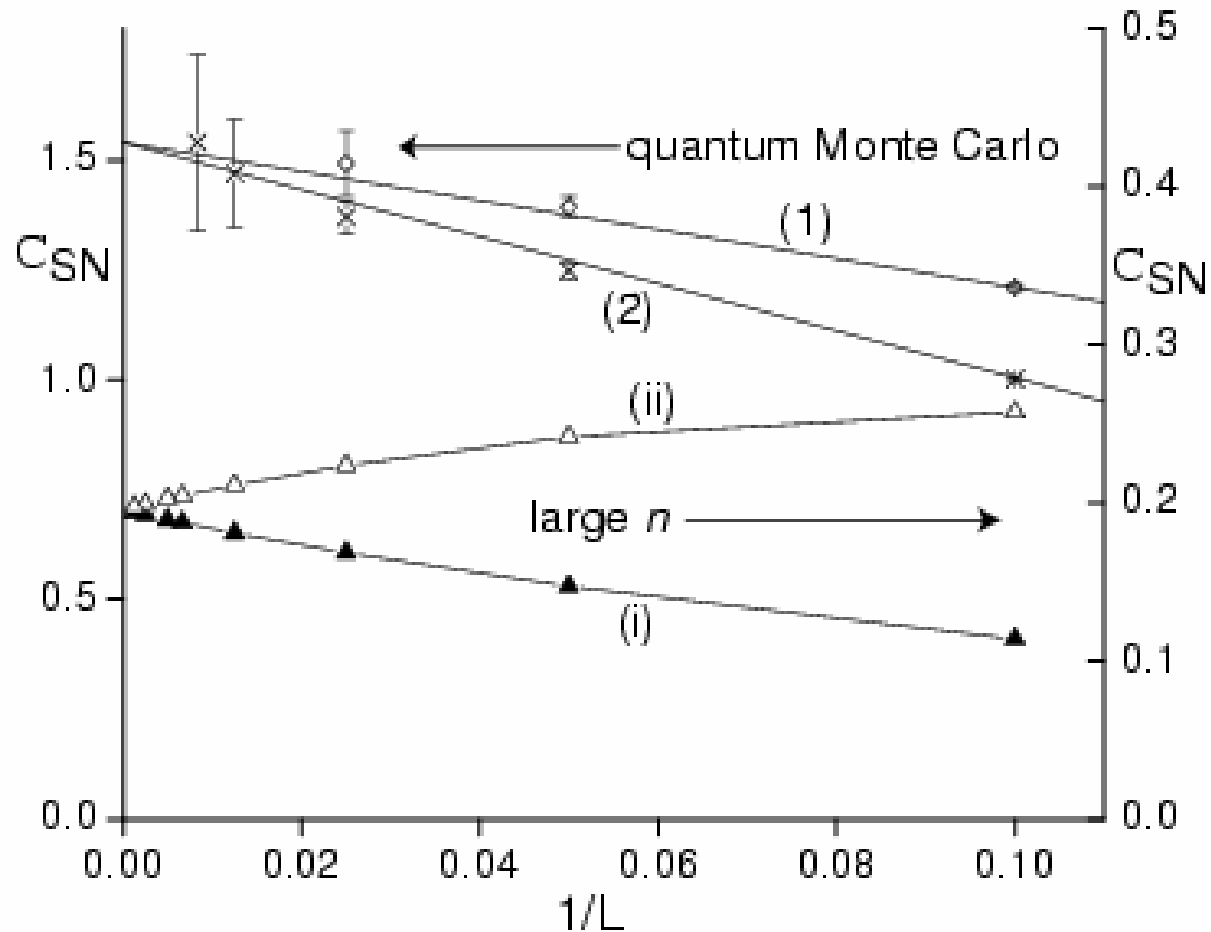
Conductance is *independent* of the specific bare values of  $H$  and  $C$ .

# Large $n$ computation of conductance



$$g = \frac{4e^2}{h} F_X(y) \quad ; \quad y = c_1 \omega L^z$$

# Quantum Monte Carlo and large $n$ computation of d.c. conductance



$$g = \frac{4e^2}{h} C_{SN}$$

## Conclusions

- Universal transport in wires near the superconductor-metal transition
- Theory includes contributions from thermal and quantum phase slips ---- reduces to the classical LAMH theory at high temperatures
- Sensitivity to leads should be a generic feature of the ``coherent'' transport regime of quantum critical points.